

**ELECTRON, ION AND ATOM
COLLISIONS LEADING TO
ANOMALOUS DOPPLER
BROADENING IN HYDROGEN
AND HYDROGEN RARE GAS
MIXTURES**

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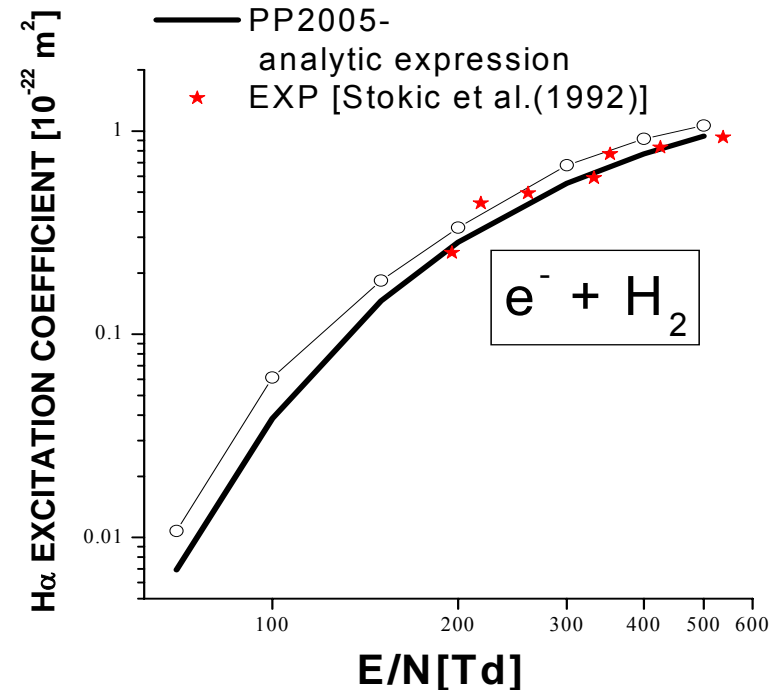
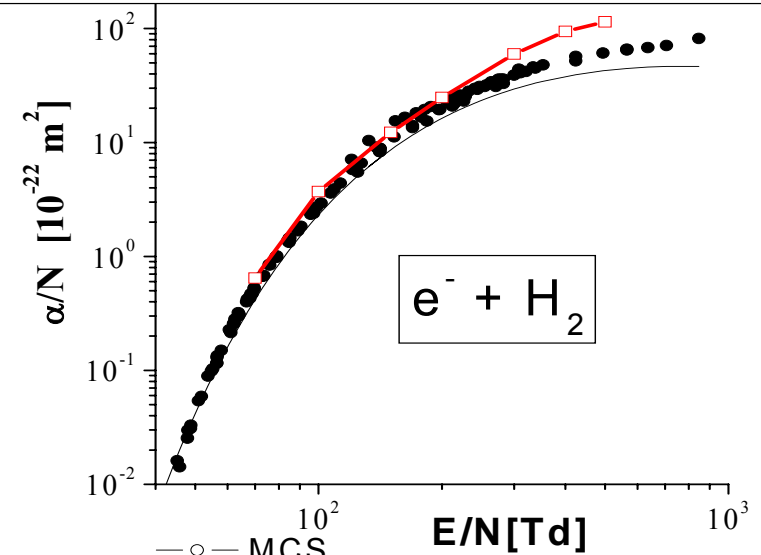
Cross section set for electron scattering on H₂

• *Table E. Processes for electron scattering on H₂. Isotropic scattering.*

No	Process	Threshold [eV]
• 1)	elastic scattering	0.000
• 2)	J=0→J=2	0.044
• 3)	J=1→J=3	0.073
• 4)	Vibrational excitation (v=1)	0.516
• 5)	Vibrational excitation (v=2)	1.000
• 6)	Vibrational excitation (v=3)	1.500
• 7)	B ³ Σ excitation	8.900
• 8)	B ¹ Σ excitation	11.300
• 9)	C ³ Π excitation	11.750
• 10)	A ³ Σ excitation	11.800
• 11)	C ¹ Π excitation	12.400
• 12)	G ¹ Σ (v=2) excitation	13.860
• 13)	D ³ Π	14.000
• 14)	DISS. EXC.(N=2) Lyman α	15.000
• 15)	RYDBERG SUM	15.200
• 16)	IONIZATION (Rapp and EG)	15.400
• 17)	DISSOC.EXC (N=3) Ha	16.600

Electron impact dissociative ionization is included by introducing branching of 7 % to ionization cross section.

• Dutton (1975)
 —□— MCS(isotropic)
 ——— Phelps and Petrovic(2005) fit

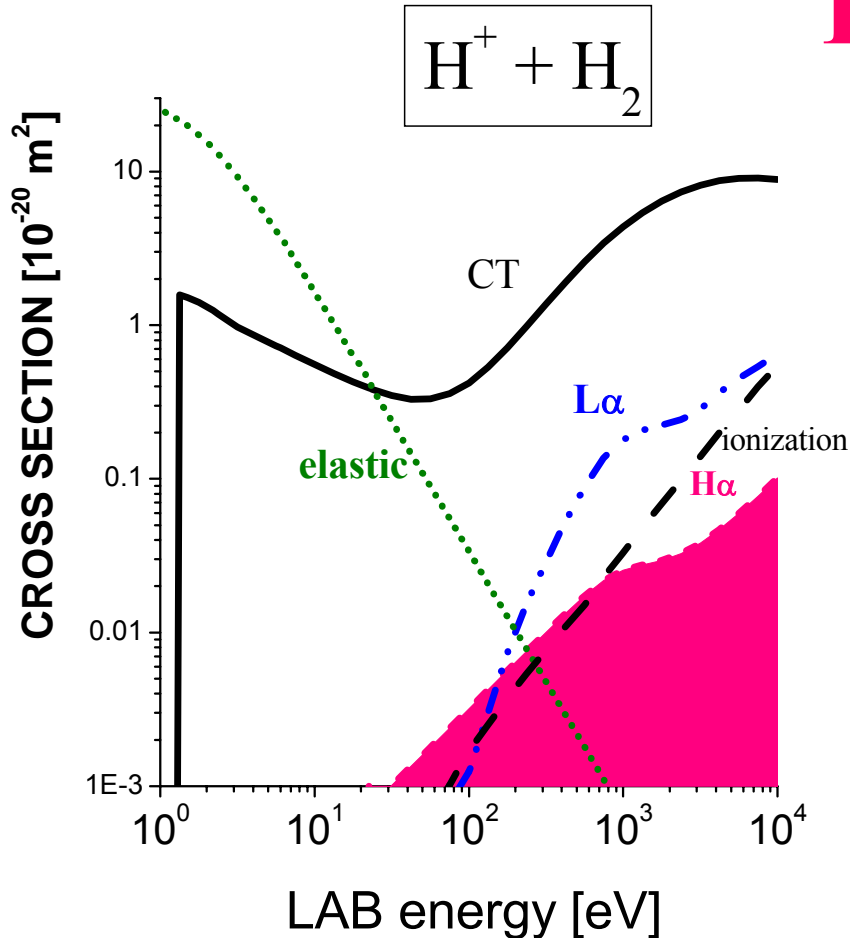


Heavy particle cross sections

- These cross sections (PP2005) are based on Phelps (1990) data and are modified to fit spatial excitation and Doppler broadened profile of H α excitation in Townsend discharge by his multibeam method.

PP2005 – Phelps and Petrovic (2005)

H⁺ + H₂ cross sections



No	Process by product	Anisotropy	CMS threshold [eV]	LAB threshold [eV]
1)	elastic scattering (an)	Isotropic	0	0
2)	CT (an) Prod. of slow H ₂ ⁺ , fast H	Forward	0.66667	1.0
3)	Lyman α....[P1990]	Forward	11.9	17.85
4)	Hα production (an)	Forward	13.3333	20.0
5)	ionization [P1990] [§]	Forward	15.4	23.1

Vib-Vibrational excitation cross section is sum of v=0-1,0-2,0-3 transitions, from P1990 and is used only in P2006.

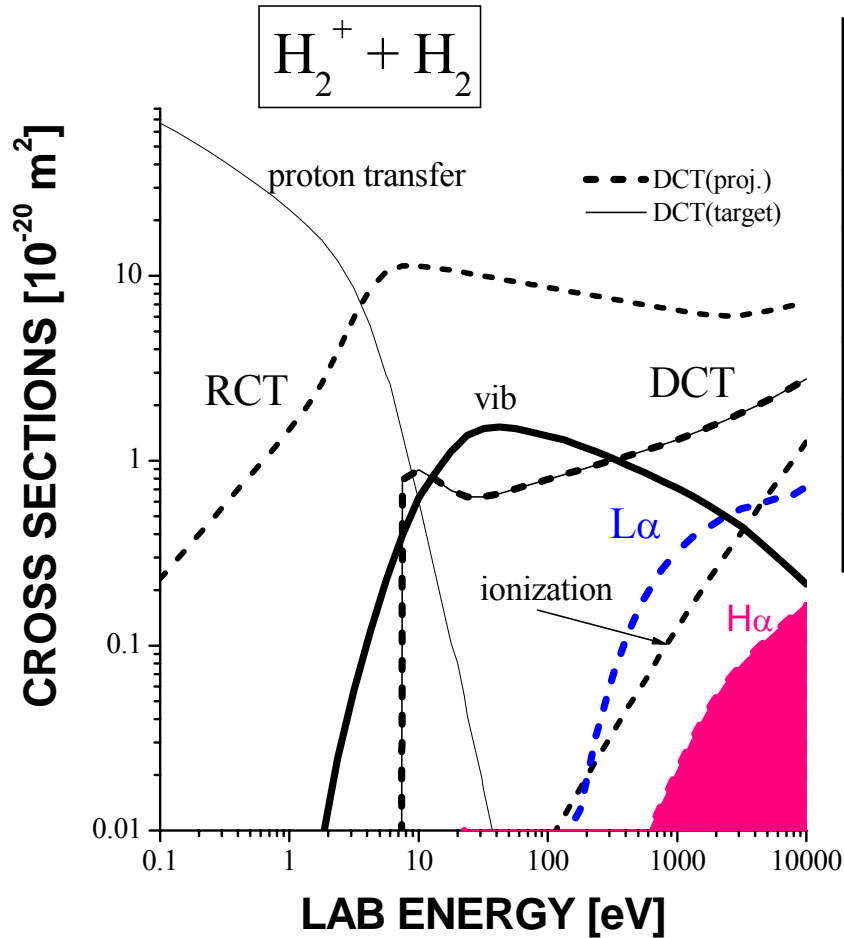
an – analytic cross section (PP2005).

[§] - production of H₂⁺

P1990 – A. V. Phelps, J.Phys.Chem.Ref.Data,19(3) (1990).

CT – charge transfer

$\text{H}_2^+ + \text{H}_2$ cross sections



No	Process by product	Anisotropy	CMS threshold [eV]	LAB threshold [eV]
1)	$\text{H}_3^+ + \text{H}$ (an)	Isotropic	0	0
2)	$\text{H}_2(v=1)$ [P1990]	Forward	0.516	1.032
3)	DCT proj (an)	Forward	3	6
4)	DCT target (an)	Forward	3	6
5)	Lyman α [P1990]	Forward	11.3	22.6
6)	e- prod. [P1990] ^s	Forward	15.4	30.8
7)	H_α excitation (an)	Forward	10	20

an – analytic cross section (PP2005),

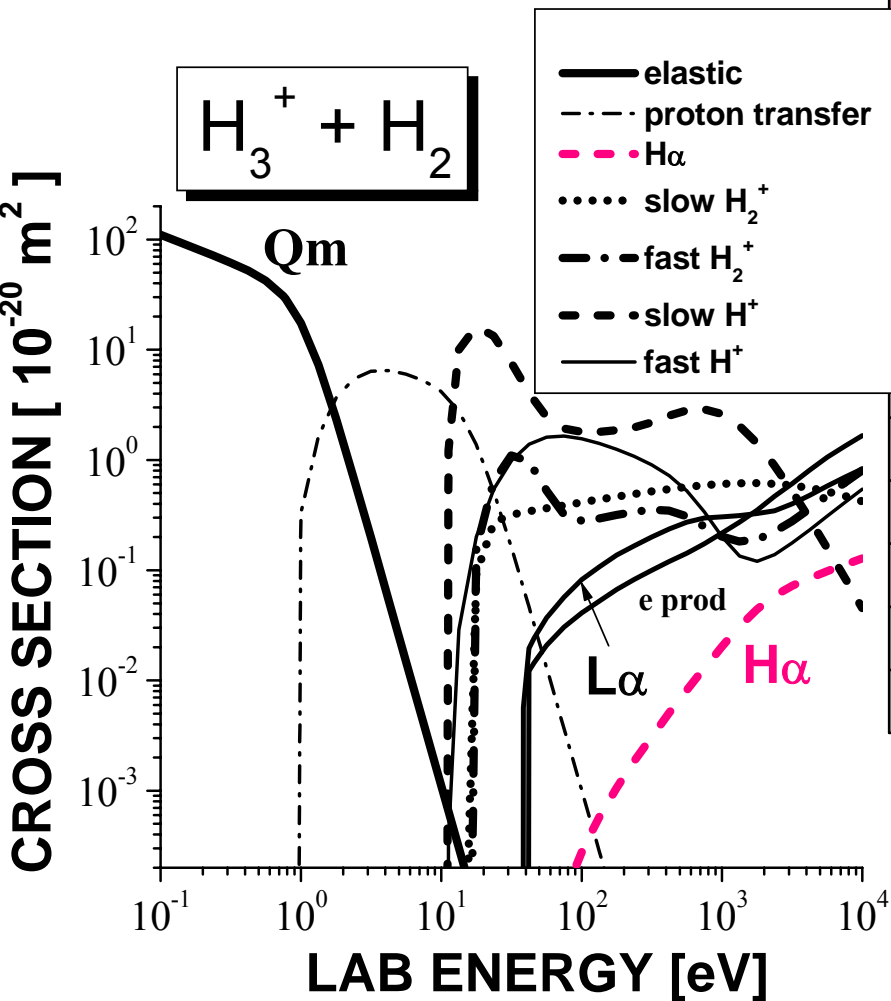
^s - production of H_2^+ ,

P1990 – A.V. Phelps, J.Phys.Chem.Ref.Data,**19**(3) (1990),

RCT – resonant charge transfer,

DCT - dissociative charge transfer.

