

**NAUČNI RADOVI**  
**Prof. dr Katice Hedrih**  
**(sa bibliografijom)**

Priredili: Dr Slaviša Milisavljević  
Dr Žarko Mijajlović

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## KATICA (Stevanović) HEDRIH

*Full professor-Scientific Research Full Professor – Project Leader of Project ON144002  
in Mathematical Institute SANU Belgrade (2009- )*

*Full professor and the Head of the Chair for Mechanics (1977-1979, 1981-1983, 1986-2004)*

*Head of Centre of Nonlinear Dynamics and Active Structure (2005-2009)  
at the Mechanical Engineering Faculty of the University of Niš*

*Academician of Ukrainian Higher Education Academy of Sciences*

*Member of Serbian Scientific Society*

*Academician of the Academy of Nonlinear Sciences*

*Scientific Secretary of the Yugoslav Section of Academy of Nonlinear Sciences (1997-2010)*

*Member of American Academy of Mechanics*



Katica (Stevanović) HEDRIH, Doctor of Technical Sciences, *Scientific Research Full Professor in Mathematical Institute SANU-Belgrade*, University Professor, Bachelor Mechanical Engineer, Full Professor and the Head of the Chair for Mechanics at the Mechanical Engineering Faculty of the University of Niš (1977-1979, 1981-1983, 1986-2004) and a Full Professor of the Mechanical Engineering Faculty, University of Priština, Project Leader of republic scientific projects: Subproject – Current problems of mechanics with applications (1995-2000), Project 1616 - Real Problems on Mechanics (2001-2004) at the Mathematical Institute of SASA in Belgrade, Project 1828 –Dynamics and Control of Active Structure (2001-2004) at Faculty of Mechanical Engineering Niš, current Project ON144002 Theoretical and Applied Mechanics of the Rigid and Solid Bodies. Mechanics of Materials (2006-2010) an academician of the *Higher*

*Education Academy of Sciences of Ukraine* (since 1996), a *member of Serbian Scientific Society* (starting from 2008) and an academician of the *International Academy of Nonlinear Sciences ANS. – Moscow* (since 1997), Editor-in-chief of the University of Niš scientific journal “**FACTA UNIVERSITATIS**” (1989-2004) and Editor-in-Chief of the Series Mechanics, Automatic Control and Robotics (1990-2011), member of Editorial Board of *Int. Journal Nonlinear Sciences and Numerical Simulations, Freund Publishing House LTD* (1999-), and *J. Mathematical Problems in Engineering*, Hindawi Publishing Corp.<http://www.hindawi.com/> (2004-), a member of GAMM and Tensor Society, member of International ASME, American Academy of Mechanics and a European Society for Mechanics Member. She is also reviewer and referee of the numerous university scientific publications and papers published by Elsevier, Springer, Hindawi Press, Freund Publishing House and other. Referee of *Zentralblatt* (with more than 100 reviews). She is the author of the monographs: *Vectors of the Mass Moments* (1998), *Analytical Dynamics of Discrete Hereditary Systems* (co-author O.A. Goroshko, 2001). and *The Vector Method of the Heavy Rotor Kinetic Parameters Analysis and Nonlinear Dynamics* (2001). She was the chief and project-leader of a number of scientific projects in areas of mechanics and mechanical engineering. She is one of co-authors of the research project and SASA edition-publication - The Life and Work of Serbian Scientists with four published bibliographies. She is the author of a number of scientific papers, and of university study books and textbooks in the area of Oscillations Theory, Theory of Elasticity, Strength of Materials, Mechanics, Mathematical Physics, Philosophy of Natural Sciences, History of Mechanics. She was a supervisor of a number of magisterium of sciences (10) and doctoral dissertations (8) in the area of technical sciences – nonlinear and deformable body mechanics and member of numerous commission for evaluation of the dissertations. Her papers and books were cited many times and two paper were cited by *Yu. A. Mitropolskiy and B.I.Moseenkov in Monograph: Asimptotičeskie rešenija uravnenij v časnih proizvodnih*, Kiev 1976, (Listed under No. 138 and 139). Her first doctors of technical sciences are now university professors and Project leader and supervisor of new generation of the Ph. D. students.

Katica R. (Stevanović) HEDRIH was born on August 28<sup>th</sup> 1944 in Bobovište. As a member of the first Yugoslav competition team she was a contestant of the Fifth Mathematical Olympics in Vroclav. Poland, in 1963. She graduated mechanical engineering, the first in generation, as the best graduated

student of the faculty and the University of Niš in 1966/67. She carried the “štafeta mladosti” in 1969. She got a Magisterium of Science degree in the area of mechanics (1972) and became a Doctor of the Technical Sciences (1975) at the Mechanical Engineering Faculty of University in Niš, and she also took and passed the candidate minimum (1971) in Mathematical Physics, the area of Nonlinear Oscillations and Nonlinear Differential Equations at the Mathematical Institute of the Ukrainian National Academy of Science in Kiev evaluated by commission headed by academician Y. A. Mitropolskiy. She is a University full professor since 1986.

She was the organizer of two Yugoslav congresses on theoretical and Applied Mechanics (YUCTAM Niš-1995 and Vrnjačka Banja 1997), as well as of a number of minisymposia of international rank ((YUSNP Niš 1991 and YUSNM Niš 2000, ISNM NSA Niš 2003, Integrity of Dynamical Systems at IFNA WCNA, Orlando, 2004; Integrity of Dynamical Systems –European Fracture Conference EFC16-Greece 2006 and APM Saint Petersburg 2007; MS – Analytical Mechanics at Nonlinear Dynamic Shanghai 2007, MS – Kinetic Control and Vibrorheology at ESMC Lisbon 2009 and ICDVC Hangzhou 2010m and other.).

She is the author of a number (10) of university study books and textbooks in the area of Oscillations Theory, Theory of Elasticity, Strength of Materials, Mechanics, Partial Differential Equations and Integral Equations with Application in Engineering, Philosophy of Natural Sciences, History of Mechanics.

She attended, with invited lectures or as invited participant, numerous University Mechanics Seminars or Scientific Meetings in the area of nonlinear mechanics (University of Rochester Seminar 1989, USA; University of Waterloo Seminar on Mechanics 1989., Canada; Rochester Institute of Technology, 1989.; IUTAM Symposium-Nonlinearity and Chaos in Engineering Dynamics, UCL 1993.; Inter. Conf.: *Stability, Control and Rigid Bodies Dynamics - ICSCD 96*, Donetsk – Mariupol; Seminar on *National Technical University of Athens, 1986.*; *SANU - Serbian Greek Symposium on Solid Mechanics 1997.*; *Greek-Germany-Polish-Serbian Symposium on Mechanics - Recent Advances in Mechanics, Xanthi, 1998, Democritus University of Thrace*; Third International Symposium on Classical and Celestial Mechanics, Velikie Luki, Russia, 1998; *Parallel General Lecture-Third International Conference on Nonlinear Mechanics ICNM 1998, Shanghai, China*; *5th National Congress on Mechanics, Ioannina, 1998. Patras 2007*; *Int. IEEE-Conference Control Oscillations and Chaos COC 2000 Saint Petersburg, Russia*; *ISUMEL Lvov 2001,2003,2005,2007,2009 Ukraine*; Int. Symposium *Dynamical Systems and Applications-Lodz 2001, 2010. Poland*; Int. Conf. *Differential Geometry and it's Applications*, Tensor Society Tsukuba, Japan 2002.and Sapporo 2007; Int. Symposium *Analysis, Manifolds and Mechanics*, Calcutta, 2003, University of Kalyani, India, 2003 and 2007, IUTAM Symposium *Chaotic Dynamics and Control of Systems and Processes in Mechanics*, Roma 2003. ....Workshops IFAC FDA Bordeaux 2004, Porto 2006, Ankara 2008, ENOC Moscow 2002, Eidhoven 2005, DINCON Brasil 2010, Nonlinear Vibrations Virginia Tech 2010, ICVDC Hangzhou 2010, and other) and contribution papers, of a large number of leading international congresses and scientific meetings, as well as of university scientific seminars (Ukraine, Canada, USA, Germany, Byelorussia, Greece, Israel, Austria, Bulgaria, Chesz, China, England, Denmark, Russia, Poland, Japan, Romania, Turkey, Portugal, France, India, Australia, Brazil, ...) in the area of mechanics and Nonlinear Dynamics and she is the author of over 400 bibliographical units in areas of mechanics, technical sciences and mathematics. Her papers were referenced in well-known reference journals. She is the author of the monographies: *Vectors of the Mass Moments (1998)*, *Analytical Dynamics of Discrete Hereditary Systems (co-author O.A. Goroshko, Ukraine 2001)*. and *The Vector Method of the Heavy Rotor Kinetic Parameters Analysis and Nonlinear Dynamics (2001)*. She was the chief and project-leader of a number of scientific projects in areas of mechanics and mechanical engineering starting from the 1977. Shi is founder and chair of two Scientific Seminars; Theoretical and Applied Mechanics at Mechanical Engineering Faculty University of Niš (1976-2004) and Nonlinear Dynamics – Milutin Mulanković (staring from 2005). Katica (Stevanović) HEDRIH is, also, a member of numerous International Scientific Meeting held in Ukraine, Yugoslavia, Poland, China, Turket, Makedonia, Serbia, India and other.

She was, as a student a member of the first University Council in Niš (1975), and as a full professor a member of the first Educational-scientific Council of the University in Niš (1987-1988), and a member of the governing board (1994) of the Mathematical Institute SASA in Belgrade.

#### Books:

*Vectors of the Mass Moments* (Topics from Mathematics and Mechanics), *Selected Chapters of Nonlinear Oscillation Theory*, *Selected Chapters of Elasticity Theory*, *Collections of solved exams problems of Elasticity Theory*, *Collections of solved exams problems of Oscillation Theory*, *Collections of*

*solved exams problems of Oscillation Theory (co-autor P. Kozić), Collections of solved exams problems of Strength of Materials (co-author M. Maksić), Natural Sciences today (co-authors M. Antić and D. Djordjević), Ljubomir Klerić (SASA Life and work of Serbian Scientists – First volume), Kosta Alković (SASA Life and work of Serbian Scientists – Third volume), Tatomir P. Andjelić (SASA Life and work of Serbian Scientists – Sixth volume) and Danilo P. Rašković (SASA Life and work of Serbian Scientists – Tenth volume) and Tatomir P. Andjelić (CD – 125 anniversary of Mathematical Institute Belgrade), Partial Differential and Integral Equations with Applications (co-authors S. Janković and P. Protić), Analytical Dynamics of Discrete Hereditary Systems (co-author O.A. Goroshko), The Vector Method of the Heavy Rotor Kinetic Parameters Analysis and Nonlinear Dynamics, and other.*

Editor in Chief of the Following Journals: *Facta Universitatis* (1990-2001), *Facta Universitatis Series Mechanics, Automatic Control and Robotics*, University of Niš (1991- 2009 ), and Editor of a number of Scientific Proceedings and ANN Monograph Advances in Nonlinear Sciences (Vol. 2, 2008)..