$\text{H}_3^+ + \text{H}_2$ cross sections

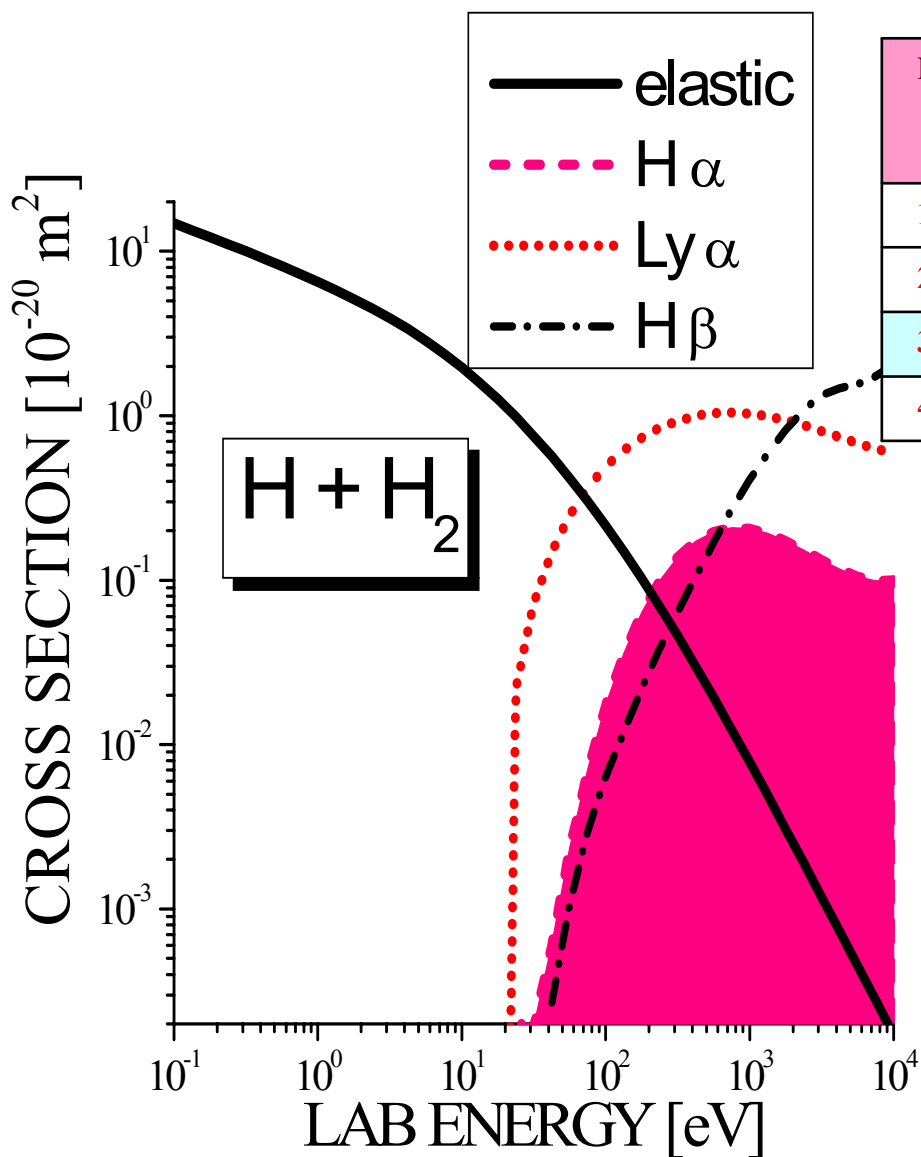


No	Process by product	Aniso-tropy	CMS Thres-hold [eV]	LAB Thres-hold [eV]
1)	elastic scattering (an)	Isotropic	0	0
2)	Proton transfer (an)	Backward	0.312	0.78
2)	fast H_2^+ (an)	Forward	6.2	15.5
3)	fast H^+ (an)	Forward	4.4	11
4)	fast $\text{H}_2 +$ slow H^+ (an)	Backward	4.4	11
5)	fast $\text{H} +$ slow H_2^+ (an)	Backward	6.2	15.5
6)	$\text{H}\alpha$ excitation (an)	Forward	18.32	45.8
7)	Lyman α [P1990]	Forward	15.4	37
8)	e- prod. (e^-, H_2^+) [P1990]	Forward	14.8	38.5

an – analytic cross section -PP2005.

P1990 – A.V. Phelps, J.Phys.Chem.Ref.Data,19(3) (1990).

(fast)H + H₂ cross sections

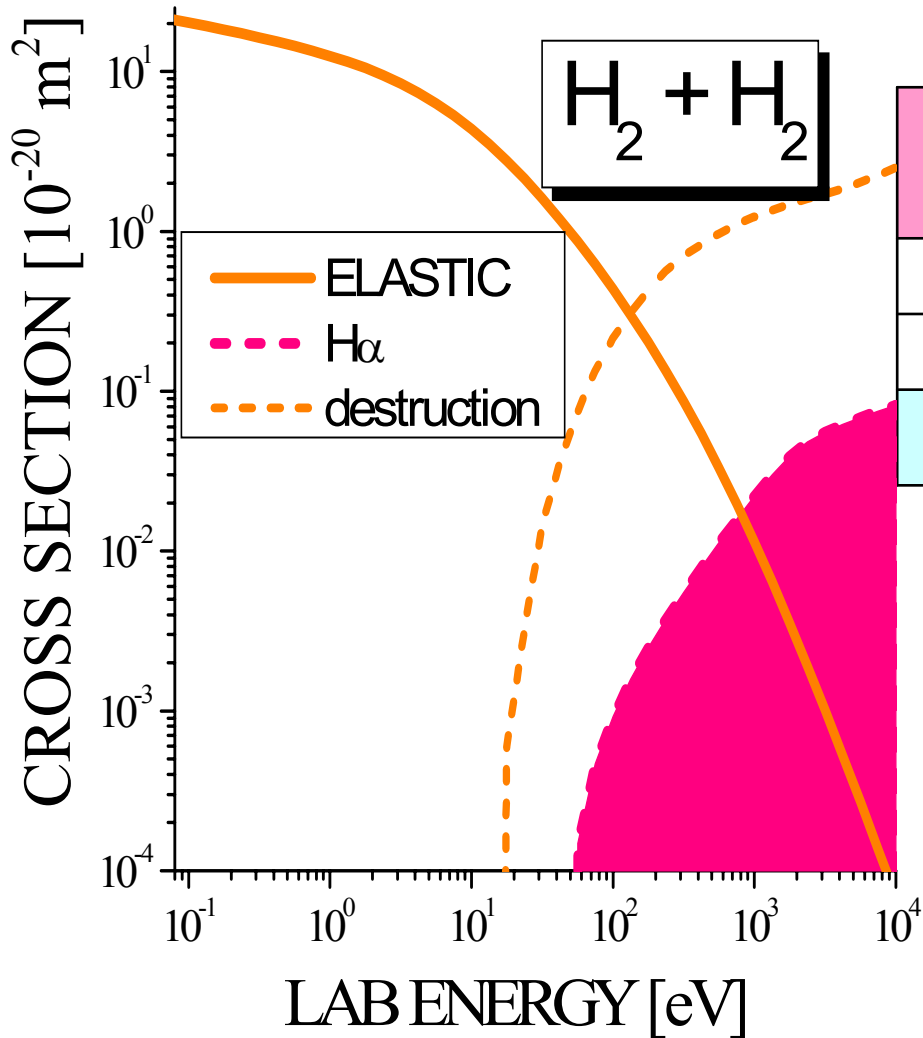


No	Process by product	Anisotropy	CMS threshold [eV]	LAB threshold [eV]
1)	elastic scattering (an)	Isotropic	0	0
2)	H α excitation (an)	Forward	17.333	26.0
3)	H β excitation [P1990]	Forward	17.000	25.5
4)	L α excitation (an)	Forward	12.000	18.0

an – analytical cross section (PP2005).

P1990 – A.V. Phelps, J.Phys.Chem.Ref.Data,**19**(3) (1990).

(fast)H₂ + H₂ cross sections



No	Process by product	Anisotropy	CMS threshold [eV]	LAB threshold [eV]
1)	elastic scattering (an)	Isotropic	0	0
2)	H α excitation (an)	Forward	22.90	45.8
3)	H ₂ destruction [(f)H formation] [P1990]	Forward	4.4781*	8.9562

an – analytic cross section (PP2005).

P1990 – A.V. Phelps, J.Phys.Chem.Ref.Data,**19**(3) (1990).

* E.W. Mc Daniel, 1989, Atomic Collisions, Electron and Photon Projectiles, p.655. Cross section for H₂ destruction is tabulated from 17.78 eV. Cross section is linearly extrapolated to 0 at 8.9562 eV. It is assumed that destruction proceeds via projectile dissociation.

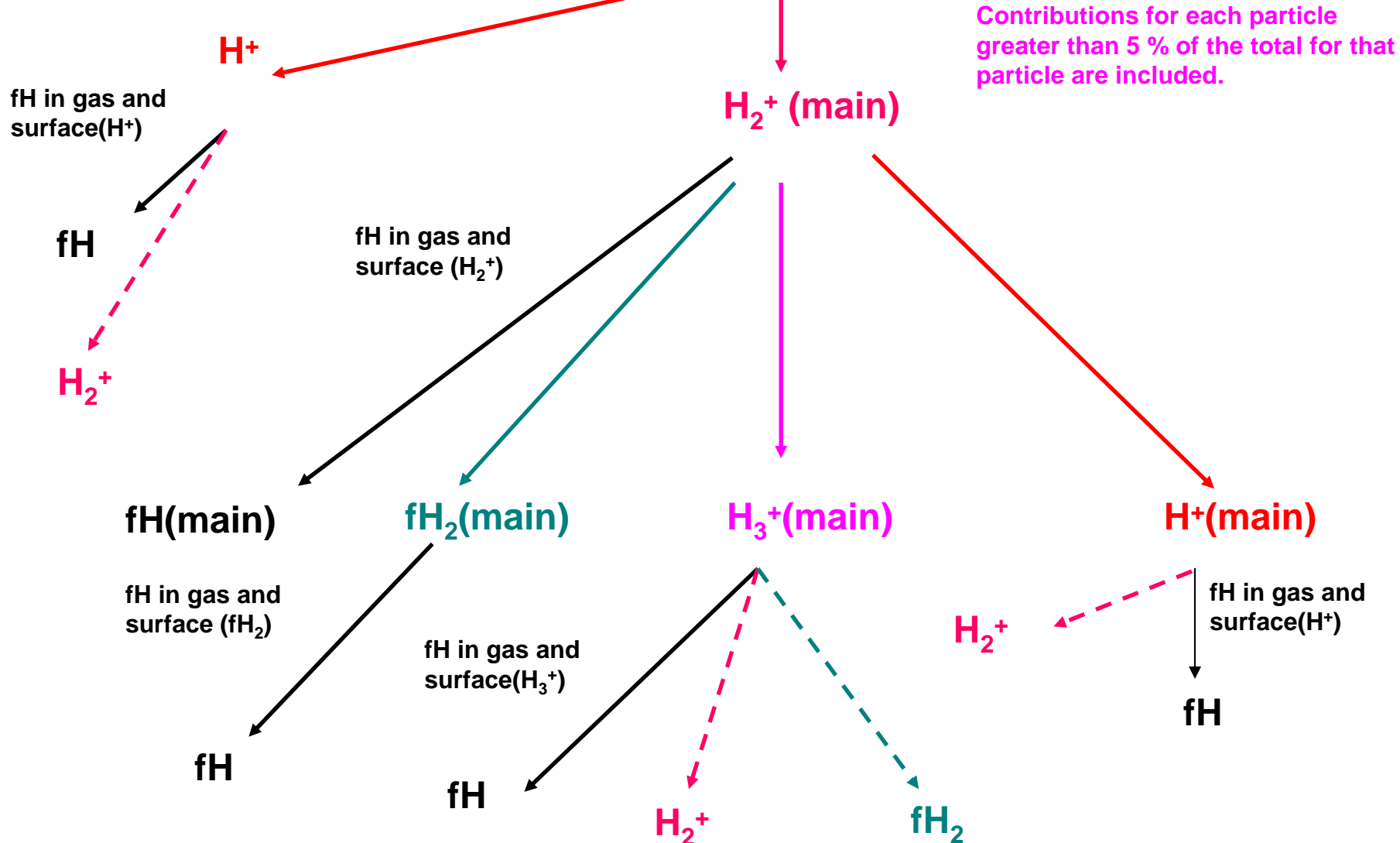
Modeling heavy particle refl. on surface

1. Each charged particle born in the discharge (H^+ , H_2^+ , H_3^+) is **neutralized** at the surface.
2. H^+ , H_2^+ and H_3^+ form one, two and three **H atoms** upon reflection from the surface, respectively, with 2/3 of the incoming energy per particle, and 50 % probability of escape
3. Impact of **fast H** results only in backward reflection; impact of **fast H_2** produces two **H atoms** with 2/3 of incoming energy per particle, also with 50 % probability of escape
4. H atoms are followed backward ONLY if they have kinetic energy sufficient to excite **$H\alpha$** .
5. Fast H atoms are **backscattered diffusely** (cosine distribution).
6. Anode is assumed to be a perfect absorber for all particles ($R_a=0$).

Monte Carlo Code

$e^- + H_2$ Ionization of H_2

DI



Monte Carlo Simulation RESULTS

$E/N=10$ kTd, $E=609.5$ V/cm, $p=185$ mTorr, $d=3.9$ cm

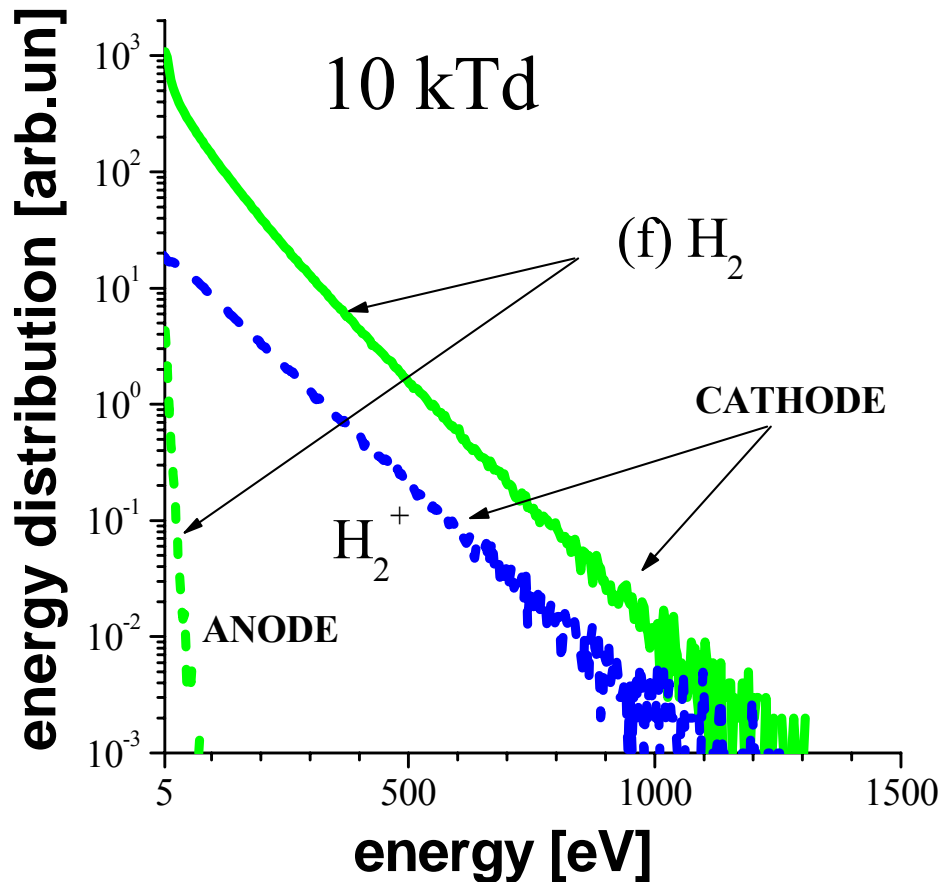
Heavy particle *membrane* energy distributions of particles approaching the cathode and the anode