Member of Editorial Board of the following Journals: *International Journal of Nonlinear Sciences and Numerical Simulations*, Freund Publishing House LTD ( od 1999-), *Facta Universitatis Series Living and Working Environmental Protection*, University of Niš (2001- ), *Nauka Tehnika Bezbednost* (Science Technique Security), Institut bezbednosti, Beograd (2001- 2005) , *J. Mathematical Problems in Engineering*, Hindawi Press (2004-), *Journal of Non-Linear Modeling in Science and Engineering*, <http://www.demon.co.uk/cambsci/ijnms.html>, Scientific Technical Review SA (2006-) and other.

Referee of *Zentralblatt fur Mathematik und ihre Grenzgebiete Berlin* (more than 100 reviews) and Journals *Theoretical and Applied Mechanics*, JDM, Beograd.(1975-1997, 2003-), *Facta Universitatis Series Mechanics, Automatic Control and Robotics*, University of Niš (1990-), *Facta Universitatis Series Living and Working Environmental Protection*, University of Niš (1995-), *Facta Universitatis Series Mechanical Engineering, University of Niš* (1993-), *Neurosciences letters*, Elsevier, *Journal of Sound and Vibrations*, Elsevier, *European Polymer Journal*, Elsevier, *FME Transaction*, Faculty of Mechanical Engineering University of Belgrade, *Material Letters*, Elsevier, *Journal Nonlinear Analysis - Theory, Methods and Applications, Series B: Real-world Applications*, Pergamon Press, *Acta Mechanica Sinica*, JVS, *Journal of Solid and Structures*, *Nonlinear Dynamics*, *J. Of Nonlinear Mechanics*, *The Proceedings of Shanghai International Symposium on Nonlinear Science & Applications'03*, as a special issue of *International Journal of Bifurcation & Chaos* published by World Scientific Co., *Archive of Applied Mechanics - Manuscript Central Account Info (SY-23)*-Springer, *Workshop Preprints/Proceedings No 2004-1 IFAC workshop on Fractional Differentiation and its Applications FDA 04*, ENSEIRB, Bordeaux France, July 19-21, 2004. *Signal Processing*, Elsevier, ENOC 2005, EuroMech, and other.

**Professors:** *Draginja Nikolić, professor of Mathematics, Professor Dr Ing. Math. Danilo P. Rašković, Academician Yuriy Alekseevich Mitropoljskiy, Academician Tatomir P. Andjelić, Professor dr Dragoslav Mitrinović, Profesasor dr Jurij Korobov and other.*

**Subject Reference:** *Mechanics, Nonlinear Mechanics, Theory of Oscillations, Theory of Elasticity, Elastodynamics, Photoelasticity, Piezoelectricity, Ultrasonics, Electromechanical Systems, Mechanical Engineering, Applied Mathematics, Physical Mathematics; Strength of Materials, Machine Dynamics, Computational Mechanics, Control Motions and Nonlinear Dynamical Systems, Analytical Dynamics, Damage and Fracture Dynamics, Active Structure Dynamical Systems, History and Philosophy of Sciences.*

**Honours and Awards:**

Best graduate student of 1966/67 at Faculty of Mechanical Engineering, and Best graduate student of 1966/67 at University of Niš.

Best Thesis of Bachelor's (Master) degree at Yugoslav Faculties of Engineering, 1967.

**Fact:** *For period of 33 years (from 1960 to 1993) between students at Mechanical Engineering Faculty University of Niš K. (Stevanović) Hedrih is student whit best examine evaluations (9,67) and all exams in first examination term.*

Member of the Olympic Team of Yugoslavia at International Mathematical Olympiad in Vroclav Poland (1963)

“*Štafeta mladosti*” in 1969 and **Gold Watch Prize-present of Yugoslav President** with Signature Tito, 1969.

Medallion (Plague)“*Archimed*” and Charter 2007 of Scientific-Technical Institute of Serbian Army for scientific work.

Prize *Saint Volodimir (Nagrada Svatoga Volodimira)* for 2010 of Ukrainian Higher Education Academy of Sciences

Medallion (Plague) and Charter 2008 of Cankaya University, Ankara, Turkey for Scientific advances in **IFAC FDA Workshop Fractional differentiation and Applications.**

Medallion (Plague) and Charter 2010 of Cankaya University, Ankara, Turkey for Scientific advances in **International Conference Nonlinear Sciences and Complexity – NSC 2010.**

Gold Medallion of Faculty of Mechanical Engineering of Niš.1985,  
Medallion of Faculty of Mechanical Engineering of Niš for First Postgraduate Student – First Magistar.of Technical Science (Mechanics) 1995.

Prize of Local Editorial Zentralblatt Belgrade 1999;

First Prize of the Yugoslav Association of Pedagogues for Pedagogical Critique 2000;

*Short lectures at Scientific Congresses and Symposiums approximately 200; Invited Scientific Lectures at Scientific Congresses and Symposiums, and Seminars: approximately 50. Invited Plenary and Keynote Lectures more then 20.*

*Supervisor of Doctor of Technical Sciences Theses 8; Supervisor of Magister of Technical Sciences Theses 10; Member of scientific commissions for evaluations of scientific levels and defense of Doctor of Technical Sciences Theses 26 and of Magister of Technical Sciences Theses 27; Supervisor of graduated student (equivalent to Master degree now) works 10 and member of commissions for defense more then 100.*

*Scientific Project Leader 7 in area of basic sciences (Mechanics) and each with duration of 5 years and Scientific Sub Project Leader 3 supported by Ministry of Science; Researcher at Projects of Technology 5; Professional Projects in Mechanical Engineering (Project Leader (4) or Research (3)). Scientific Papers in International and National Journals and Chapters in Books: approximately 90, and total approximately more then 300.*

**Scientific Visits and participation in the Seminars or international Scientific Meetings** : multiple visits to Ukraine-Kiev, Lvov and Kharkov (1969, 1970, 1996, 1998, 2001, 2003), Russia-Moscow State University and Institute on Mechanics as well as Institute of Control and Institute of Mechanical Engineering Problems in Russia (1995, 97, 98, 2000, 2002, 2005, 2007, 2008), Poland- University of Cracow, Warsaw and Poznanj and Lodz (1963, ..... 1999, 2001, 2003, 2005, 2007, 2009), Germany GAMM ....., England (1993, 2003), Byelorussia, University of Waterloo, (1989), Canada, Institute of Technology Rochester (1989), Cornell University (1989) USA., Israel Institute of Technology (1992), Technical University of Athens (1997), Shanghai University China (1998, 2002), Poland Technical University Lodz (2000), Technical University of Denmark, Lyngby, Copenhagen Denmark (1977, 1999), Tsukuba University and Tensor Society .Japan (2002), M.C. Chaki Centre for Mathematics and Mathematical Sciences, Calcutta, India, 2003, University of Kalyani, India, 2003., University La Sapienza Roma IUTAM (2003), Romania Politehnika Timisoara (2002), Technical University of Wien (2003), Greece Aristotelian University Tesseloniki (2003), Tianjin University China 2004, University of Ljubljana (2002), ENSEIRB Bordeaux 2004, WCNA Orlando 2004, University of Luisiana, Lafayette USA 2006, University Otto von Geuricke 2004., Politehnika Warsaw 2004, University of Luxembourg 2005, ..... ICTAM Adelaide, Australia 2009, Porto 2008, Lisabon Portugal 2009, Brasil 2010, Virginia Tech 2010, University in Hagzhou 2010.)

Prof. Dr K. (Stevanović) Hedrih has been further honored with inclusion in Who's Who in Serbia and as a fellow of the American Biographical Institute Research Association. The American Biographical Institute also named her "Woman of the Year" for 1997, with biographical listings in Five Thousand Personalities of the World and the International Directory of Distinguished Leadership. International Directory of Distinguished Leadership (by the Editorial Board ABI)- Eighth Edition 1998. Member of the ABI's Research Board of Advisors -RBA 1998. Distinguished biography of the MILLENNIUM HALL OF FAME 1998- ABI. (Hall of Fame Testimonial Plaque). 2000 Millennium MEDAL OF HONOR - ABI 1998. ABI - American Biographical Institute - Research Fellow Recognition 1996 - 24K gold-plated coin engraved ABI Research Fellow. K. Hedrih is listed in the Directory of the European Research and Development and the Who's Who in European Research and Development 2003. 2000 Outstanding People if the 20th Century - Incorporating the Outstanding Achievement Awards, International Biographical Center Cambridge, CB2 3QP, England.(1998)  
IBC

#### **Professional Career:**

Assistant, Faculty of Mechanical Engineering, University of Niš, (1968-1975)

Assistant Professor, Faculty of Mechanical Engineering, University of Niš, (1975-1981)

Associate Professor, Faculty of Mechanical Engineering, University of Niš, (1981-1985)

Full Professor, Faculty of Mechanical Engineering, University of Niš, (1986-....)

Full Professor – Scientific Research Full Professor at Mathematical Institute SANU Belgrade (2009-..)

Full Professor on Mechanics at Technical Faculty in Bor University of Belgrade (1986-1989)

Full Professor on Theory of Vibrations Mechanical Engineering University of Priština (1994-)

Elected for Full Professor on Mechanics at Faculty of Technical Academy of Yugoslav National Army (1998)

**Head of the Chair for Mechanics (1977-1979, 1981-1983, 1986-2004)**

Vice-dean of Faculty of Mechanical Engineering University of Niš (1978-1980).

Seminar Leader: Theoretical and Applied Mechanics at Faculty of Mechanical Engineering University of Niš (1976-2005) and Seminar Nonlinear Dynamics – Milutin Milanković (2005-2009).

No

Project Leader in area of Mechanics at Mathematical Institute SANU - Belgrade (1990 - .....);

Project leader in area of Mechanical Engineering and Mechanics at Faculty of Mechanical Engineering University of Niš (1976 – 1995, 2001-2005, 2006-2010);

Expert of Yugoslav Ministry of Sciences, Technology and Development in area 1111 Mathematics, 1113 Physics and 1223 Mechanical Engineering.

President of Organizing Committee and Member of Scientific Committee of XXI Yugoslav Congress of Theoretical and Applied Mechanics Niš 1995 and XXII Yugoslav Congress of Theoretical and Applied Mechanics Vrnjačka Banja 1997; Symposium of Serbian Society of Mechanics "Nonlinear Problems in Mechanics" Arandjelovac 1983; "YUGOSLAV CONFERENCE ON NONLINEAR DETERMINISTIC AND STOCHASTIC PROCESSES IN DYNAMICAL SYSTEMS WITH APPLICATIONS" Niš 1991;; Minisymposium "Nonlinearity and Chaos in Engineering Dynamics" Niš 1995., The Fifth Symposium on Nonlinear Mechanics – The Nonlinear Sciences at the Threshold of Third Millennium Niš 2000.