H_2^+ ions and (f) H_2

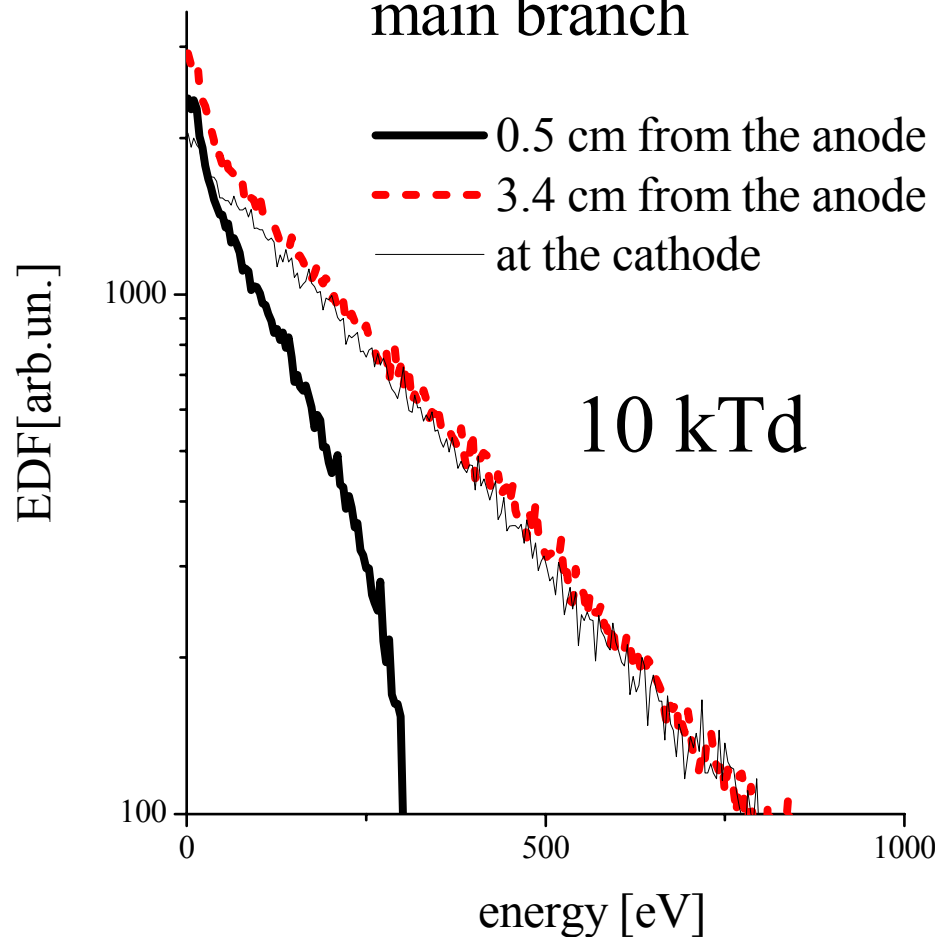
PP2005

Branch e, H_2^+ , H_2

10 kTd



H_3^+ ions
main branch

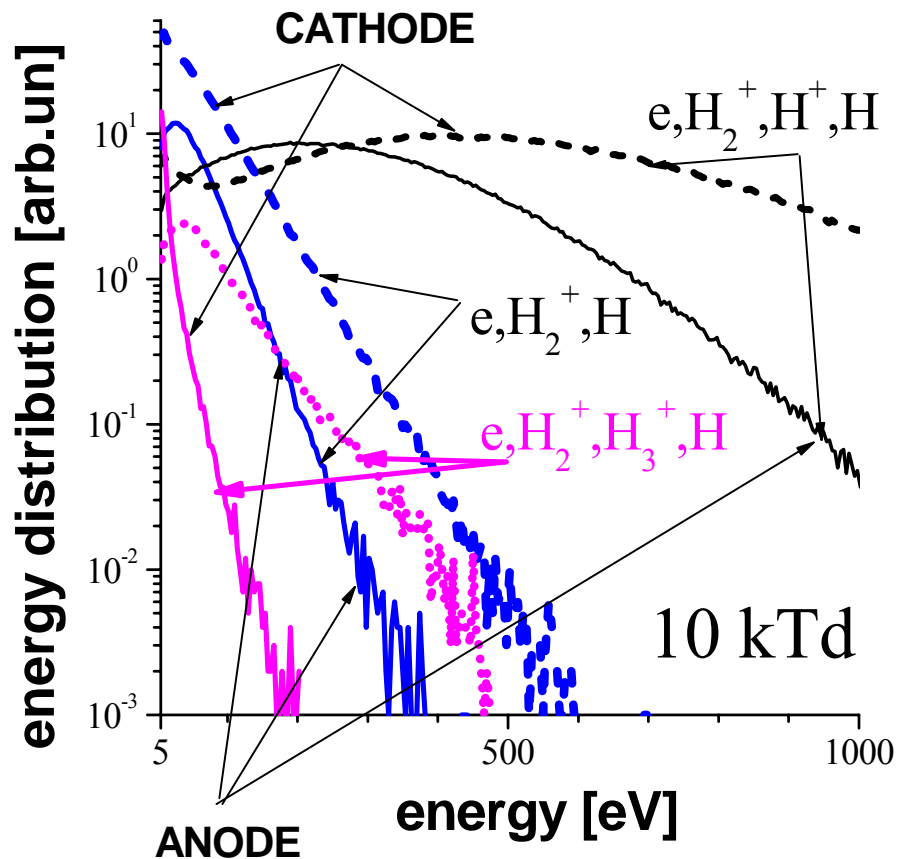


MOST IMPORTANT CONTRIBUTION – FAST H ATOMS

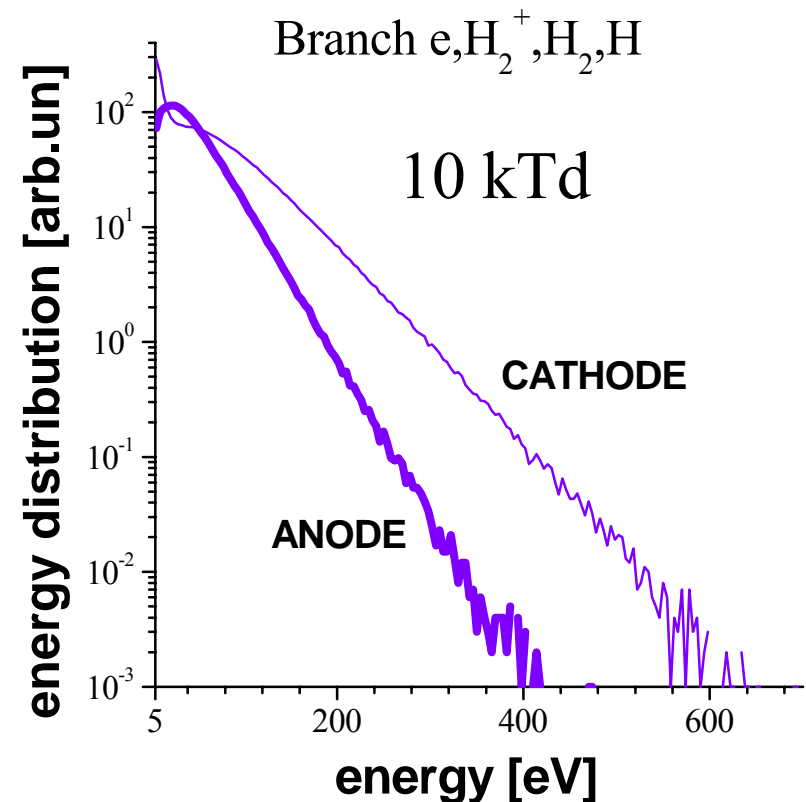
MEMBRANE ENERGY DISTRIBUTION OF fast H ATOMS
ARRIVING TO THE ELECTRODES

PP2005

ionic contributions to (f)H



(f)H₂ contribution to (f)H



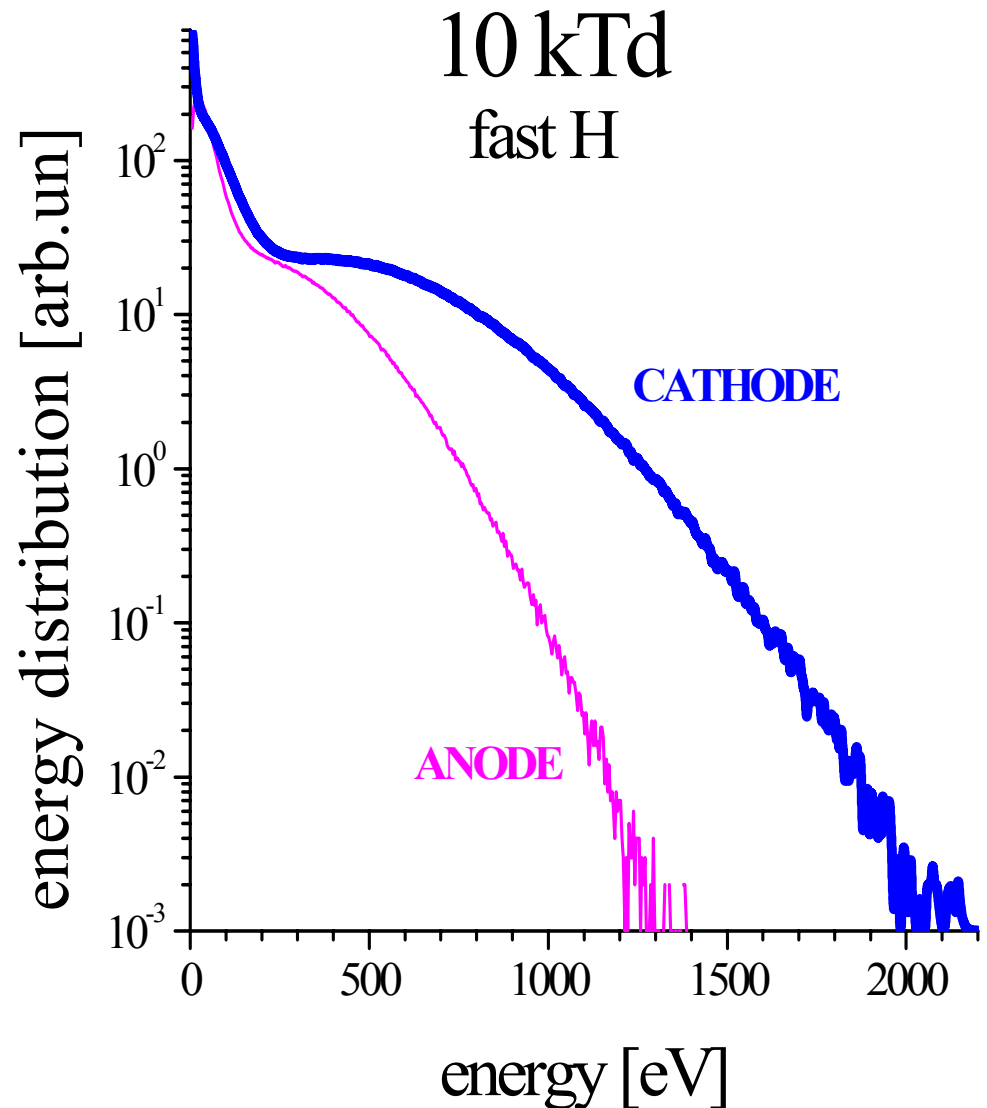
MEMBRANE ENERGY DISTRIBUTION OF fast H ATOMS ARRIVING TO THE ELECTRODES