Member of Governing Board of Mathematical Institute SANU Beograd (1994).

## SPISAK RADOVA

**Katica R. (Stevanovic) Hedrih**  
**u periodu 2005-2010**

**(List of Selected Papers – Period 2005-2010)**

### **I. Radovi publikovani u časopisima za period 2005-2010 godina**

(sa ISSN brojevima, kao i sa i bez impact faktora)

### **I. List of Papers published in Scientific Journals with categorization )**

#### **2010.**

1\* Hedrih (Stevanović) K., Optimal control in nonlinear system with no ideal constraints, Commun Nonlinear Sci Numer Simulat, journal homepage: [www.elsevier.com/locate/cnsns](http://www.elsevier.com/locate/cnsns), CNSNS 1579 No. of Pages 13, Model 3G

[Optimal control in nonlinear system with no ideal constraints](#), *Communications in Nonlinear Science and Numerical Simulation*, *In Press, Accepted Manuscript*, Available online 6 May 2010,

Katica R. (Stevanović) Hedrih

[Preview](#) [PDF \(574 K\)](#) | [Related Articles](#) (Science Direct)

(Stevanović) Hedrih KR. Optimal control in nonlinear system with no ideal constraints. Commun Nonlinear Sci Numer Simulat (2010), doi:10.1016/j.cnsns.2010.04.053

ISSN 1007-5704

M23=3

2\* Hedrih (Stevanović) K., Simonović J. D., *Non-linear dynamics of the sandwich double circular plate system*, Int. J. Non-Linear Mech. (2010), doi:10.1016/j.ijnonlinmec.2009.12.007

International Journal of Non-Linear Mechanics 2009. 12 . 007.

[Non-linear dynamics of the sandwich double circular plate system](#),

*International Journal of Non-Linear Mechanics*, *In Press, Corrected Proof*, Available online 4 January 2010

Katica R. (Stevanović) Hedrih, Julijana D. Simonović

[Preview](#) [PDF \(1676 K\)](#) | [Related Articles](#) (Science Direct)

K.R.(Stevanović) Hedrih, J.D.Simonović, Non-linear dynamics of the sandwich double circular platesystem, Int. J.Non-Linear Mech. (2010), doi:10.1016/j.ijnonlinmec.2009.12.007

ISSN 0020-7462

M21=8

IF= 1.716

3\* Katica R. (Stevanovic) Hedrih and Vera Nikolic-Stanojevic, **A MODEL OF GEAR TRANSMISSION: FRACTIONAL ORDER SYSTEM DYNAMICS**, (Research Article), Mathematical



Problems in Engineering, Received 24 January 2010; Revised 2 March 2010; Accepted 6 May 2010.

(<http://www.hindawi.com/journals/mpe/aip.972873.html>)

<http://www.hindawi.com/journals/mpe/aip.6.html>

**ISSN 1024-123x      M23=3      IF =0.553**

4\* Hedrih (Stevanović) K., Vibrations of a Heavy Mass Particle Moving along a Rough Line with Friction of Coulomb Type, ©Freund Publishing House Ltd., International Journal of Nonlinear Sciences & Numerical Simulation 10(11): 1705-1712, 2009

<http://www.freundpublishing.com/International Journal Nonlinear Sciences Numerical%20Simulation/MatrixPrev.htm>

K.R. (Stevanović) Hedrih, Vibrations of a Heavy Mass Particle Moving along a Rough Line with Friction of Coulomb Type, International Journal of Nonlinear Sciences and Numerical Simulation, Vol. 11, No.3 March 2010, pp. 203-210.

**ISSN 1565-1339      M21=8      IF= 8.479**

<http://www.reference-global.com/toc/ijnsns/11/3>

5\* Hedrih (Stevanović) K., Hedrih A. N., Eigen modes of the double DNA chain helix vibrations has been qualified for publication in Journal of Theoretical and Applied Mechanics (JTAM), no. 1, vol. 48, 2010., pp. 219-231

**ISSN 1429-2955      M23=3**

6\* Hedrih (Stevanović) K., Tensor equations of discrete dynamically defined and undefined systems with hereditary and creep light elements, Analele Stiintifice Ale Universitatii "Alexandru Ioan Cuza" Din (ASI (S.N) Matematica -Scientific Annals of "Al.I. Cuza" University of Iasi, Matematica, Tom XCI, 2010, f. 1, pp. 131-149.

**ISSN 1221-8421      M23=3**

7\* Hedrih (Stevanović) K., Raičević V., Jović S., Vibro-impact of a Heavy Mass Particle Moving along a Rough Circle with Two Impact Limiters, ©Freund Publishing House Ltd., International Journal of Nonlinear Sciences & Numerical Simulation 10(11): 1713-1726, 2009

<http://www.freundpublishing.com/International Journal Nonlinear Sciences Numerical%20Simulation/MatrixPrev.htm>

K.R. (Stevanović) Hedrih, V. Raičević, S. Jović, Vibro-impact of a Heavy Mass Particle Moving along a Rough Circle with Two Impact Limiters, International Journal of Nonlinear Sciences and Numerical Simulation, Vol. 11, No.3 March 2010, pp. 211-223.

**ISSN 1565-1339      M21=8      IF= 8.479**

8\* Camelia Frigoiu, Katica (Stevanovic) Hedrih - On the Geometrization of the Rheonomic Lagrangian Mechanical Systems Analele Universitatii Oradea, Fasc. Matematica, Tom XVII (2010), Issue No. 1, 89-97

**ISSN 1221 – 1265      M24=3**

## 2009

9\* Hedrih (Stevanović) K., Energy transfer in the hybrid system dynamics (energy transfer in the axially moving double belt system), Special Issue, **ARCHIVE OF APPLIED MECHANICS**, DOI 10.1007/s00419-008-0285-7. Archive of Applied Mechanics, (2009) vol.79, No.6-7 pp. 529-540.

<http://www.springerlink.com/nainfo.nbs.bg.ac.yu:2048/content/2081u5426316886m/>

<http://nainfo.nbs.bg.ac.yu.nainfo.nbs.bg.ac.yu:2048/Kobson/service/jcr.aspx?ISSN=0939-1533>

**ISSN 0939-1533      M23=3      IF= 0.993**

10\* Hedrih (Stevanović) K., Main chains and eigen modes of the fractional order hybrid multipendulum system dynamics, **IOP PUBLISHING PHYSICA SCRIPTA**, vol. T136, Phys. Scr. 78 (2008) 000000 (12pp) doi:10.1088/0031-8949/78/8/000000

<http://www.iop.org/EJ/journal/1402-489>

**ISSN 0031-8949      M23=3      IF= 1.088**

11\* Hedrih (Stevanović) K., Jović S., Models of Technological Processes on the Basis of Vibro-impact Dynamics, Scientific Technical Review, Vol.LIX,No.2,2009,pp.51-72.

**YU ISSN 1820-0206      M51=2**

## 2008

12\* Hedrih (Stevanović K., Energy analysis in a nonlinear hybrid system containing linear and nonlinear subsystems coupled by hereditary element (Article), **NONLINEAR DYNAMICS**, (2008) vol.51 br.1-2 str. 127 - 140. DOI 10.1007/s11071-007-9197-2  
ISSN 0924-090X (Print) 1573-269X, (Online), [Volume 51, Numbers 1-2 / January, 2008](#), pp. 127-140. DOI 10.1007/s11071-007-9197-2, SpringerLink Date, Tuesday, January 30, 2007.  
<http://www.springerlink.com.nainfo.nbs.bg.ac.yu:2048/content/rg2302474v1ru044/>  
<http://nainfo.nbs.bg.ac.yu.nainfo.nbs.bg.ac.yu:2048/Kobson/service/jcr.aspx?ISSN=0924-090X>  
**ISSN 0924-090X M21=8 IF = 1.758**  
**ISSN 0924-090X (Print) 1573-269X, (Online)**

13\* Hedrih (Stevanović K., Transversal forced vibrations of an axially moving sandwich belt system, Archive of Applied Mechanics, Springer, (2008) vol.78 br.9 str. 725-735  
<http://www.springerlink.com.nainfo.nbs.bg.ac.yu:2048/content/2081u5426316886m/>  
<http://nainfo.nbs.bg.ac.yu.nainfo.nbs.bg.ac.yu:2048/Kobson/service/jcr.aspx?ISSN=0939-1533>  
**ISSN 0939-1533 M23=3 IF= 0.825**



14\* Hedrih (Stevanović K. and Simonović J., Transversal Vibrations of a Double Circular Plate System with Visco-elastic Layer Excited by a Random Temperature Field, *International Journal of Nonlinear Sciences and Numerical Simulation*, 2008, Vol. 9, No.1, pp.47-50. <http://www.ijnsns.com/2008/TOC9.1.doc>  
<http://nainfo.nbs.bg.ac.yu.nainfo.nbs.bg.ac.yu:2048/Kobson/service/jcr.aspx?ISSN=1565-1339>  
**ISSN 1565-1339 M21=8 IF= 8.479**

15\* Katica (Stevanović) Hedrih, (2008), Energy transfer in double plate system dynamics, **Acta Mechanica Sinica**, Volume 24, Number 3 / June, 2008, pp. 331-344, DOI 10.1007/s10409-007-0124-z, Springer Berlin / Heidelberg, ISSN (567-7718 (Print) 1614-3116 (Online),  
<http://www.springerlink.com.nainfo.nbs.bg.ac.yu:2048/content/rg2302474v1ru044/>  
<http://www.springerlink.com.nainfo.nbs.bg.ac.yu:2048/content/248380442p246217/>  
**ISSN 0567-7718 M22=5 IF=0.939**

16\* Katica (Stevanović) Hedrih, (2008), Energy interaction between linear and nonlinear oscillators (Energy transient through the subsystems in the hybrid system), *ISSN 1027-3190. Ukr. mat. Qurn., 2008, t. 60, # 6, pp. 796-814.*  
<http://springerlink.com/content/5717572370176j67/>  
<http://nainfo.nbs.bg.ac.yu.nainfo.nbs.bg.ac.yu:2048/Kobson/service/ElecasDet.aspx?ID=34971&ISSN=0041-5995>  
**ISSN 0041-5995 M23(21)=3(8) (dvojezično)**  
**ISSN 1027-3190**

17\* Hedrih (Stevanović K., Vibration Modes of a axially moving double belt system with creep layer, Journal of Vibration and Control, (2008), 14(10-Sep): 1333-1347.  
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## 2008.

Kongres Internacionalne unije teorijske i primenjene mehanike **IUTAM ICTAM** se održava jednom u četiri godina i selekcija radova je veoma stroga. Oko 50% se odbija, a mali broj dobije priliku da usmeno predstavi svoje rezultate, u većini su to poster i sa 3 minuta prikaza.