Contribution of all particles
to (f)H energy distribution

EDF is shaped by

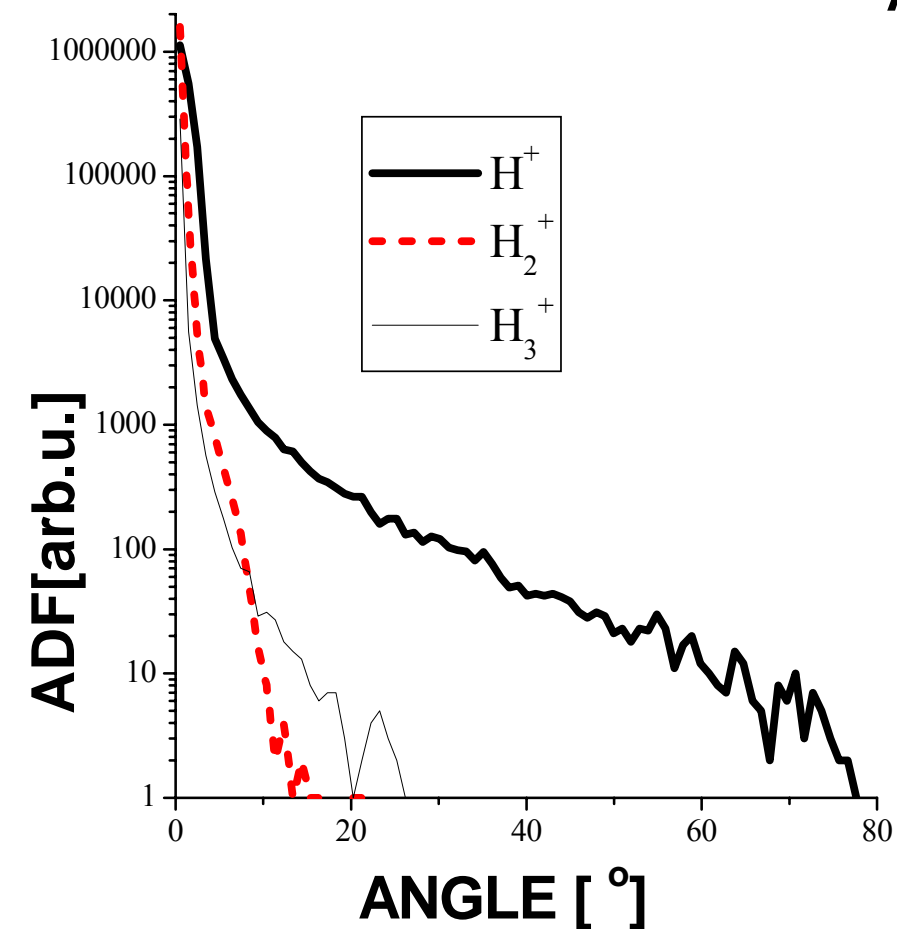
* H^+ ions at high energy

* H_2^+ and H_3^+ ions at
moderate and low energy



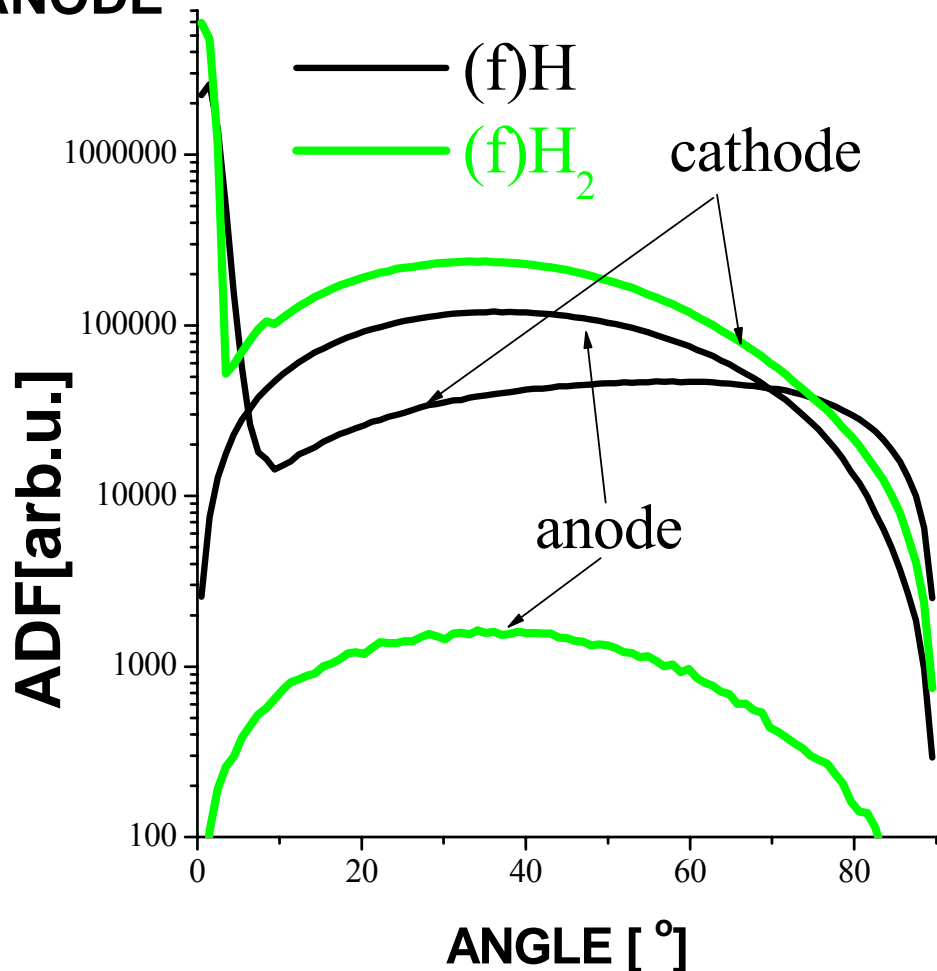
ANGULAR DISTRIBUTION OF PARTICLES AT THE ELECTRODES

**CHARGED PARTICLES
FORWARD PEAKED AT THE
CATHODE**



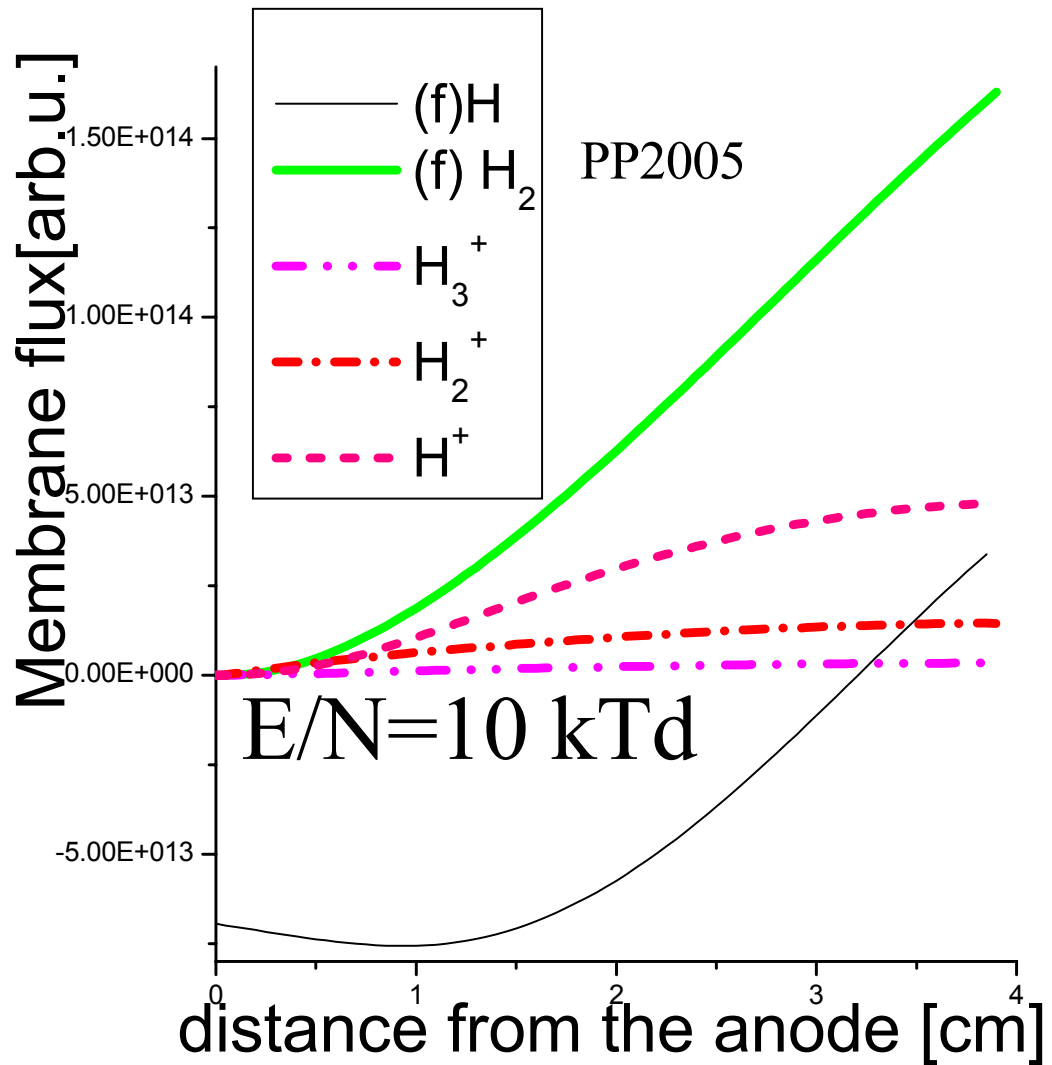
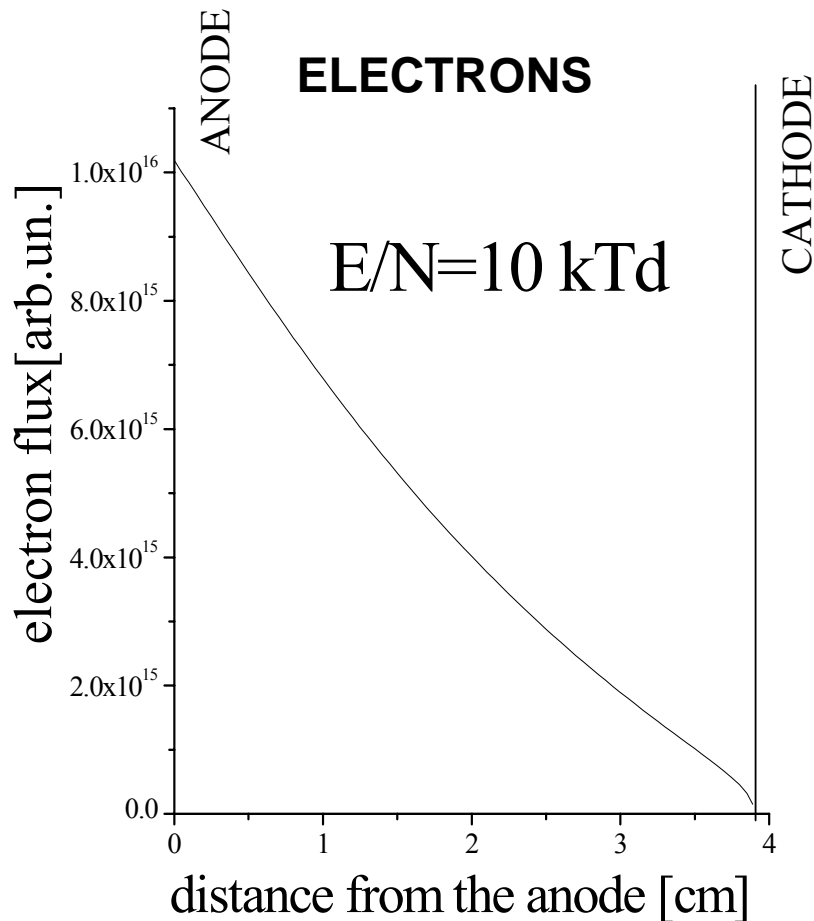
no angular dependence of reflection coefficient
PP2005

**(fn) FORWARD PEAKED AT THE
CATHODE
ISOTROPICALLY ARRIVING AT THE
ANODE**

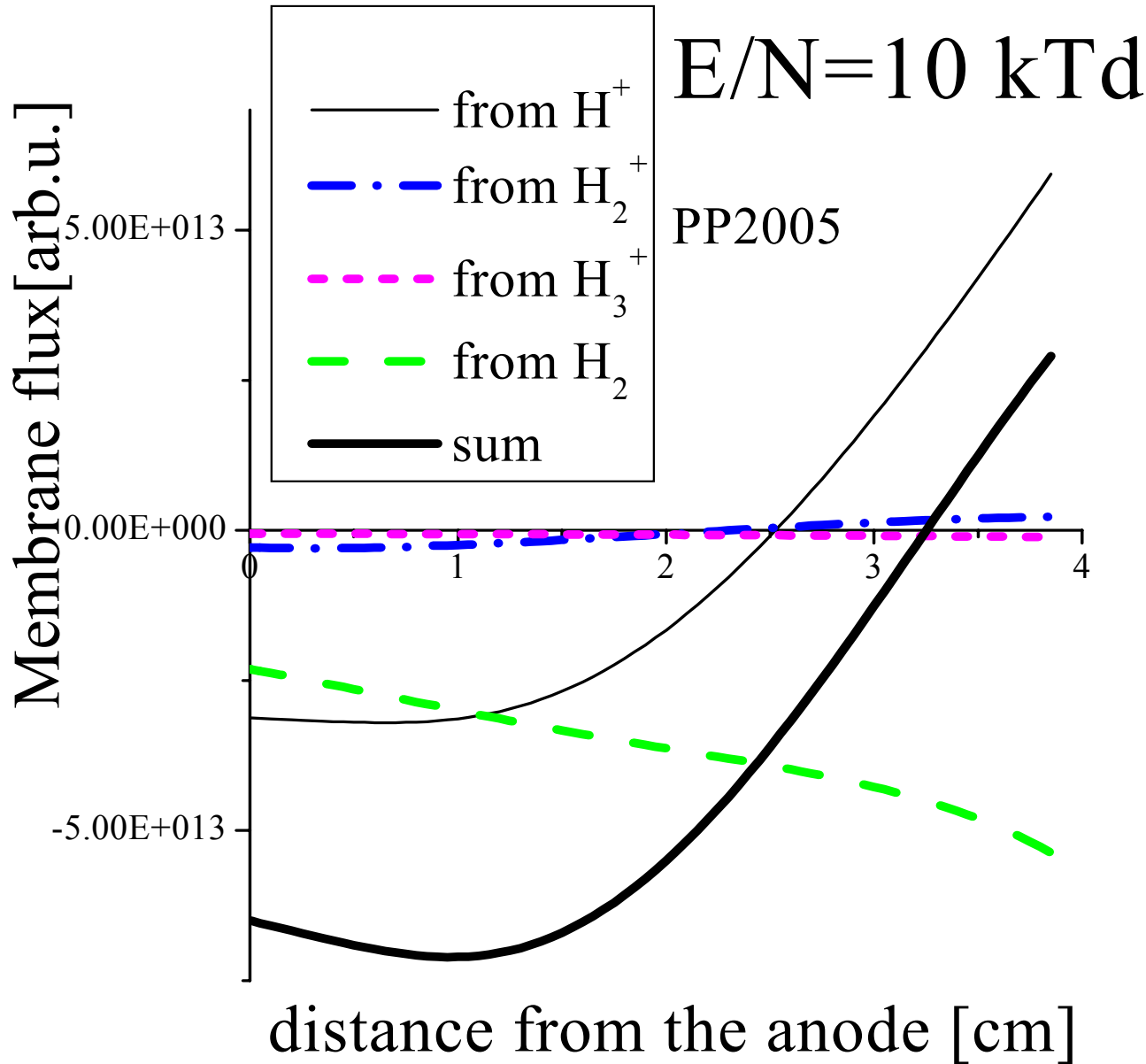


no angular dependence of reflection coefficient
PP2005

Particle fluxes



Contribution to (f)H Particle fluxes



Membrane flux a) of (f)H atoms as a function of distance for PP2005.

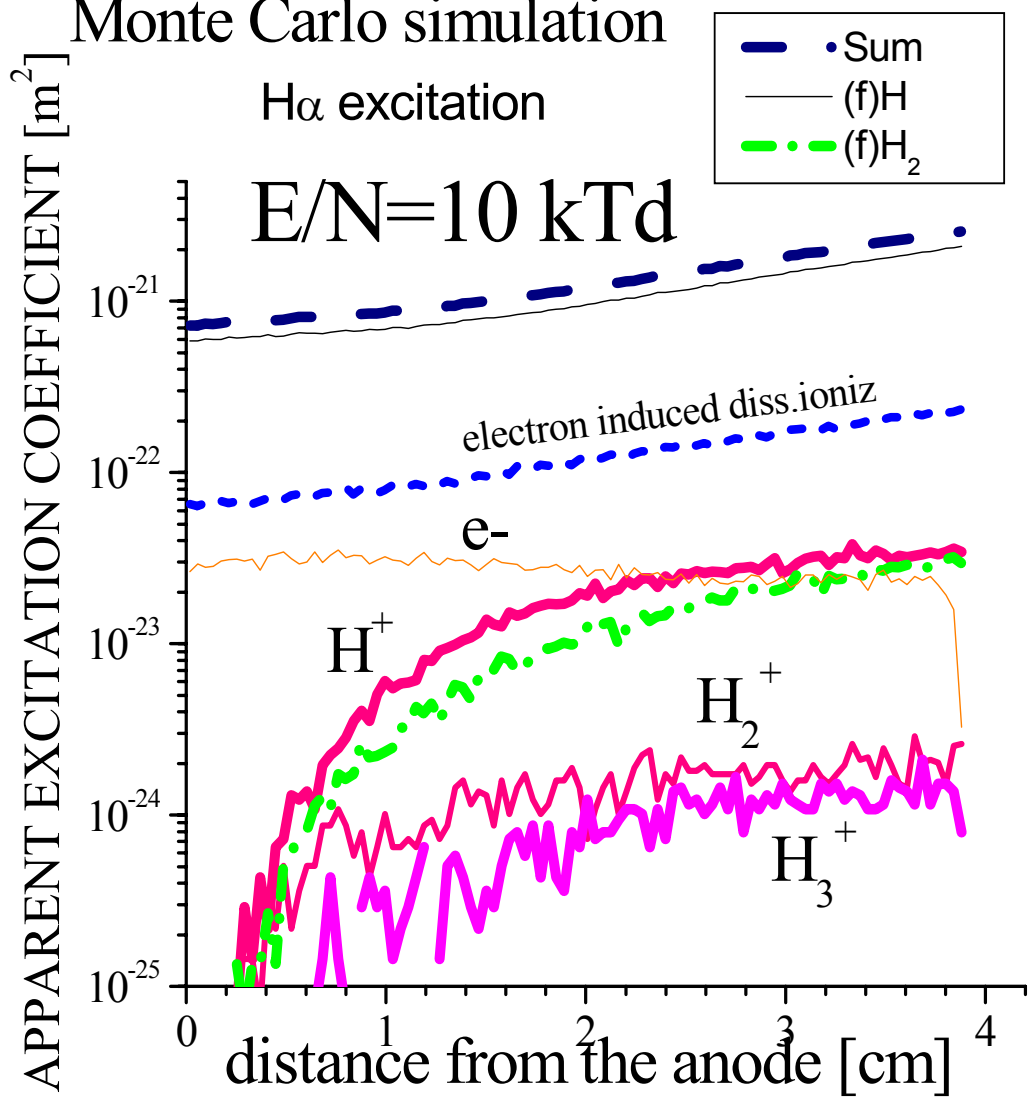
Contributions to spatial profile

for 1000000 initial electrons

Monte Carlo simulation

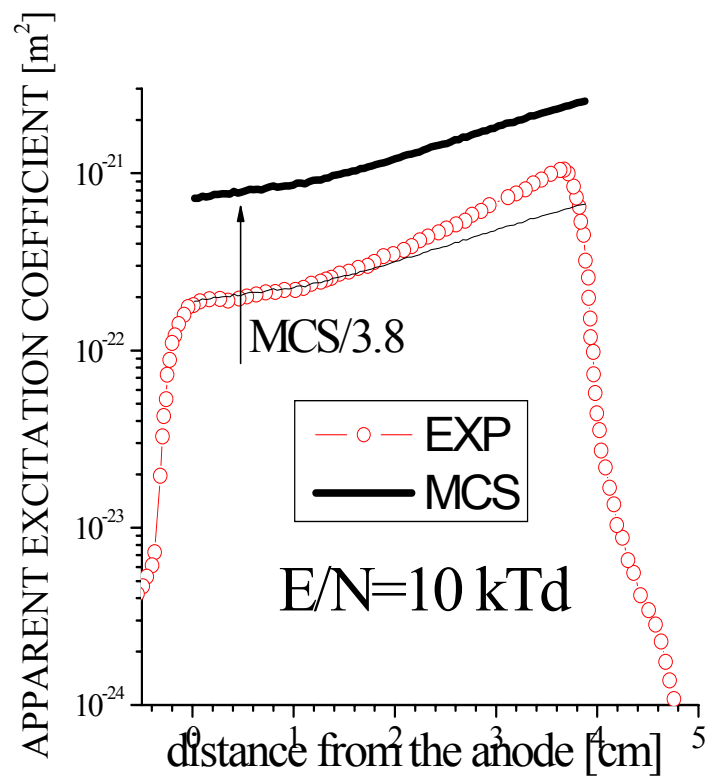
H α excitation

E/N=10 kTd



PP2005

Comparison with experiment



EXP H α Doppler profile detection

- Wavelength change for $\lambda=656.28$ nm line due to the atom emitter velocity is

$$\Delta\lambda = 0.03041\sqrt{\varepsilon[eV]} [nm]$$

excited atom energy

- For 100 eV : $\Delta\lambda=0.304$ nm
- For 1000 eV: $\Delta\lambda=0.962$ nm

Spectral resolution is 0.24 nm that gives the energy of excited species 62.3 eV

WHY SO POOR – well think of the current necessary to maintain the Townsend discharge conditions: i.e. 1-5 max 10 μ A

Contributions to Doppler profile and comparison with EXP

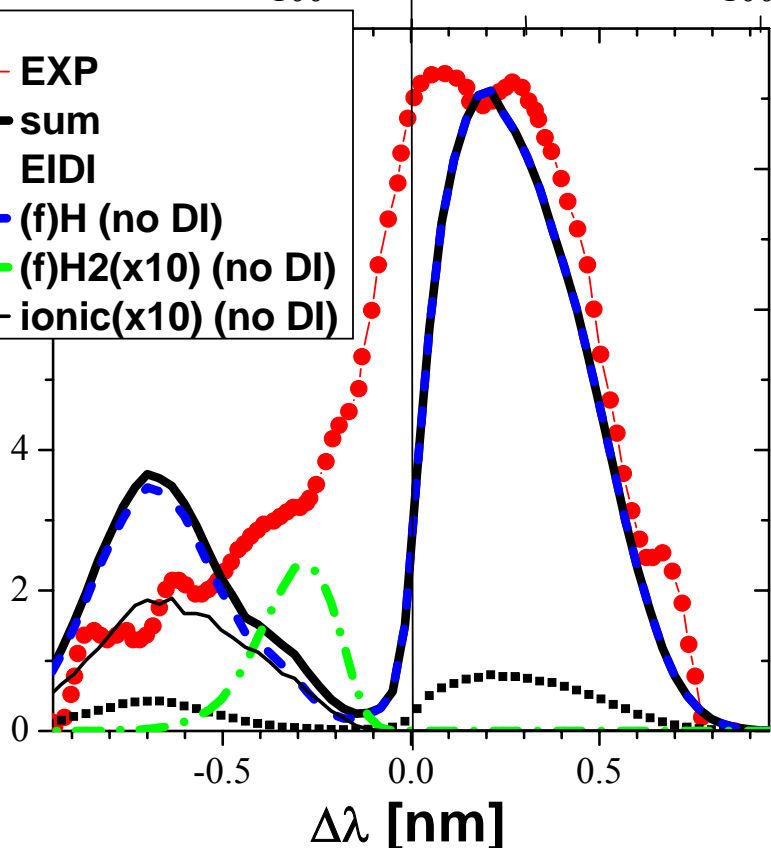
Excited Atom Energy [eV]

← Approaching Cathode Leaving Cathode →

1000 100 0 100 1000

● EXP
 — sum
 ■ EIDI
 - - (f)H (no DI)
 - · - (f)H2(x10) (no DI)
 — ionic(x10) (no DI)

Intensity [arb. un.]



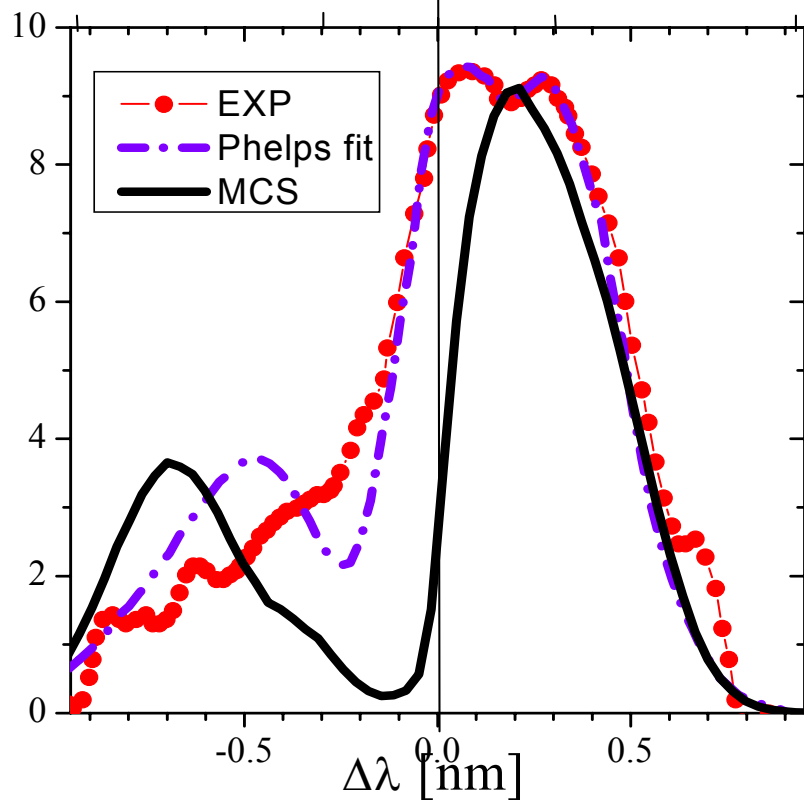
Excited Atom Energy [eV]

← Approaching Cathode Leaving Cathode →

1000 100 0 100 1000

Intensity [arb. un.]

● EXP
 - · - Phelps fit
 — MCS



Spectr. profiles for the $H\alpha$ line observed parallel to the axis of low-pressure, low current H_2 discharge at $E/N=10$ kTd ($N=0.6095 \cdot 10^{16} \text{ cm}^{-3}$). **DI** – contribution from H^+ produced in electron dissociative ionization, **fast H (noDI)**- contribution of all fast H according to the scheme without DI, **sum** - effect all particles according to the scheme
Phelps fit, **EXP** from Petrović et al., Phys.Rev. Lett. (1992) (Fig 1 a)
ionic (no DI) – contribution of H^+ , H_2^+ , H_3^+ ions without .DI, **fast H2(noDI)** – contribution from fast H2 without DI

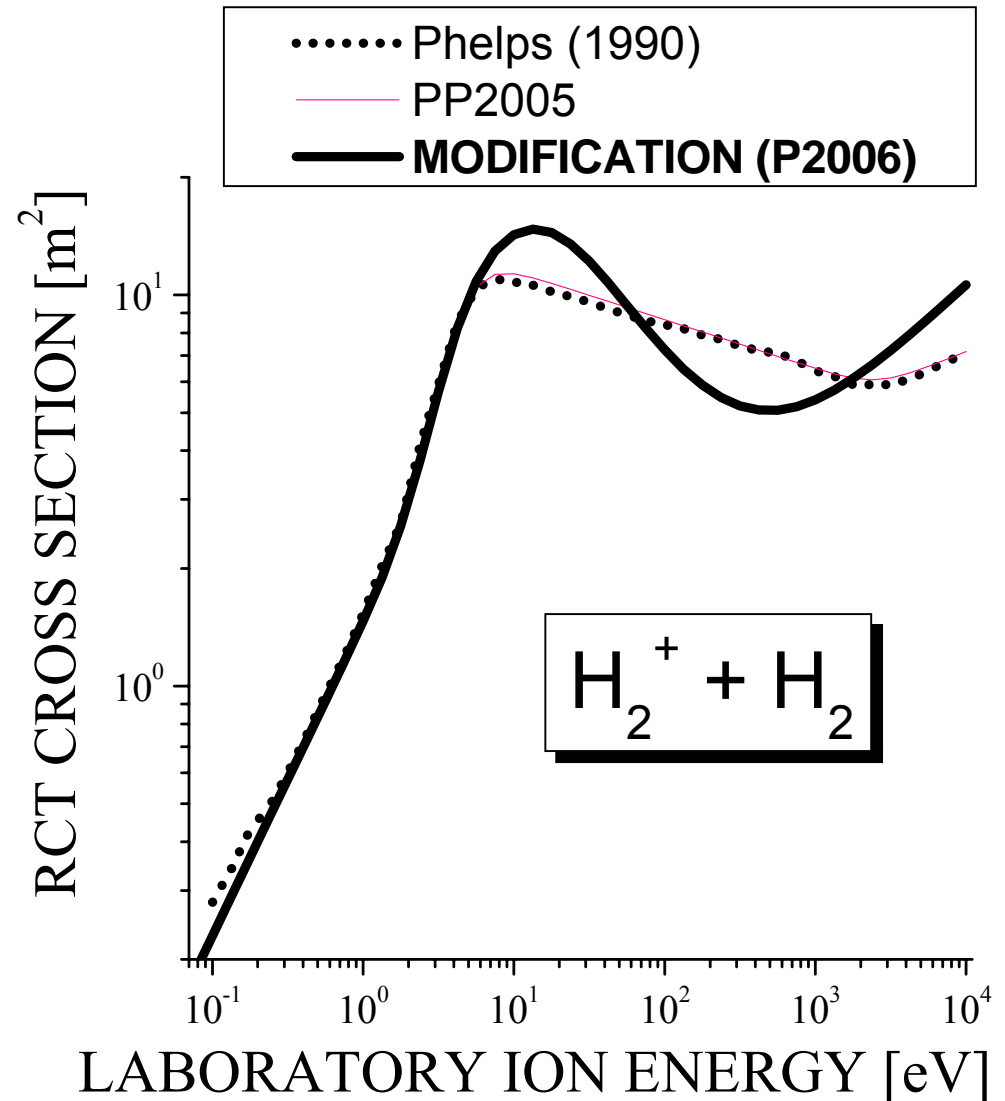
How good is present (PP2005) model?

- MCS results fit experimental spatial excitation and Doppler broadened profile of H α excitation
- Absolute spatial emission is about 4 times larger than EXP!!! Can we improve that?

by making a more realistic model?

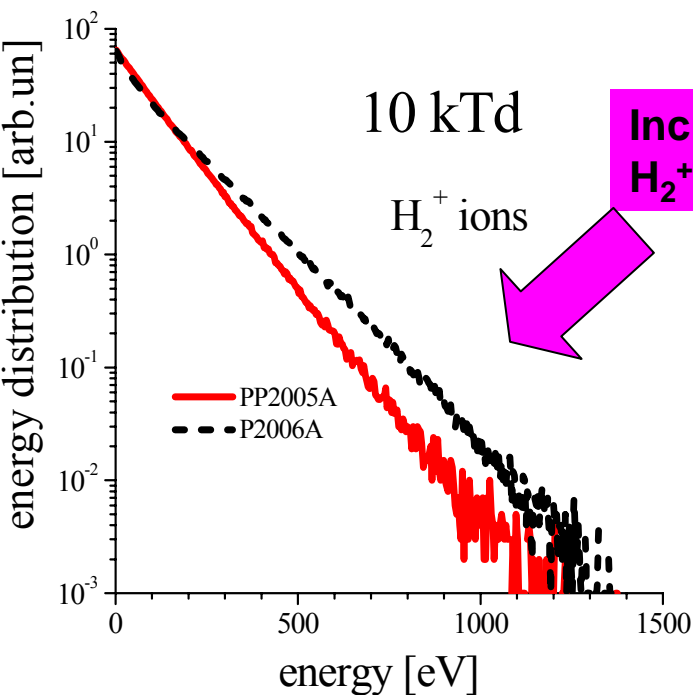
1st- will modify $\text{H}_2^+ + \text{H}_2$ cross section set:

shape of
resonant charge transfer (RCT)
cross section for H_2^+ on H_2

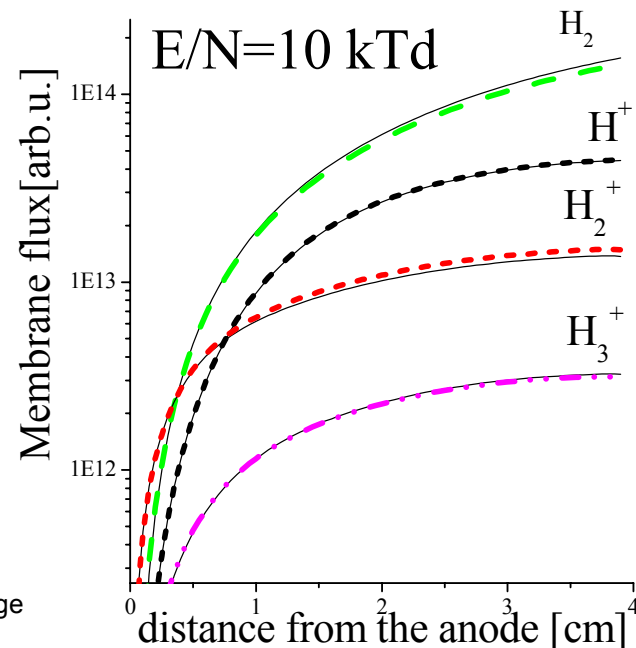


Effect of modification of the shape of RCT cross section for $H_2^+ + H_2$

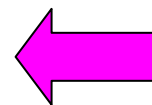
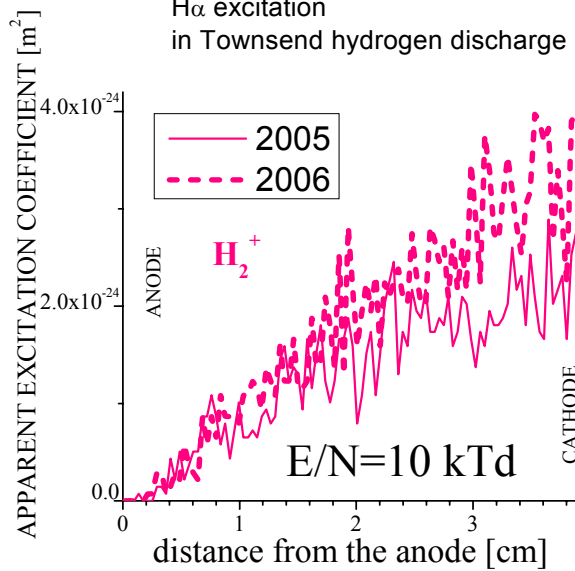
EDF at the cathode



Decrease of (f) H_2 flux
Increase of H_2^+ flux



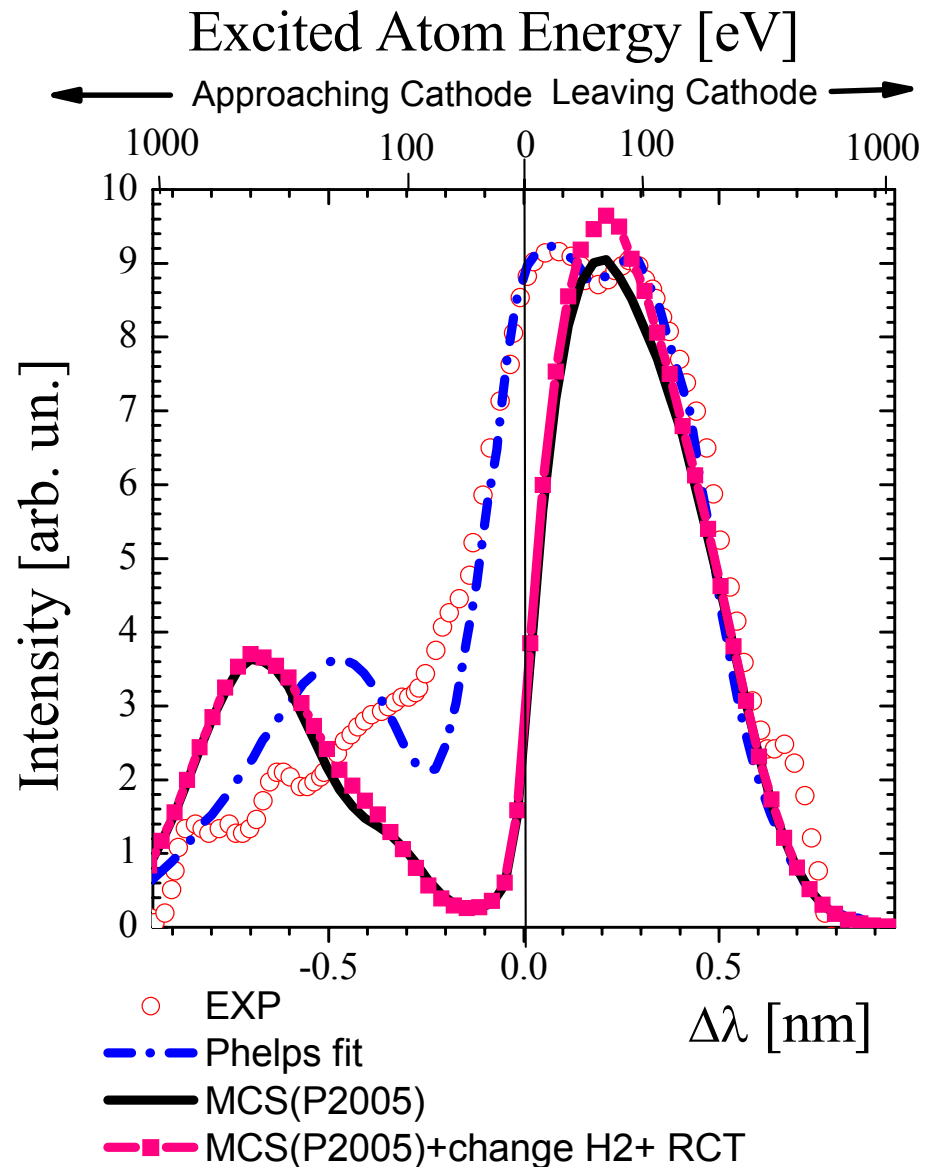
$H\alpha$ excitation
in Townsend hydrogen discharge



Increase of H_2^+ induced $H\alpha$
emission intensity close to
the cathode

Effect of modification of shape of RCT cross section for $H_2^+ + H_2$ on Doppl. profile