U okviru **IUTAM ICTAM** Adelaide 2008, *Katica R. (Stevanović) Hedrih* održala je "Session **Lecture**" u trajanju od 20 minuta uključujući i diskusiju, u okviru sekcije Oscilacije struktura - SM19 :: Structural vibrations , kojom su predsedavali Co-chairs: *Marian Wiercigroch* (UK) and *Pedro Ribeiro* (Portugal).

Kategorizacija učešća u ICTAM sa orlnim kratkim predavanjem može se smatrati velikim priznanjem naučne rezultate, posebno, kada istražrač dolazi iz male zemlje, koja nije velesila u nauci, kakva je Srbije.

Naziv predavanja je:

*Katica R. (Stevanović) Hedrih (August 29, 2008, Fri-11:20-B)*

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Hedrih (Stevanović), K., (2007), *Analogy between dynamics of thermo-rheological and piezo-rheological pendulums*, Second International Symposium on Nonlinear Dynamics, 27-30 Oct., 2007, Shanghai, China <http://www.2007isnd.com/>

Hedrih (Stevanović), K. and Ljiljana Veljović, (2007), *Nonlinear dynamics of the heavy gyro-rotor with two skew rotating axes*. Second International Symposium on Nonlinear Dynamics, 27-30 Oct., 2007, Shanghai, China <http://www.2007isnd.com/>

## 2006.

Katica R. (Stevanović) Hedrih, ENERGY OSCILLATIONS IN THE SUBSYSTEM DYNAMICS OF THE HYBRID SYSTEM (OSCILACIJE ENERGIJE U DINAMICI PODSISTEMA HIBRIDNOG SISTEMA), *To the Memory of my Professors Tatomir P. Andjelic and Danilo P. Raskovic First Heads of the Department of Mechanics at Mathematical Institute SASA, Jubilarni seminar. "60 godina Matematičkog instituta SANU" a 40-to minutno predavanje po pozivu, publikovan Apstrakt.*

Katica R. (Stevanović) Hedrih, *Theoretical and Applied Mechanics of the Rigid and Solid Bodies. Mechanics of Materials (2006-2010) (Teorijska i primenjena mehanika krutih i čvrstih tela. Mehanika materijala.), savremeni problemi, prikaz rezultata projekta ON144002 i Matematički institut SANU, Jubilarni seminar - "60 godina Matematičkog instituta SANU" a 30-to minutno predavanje po pozivu, publikovan Apstrakt.*

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Hedrih (Stevanović) K. and Simonović, J., (2006), *Characteristic Eigen Numbers and Frequencies of the Transversal Vibrations of Sandwich System*, SEECCM 06 –First South-East European Conference on Computational Mechanics, Proceedings, Editors – M. Kojic and M Papadrakakis, Kragujevac, pp. 90-94. + CD. <http://www.seeccn.kg.ac.yu>. ISBN 86-81037-13-7, COBISS.SR-ID 131758092, udc 531/533(082)

Hedrih (Stevanović) K.: Multifrequency forced vibrations of thin elastic shells. In: CD Proc. of the Fifth EUROMECH Nonlinear Dynamics Conference, pp. 2417-2426. Eindhoven University of Technology (2005)

Hedrih (Stevanović), K., (2006), *Transversal vibrations of the axially moving double belt system with creep layer*, Preprints, 2<sup>nd</sup> IFAC Workshop on Fractional Differentiation and its Applications, 19-21 July, 2006, Porto, Portugal, pp.230-235.+CD. IFAC WS 2006 0007 PT, ISBN 972-8688-42-3, 978-972-8688-42-4.ISBN, <http://www.iser.ipp.pl>

Hedrih (Stevanović), K. (2006), *Transversal forced vibration of an axially moving sandwich double belt system*, The Sixth European Solid Mechanics Conference ESMC Budapest 2006. EuroMech Main Conference., predava u zasedanju sekcije Multibody Dynamics.

Hedrih (Stevanović), K. (2006), DYNAMICS OF THE AXIALLY MOVING SANDWICH MULTI BELT SYSTEM, International Conference "Actual Problems of Applied Mathematics and Mechanics", devoted 80-anniversary from birthday Ac. Rvachev V.L., on October 23-26, 2006 in Kharkov., Član naučnog odbora konferencije i sa radom.

Katica R. (Stevanović) Hedrih, DYNAMICS OF SANDWICH STRUCTURES (DINAMIKA SENDVIČ STRUKTURA), Invited Plenary Lecture, Medjunarodne konferencije Savremeni problemi u građevinarstvu - Current Problems in Civil Engineering, Građevinski fakultet u Subotici, Univerziteta u Novom Sadu, 2 i 3. jun 2006. Abstracts and CD Full paper.