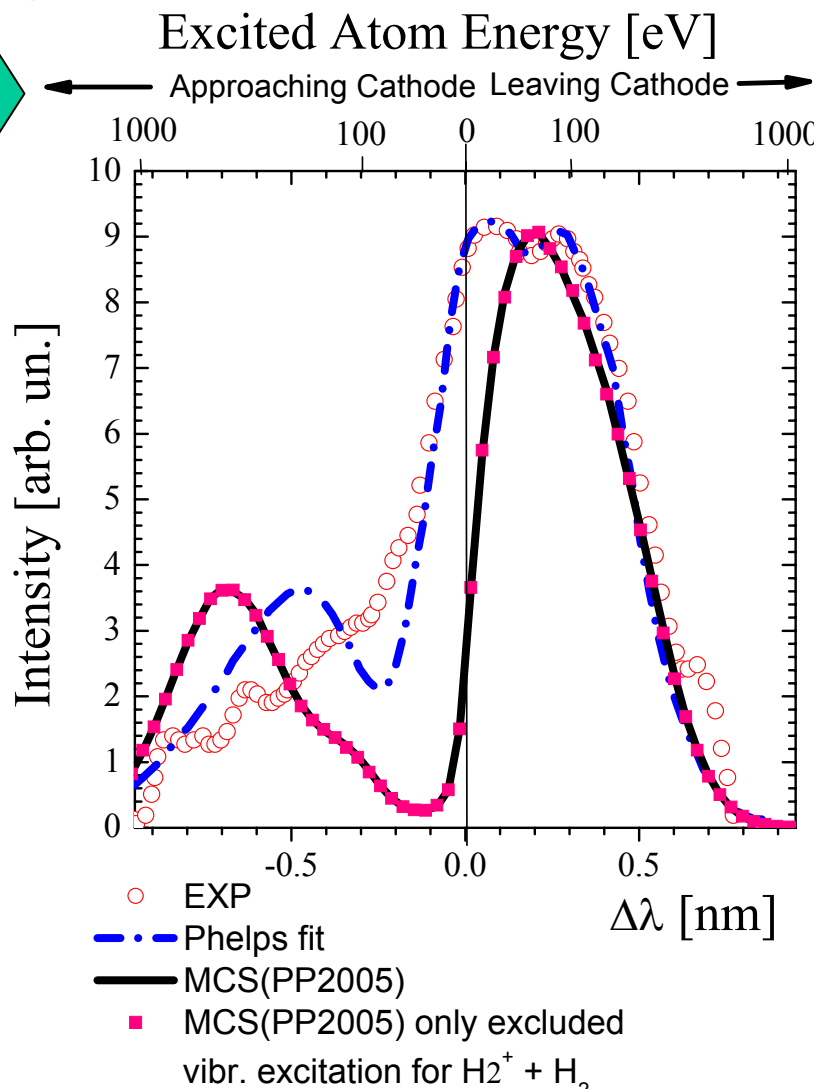
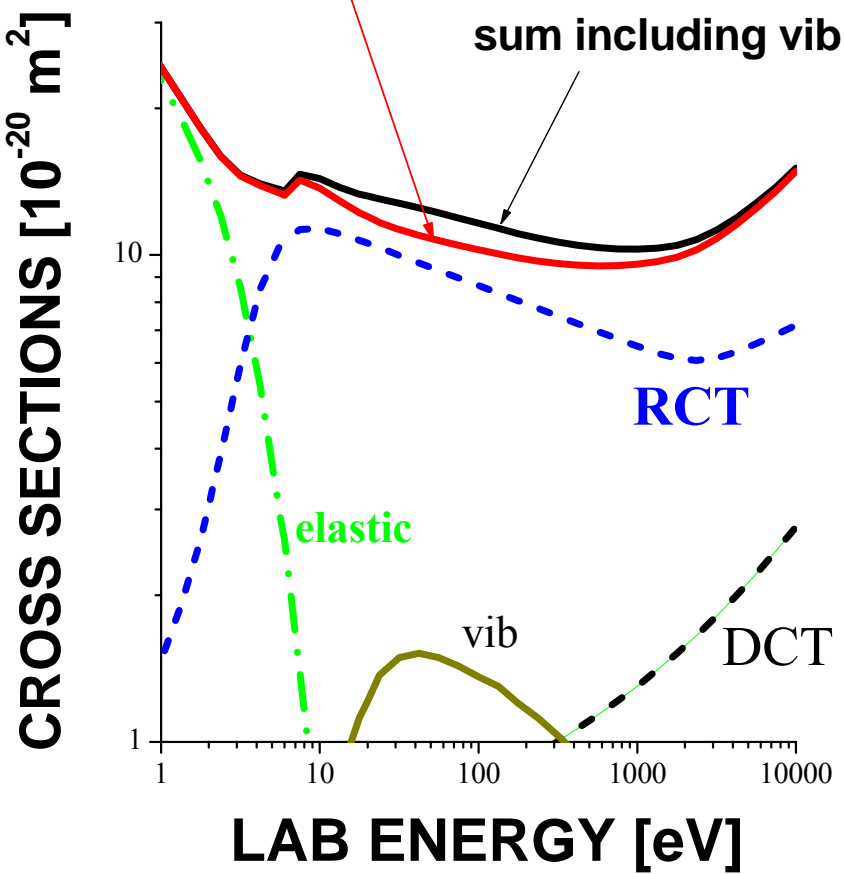
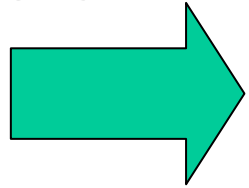
- slightly changed “direct” profile,
- increased “backward” profile due to the increased number of (f)H produced by higher energy H_2^+ ions and faster H_2 than in previous model (PP2005)



2nd –will modify H₂⁺+H₂ cross section set:

exclude vib. losses from
H₂⁺ on H₂ cross section set
sum without vib losses

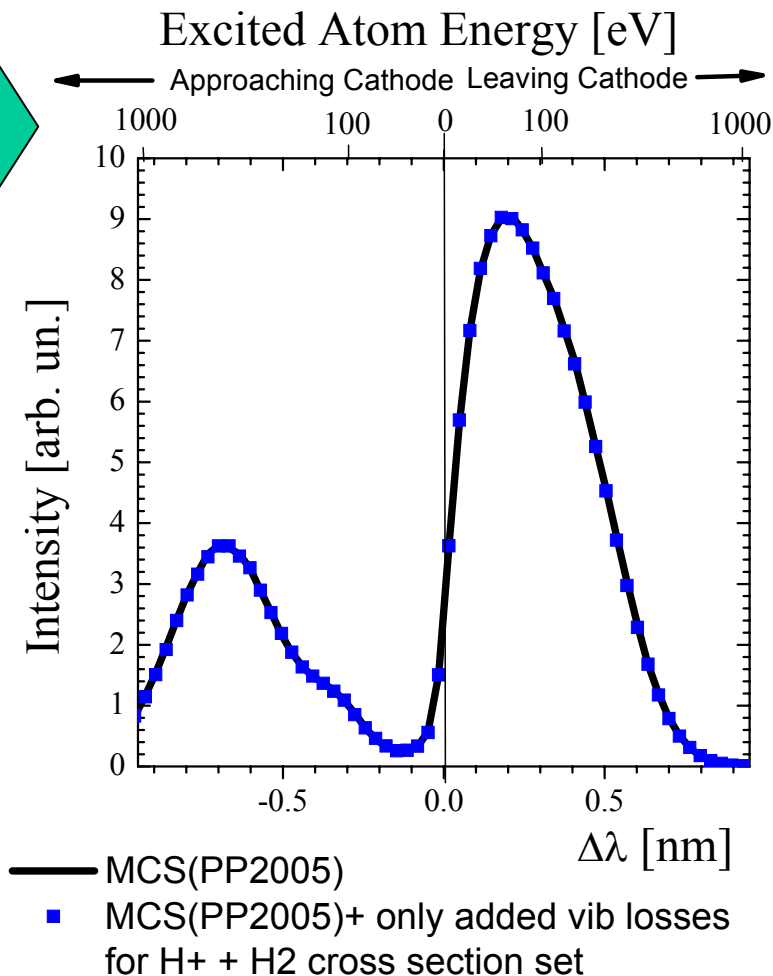
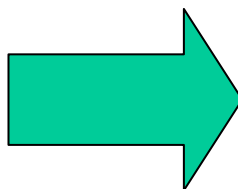
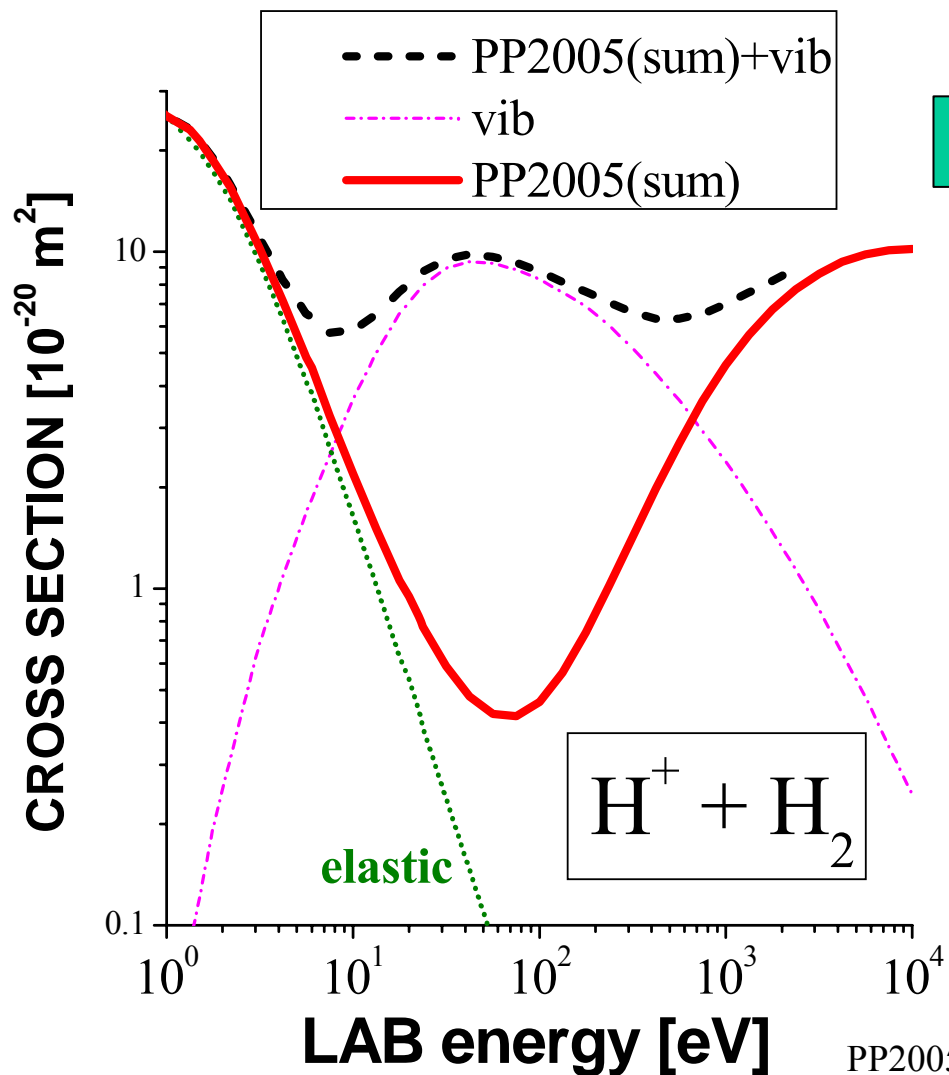
INSIGNIFICANT



3rd: Will modify $H^+ + H_2$ cross section set:

include vibrational losses for $H^+ + H_2$

INSIGNIFICANT



PP2005(sum)-sum of PP2005 cross sections
Vib-sum of vibrational $v=0,1,2$ cross sections

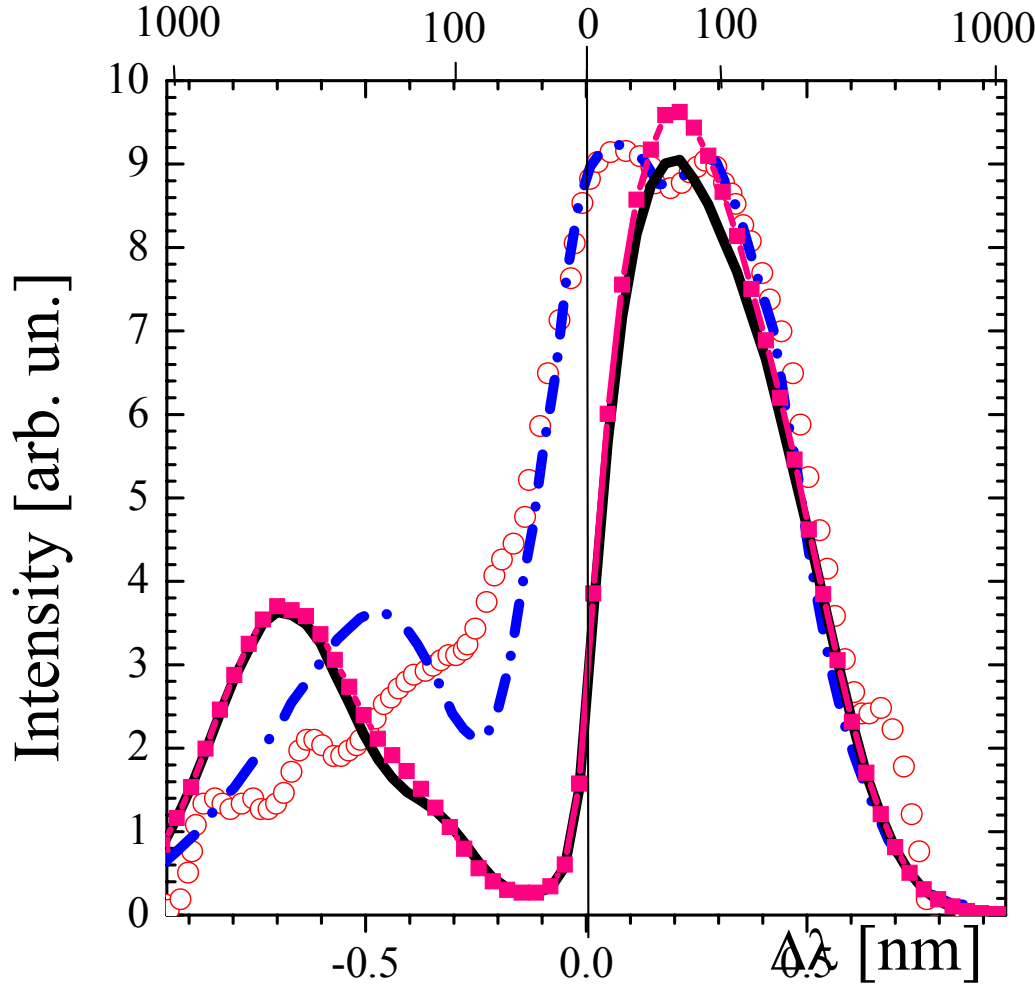
← Approaching Cathode Leaving Cathode →

Effect of ALL MODIFICATIONS OF the CROSS SECTION SET:

- shape change for RCT cross sct. for $H_2^+ + H_2$
 - excluding vib. excitation from $H_2^+ + H_2$ cross sct.
 - adding vib excitation to H^+ scattering model
- (appears to be insignificant at these E/N)

On $H\alpha$ Doppler broadened line profile.

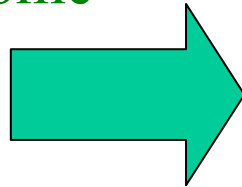
IS SMALL AT VERY HIGH E/N



- EXP
- · — Phelps fit
- MCS(P2005A)
- ■ — MCS(P2005A) H₂⁺: change RCT excl VIB

4th: will modify particle reflection model at the surface:

- Constant reflection coefficient (0.5) become energy dependent



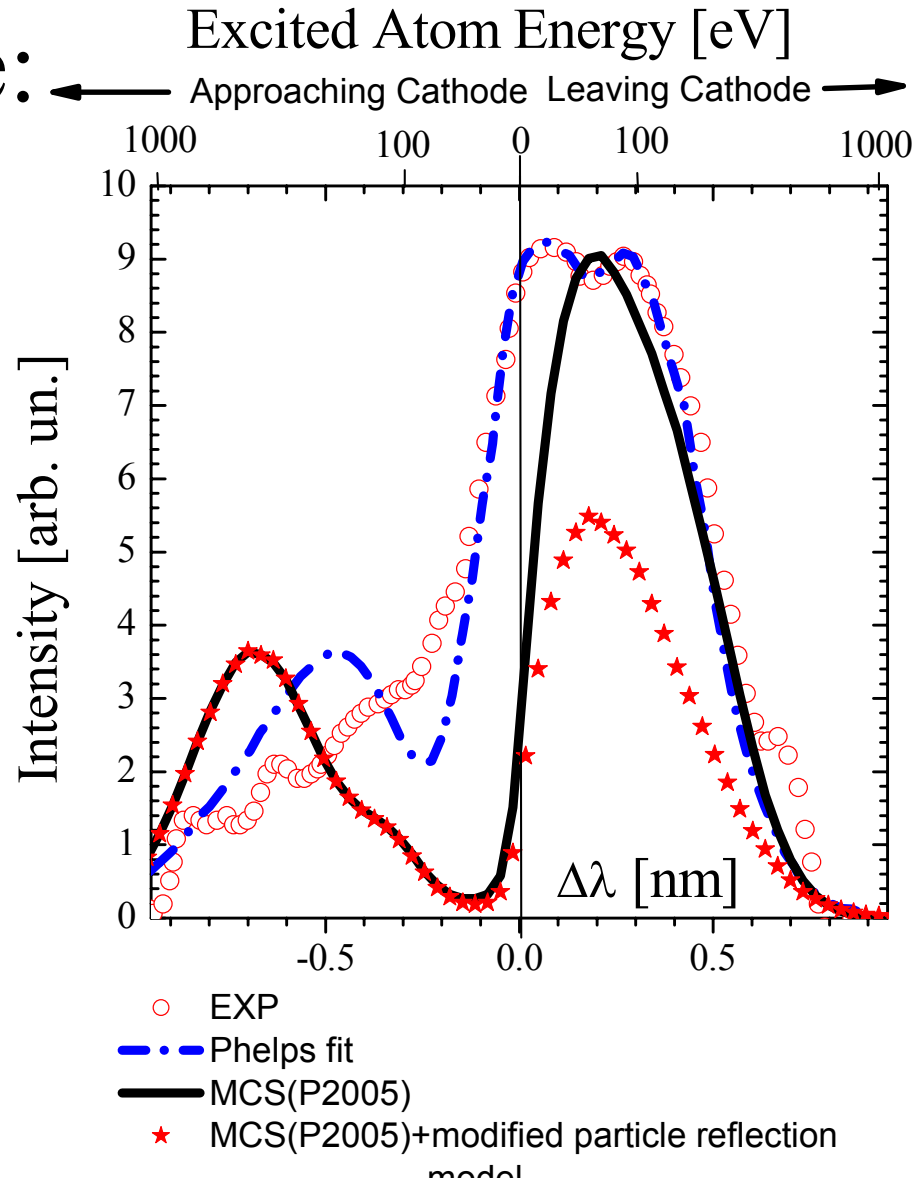
$$R = \frac{0.6}{\left(1 + \sqrt{\frac{E[\text{eV}]}{3000}}\right)^3}$$

- energy of the reflected particles instead of being 2/3 of incoming energy per particle now is uniformly distributed up to incoming energy per particle.

Effect of modification of particle reflection model at the cathode on Doppler broadened line profile:

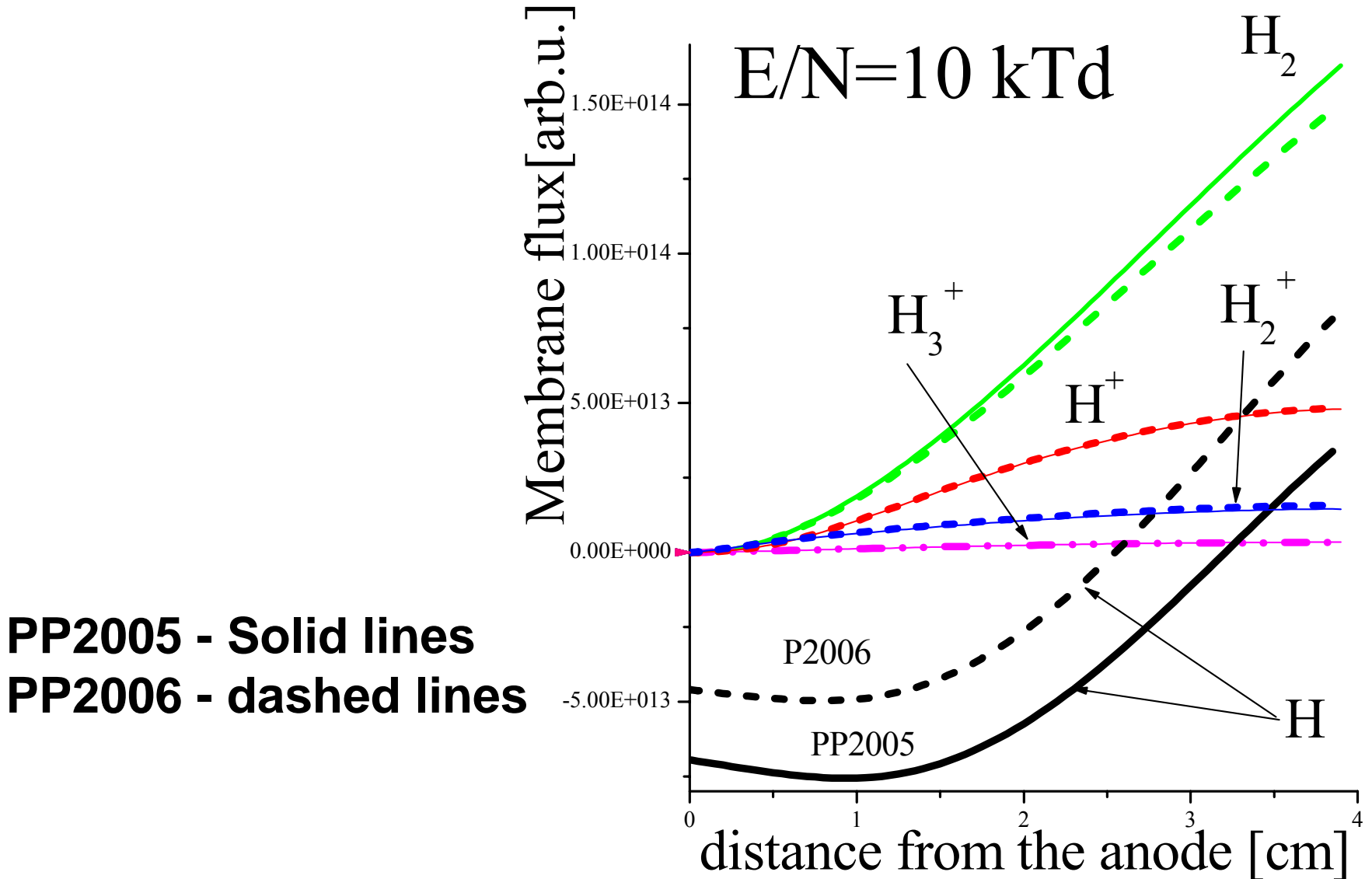
Peak due to the (f)H atom reflection leaving the cathode dropped for about 40 %

Spatial profile remained of the same shape! **Agreement** between modeling results and experiment **IMPROVED!** (see next slides).

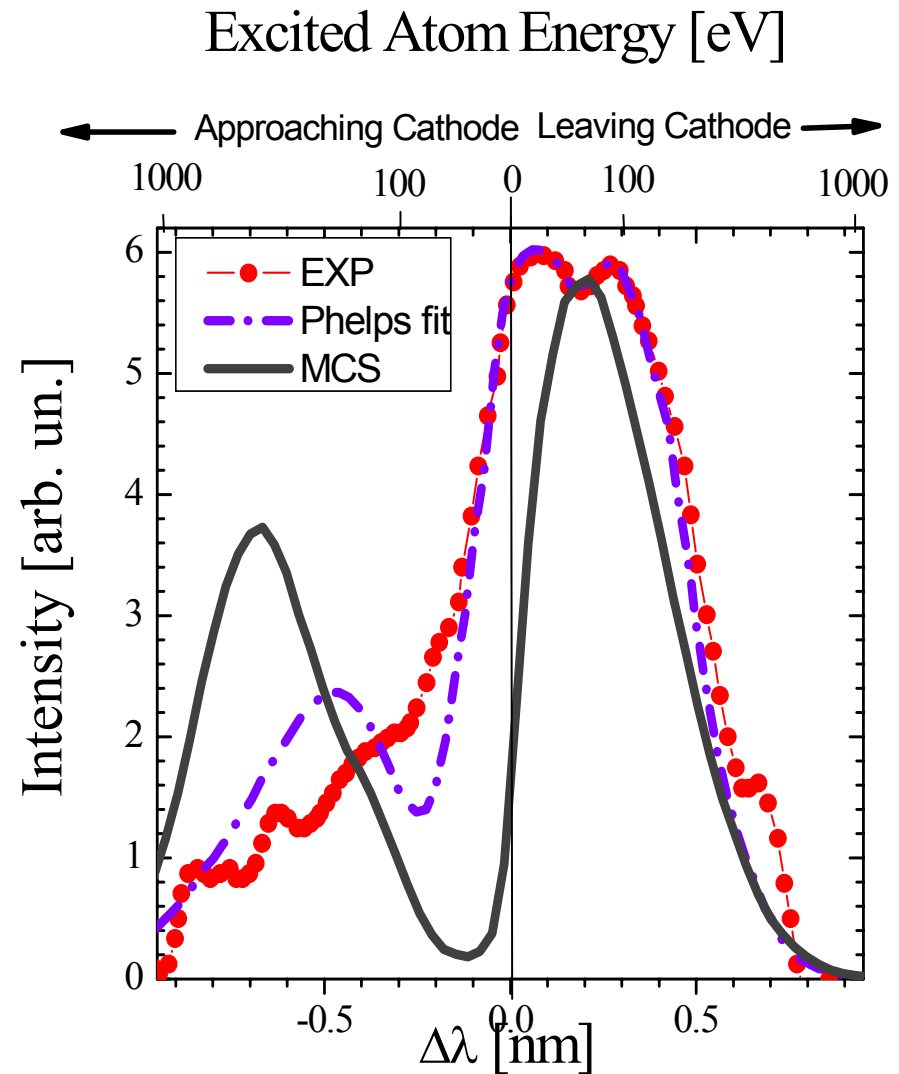
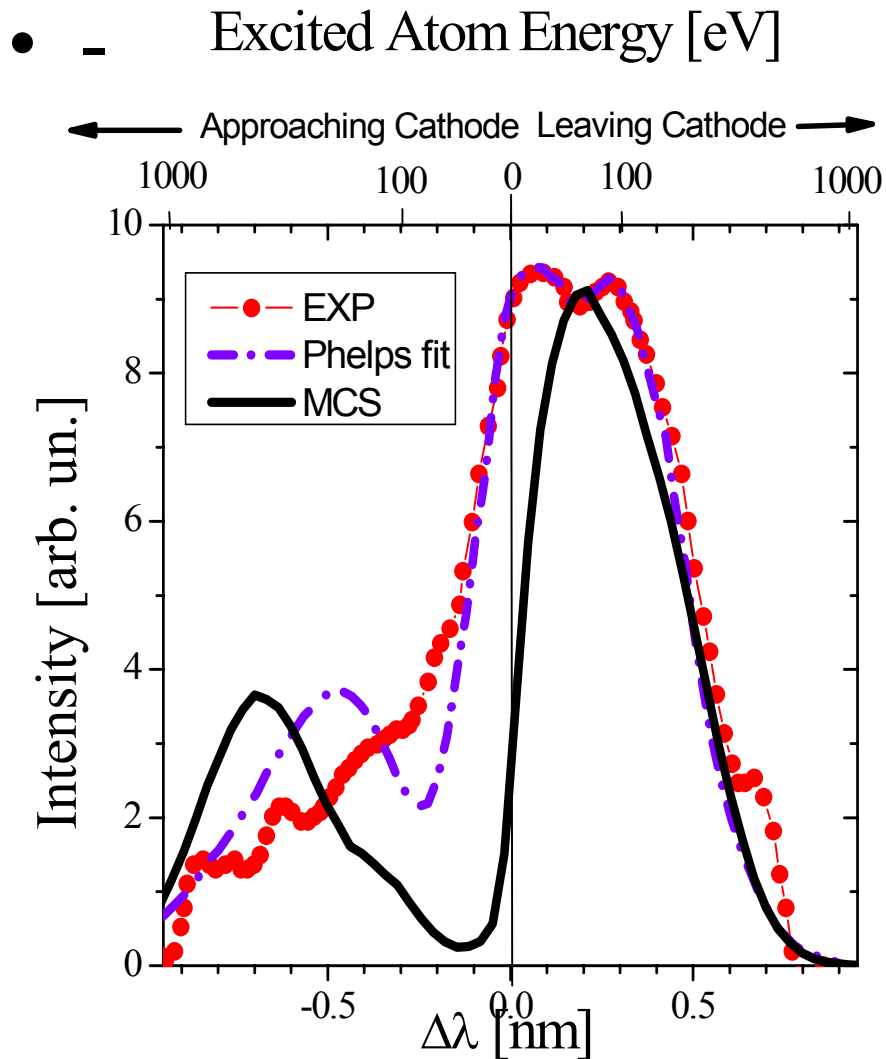


FINAL COMPARISON OF
THE RESULTS
FOR
TWO SCATTERING MODELS

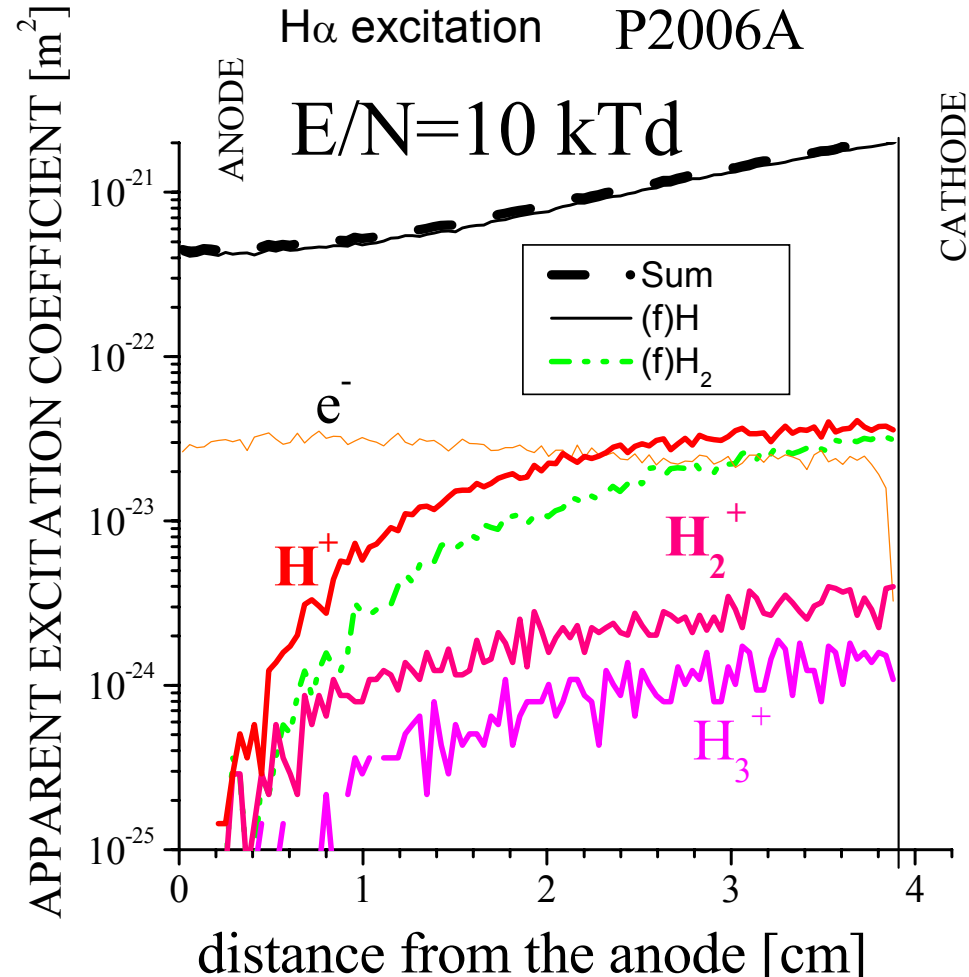
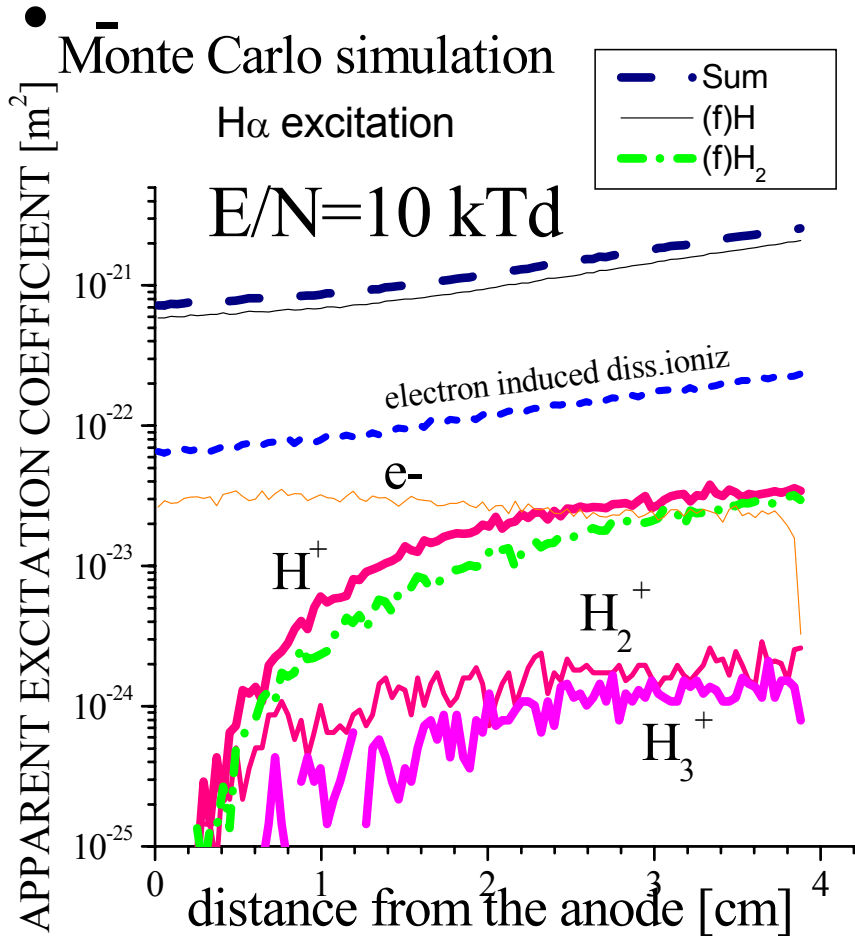
Particle fluxes for 2 scattering models



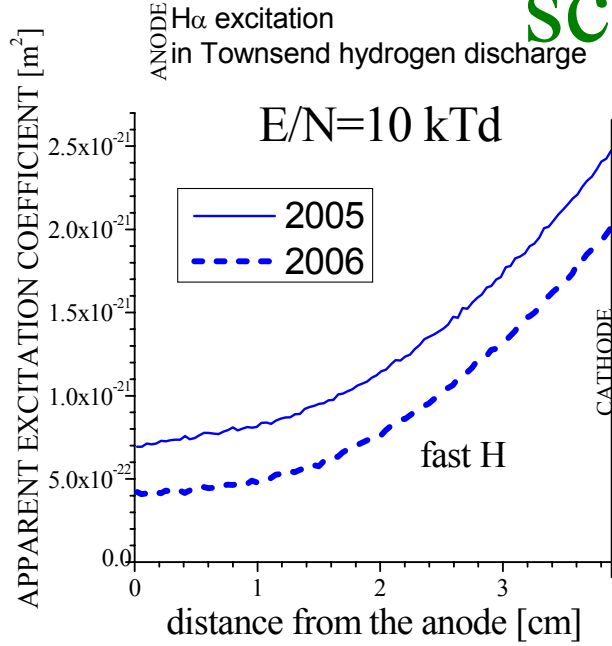
Doppler profile for 2 scattering models



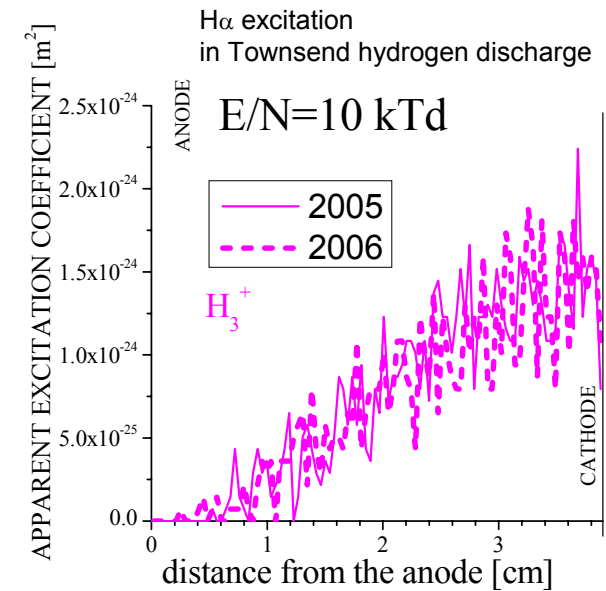
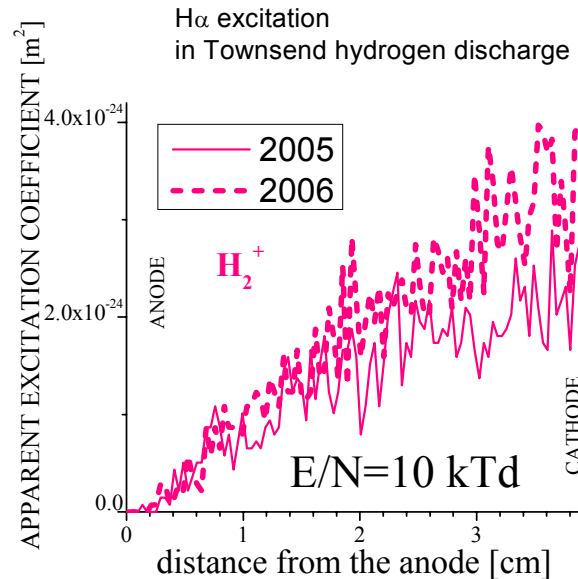
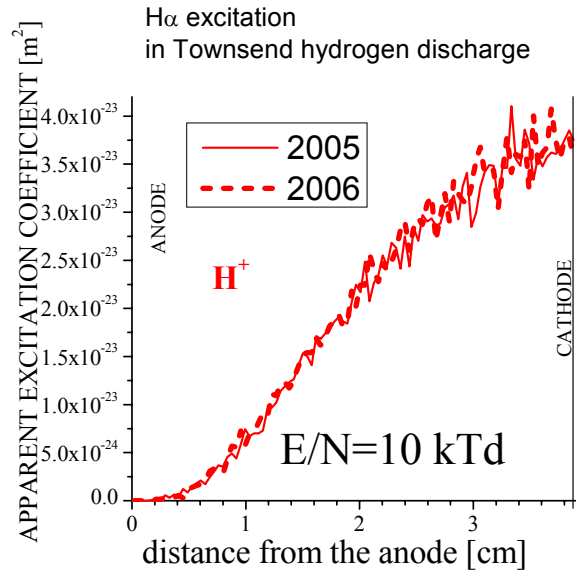
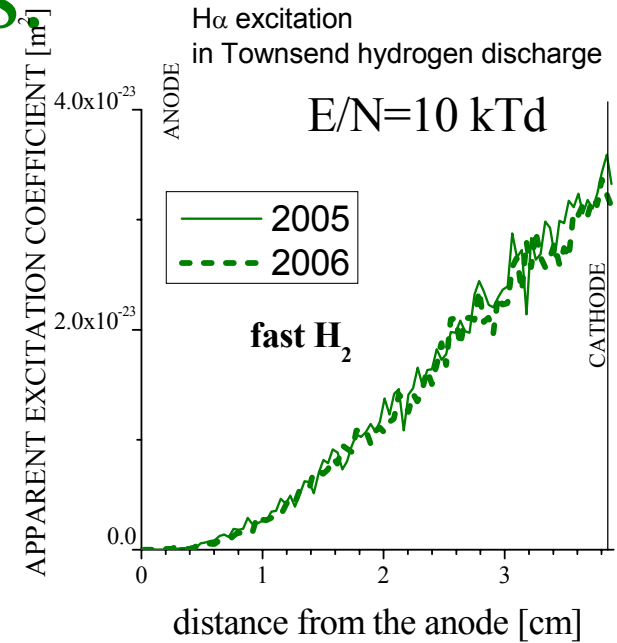
Spatial dependence of H α emission for 2 scattering models



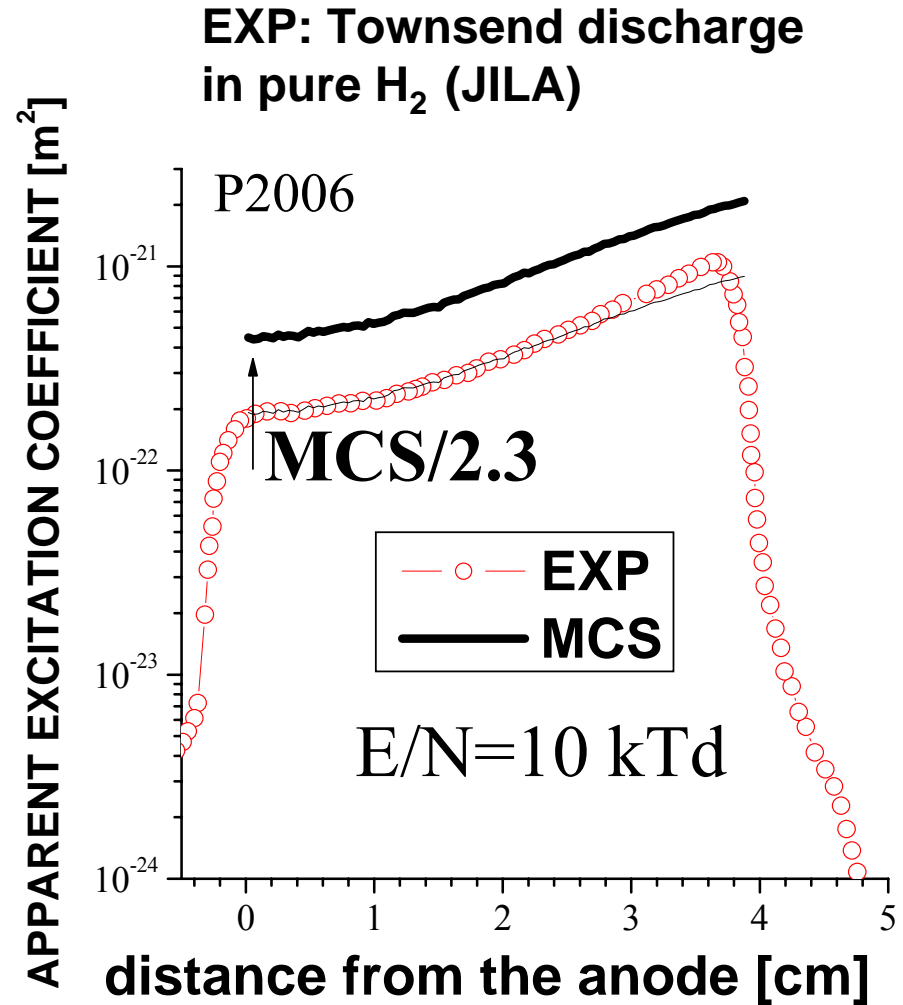
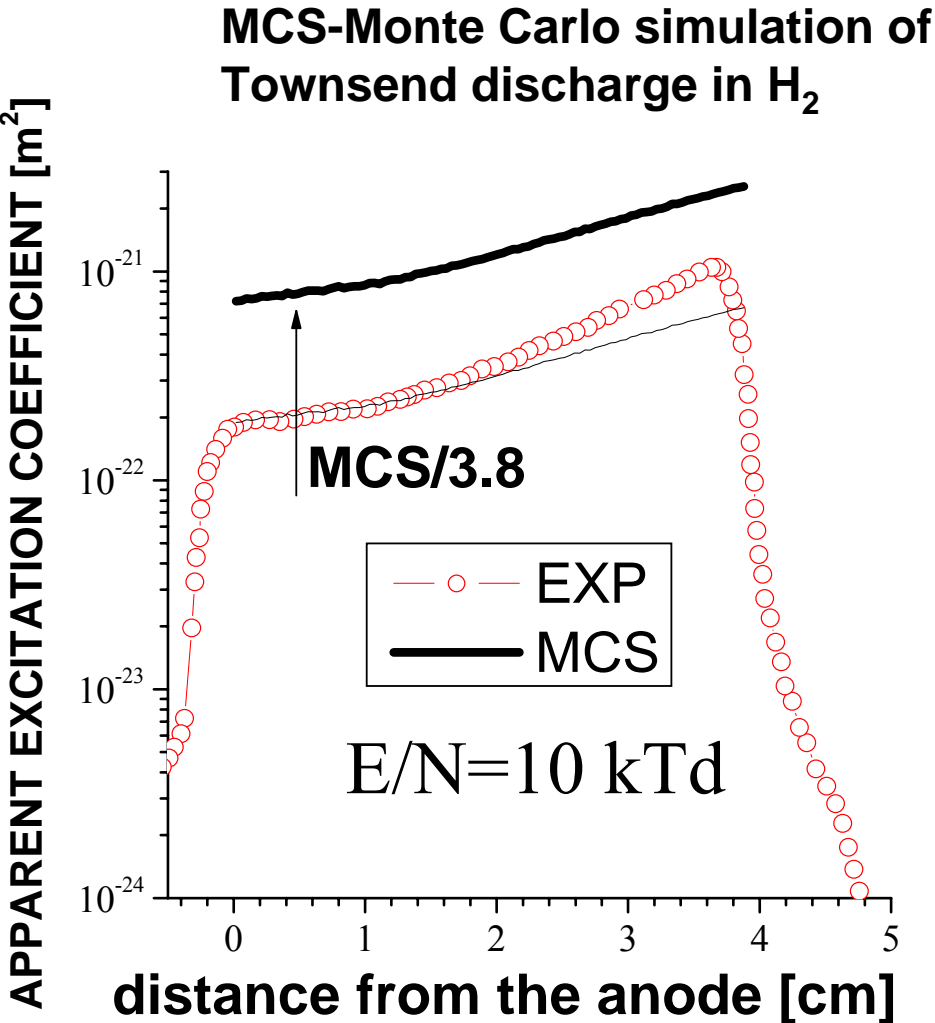
Contributions to spatial emission for 2 scattering models



PP2005 - Solid lines
PP2006 - dashed lines



Comparison of Monte Carlo results with an experimental spatial profile for 2 scattering models



for 1000000 electrons

We also analyzed

- **Effect of reflection coefficient dependence with incident angle with model PP2005,**
- **How all vibrational losses affect results obtained by model PP2005,**
- **Effect of electron anisotropy in collisions leading to singlets and ionization.**

So to conclude

- **Basic physics of the process is included in the model,**
- **Details of the model still require some fine tuning,**
- **Two key issues:**
 - **Too few collisions of ions in MC**
 - **Exact model of reflection.**

LITERATURE

- [1] Petrović Z.Lj. and Phelps A.V. (1991), Proc. of the International Seminar on Reactive Plasmas, E-3, 35
- [2] Petrović Z.Lj., Jelenković B.M. and Phelps A.V. (1992) Phys. Rev. Lett. **68**, 325
- [3] Gylys V. T., Jelenković B. M. and Phelps A. V. (1989) J. Appl. Phys., **65**, 3369
- [4] Phelps A. V. (1990) J. Phys. Chem. Ref. Data., **19**, 653
- [5] Petrović Z. Lj. and Phelps, A. V. (1989), Bull. Am. Phys. Soc., **35**, 1824
- [6] Petrović Z.Lj. and Phelps A.V. (1990) Proc. ESCAMPIG, 118
- [7] Vrhovac S., Radovanov S., Petrović Z. Lj. and Jelenković B. M. (1991) Proc. of the Joint Symposium of Electron and Ion Swarms and Low Energy Electron Scattering, Bond University, Gold Coast, Australia
- [8] Videnović I.R., Konjević N. and Kuraica M.M. (1996) Spectrochimica Acta Part B: Atomic Spectroscopy, **51**, 1707
- [9] Konjević N. and Kuraica M. (1992) Phys. Rev. A, At. Mol. Opt. Phys., **46**, 4429
- [10] Bogaerts A. and Gijbels R. (2000) J. Anal. At. Spectrom., **15**, 441
- [11] Gemišić Adamov M. and Kuraica M. M. (2004) Eur. Phys. J. D, **28**, 393
- [12] Stokić Z., M.M.F.R. Fraga, J. Božin, V. Stojanović, Z.Lj. Petrović and B.M. Jelenković (1992) Phys.Rev. A, **45**(10), pp.7463-7468.