## 2005.

Katica (Stevanović) Hedrih, *Transversal vibrations of the axially moving sandwich belts*, *Invited Lecture – 40 minutes*, *ISRAMES December 2-4, 2005. Kalyani, West Bengal, India. The International Symposium on "Recent Advances in Mathematical Sciences and Earth Sciences" 2nd to 4th December 2005. Department of Mathematics, University of Kalyani.*

Katica (Stevanović) Hedrih: *Measurements of dynamical systems integrity and fracture mechanics*, *Invited plenary lecture, ISUMEL 2005 Lviv, Ukraine, 7-й МІЖНАРОДНИЙ СИМПОЗИУМ УКРАЇНСЬКИХ ІНЖЕНЕРІВ-МЕХАНІКІВ У ЛЬВОВІ*, (МСУІМЛ — 7), 18 — 20 травня 2005 р., Присвячений 160-річчю Національного університету „Львівська політехніка”

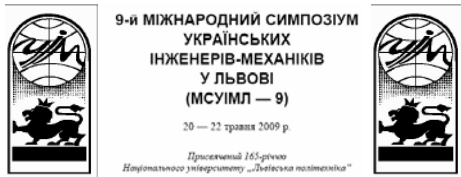
## VII\* Plenarna prefavanja ili predavanja po pozivu na naučnim skupovima štampani u apstraktu ili u celini (Plenary Lecture, Invited Lecture or Keynote Lecture presented at scientific meetings and published as Abstract of paper or full paper)

### 2010.

Hedrih (Stevanović) K., (2010), Discontinuity of kinetic parameter properties in nonlinear dynamics of mechanical systems, **Keynote Invited Lecture**, 9th Brazilian Conference on Dynamics, Control and Their Applications - 9<sup>o</sup> Congresso Temático de Dinâmica, Controle e Aplicações, June 07-11, 2010. UneSP, Sao Paulo (Serra negra), Brazil, Technical Program and Booklet of Abstracts, DINCON 2010, FUNUNeSP, Chair: pp. 14, Abstrac pp. 26  
<http://www.rc.unesp.br/igce/demac/dincon2010/instrucao.php>

### 2009.

#### 9th International Symposium Ukrainian Mechanical Engineers Lvov 2009 – ISUMEL 2009



Član Naučnog odbora i učesnik sa plenarnim predavanjem.

#### Održana predavanja

*Invited Plenary Lecture (45 minuta)- plenarno predavanje po pozivu u "Aktavom zalu" Lvovske politehnike.*

1\* Katica (Stevanović) HEDRIH, (2009), *Main chains and eigen modes of the hybrid homogeneous fractional order multichain system*, *Invited Plenary Lecture (45 minuta)*, Proceedings of 9th International Symposium Ukrainian Mechanical Engineers Lvov 2009 – ISUMEL 2009, Ministarstvo obrazovanja i nauke Ukraine, Lvov Polztechnique, Naukoviz žurnal "Mashonoznanstvo", ISBN 078-966-06-8, pp. 6-8.

Minisymposium Keynote Lecture:

Katica (Stevanović) Hedrih, Free and forced vibration of the heavy material particle along line with friction: Direct and inverse task of the theory of vibrorheology, 7<sup>th</sup> EUROMECH Solid Mechanics Conference, J. Ambrósio et.al. (eds.), Lisbon, Portugal, September 7-11, 2009, ESMC 2009 Book of Abstracts 'Mini'Symposia, izdanje Instituto Superior Tecnico, Lisbon, APMTAC, 2009, pp. 597-598, ISBN 9789899 626423

Katica (Stevanović) Hedrih, Free and forced vibration of the heavy material particle along line with friction: Direct and inverse task of the theory of vibrorheology, Booklet of Abstracts - ESMC

Lisbon 2009, Minisymposium Keynote Lecture, Minisymposium MS-24-Kinetics, Control and Vibrorheology - KINCONVIB – 2009, Faculty of Mechanical Engineering University of Niš, pp. 51-52.  
**ISBN 978-86-80587-94-3      COBISS.SR – ID 169182988      BarCod 9-788680-58794-3**

## 2008.

*Katica (Stevanović) HEDRIH, (2208), Dynamically determined and undetermined hereditary discrete systems* (External and internal degrees of freedom in the hybrid hereditary dynamics ), *Invited Lecture-Key note Lecture*, The Euromech Colloquium 498 Nonlinear Dynamics of Composite and Smart Structure (NDCS) -Nonlinear Dynamics and Chaos of Composite and Smart Structures (NDCS), May 21-23, 2008, Kazimierz Dolny, POLAND. Lublin 2008, pp. 29-39.

Katica (Stevanović) Hedrih, Mathematical analogy between hybrid system dynamics, 45 minutes Invited Plenary Lecture, Book of Extended Abstracts, Edited by Alexander M. Kovalev (IAMM NASU, [kovalev@iamm.ac.donetsk.ua](mailto:kovalev@iamm.ac.donetsk.ua)), 10<sup>th</sup> International Conference “Stability, Control and Rigid Bodies Dynamics” Donetsk (Ukraine), June 2008, pp. 125-127.

## 2007.

Hedrih (Stevanović), K., (2007), *Hybrid Systems and Hybrid Dynamics: Theory and Applications, Invited Plenary Lecture*, 8<sup>th</sup> HSTAM International Congress on Mechanics, Patras, 12 – 14 July, 2007, Greece, Proceedings, Edited by N. Bazwos, D.L. Karabalis, D. Polyzos, , D.E. Beskos and J. T. Katsikadelis, Volume I, pp. 77-86.

Hedrih (Stevanović), K., *Hybrid System Dynamics*, Proceedings, Invited Lecture, First International Congress of Serbian Society of Mechanics, Editors: D. Šumarac and D. Kuzmanović, Srpsko društvo za mehaniku, 10-13, April, 2007, pp. 79-84.  
<http://www.ssm.org.yu/congress2007/authors.html>

Goroško O. A. and Hedrih (Stevanović) K., Advances in development of the analytical dynamics of the hereditary discrete systems, Key Note Lecture, Minisymposium, Booklet of Abstracts - IDND 2007 – Analytical Dynamics of Discrete Hereditary System, pp. 27-34.

Goroshko O.A. and Hedrih (Stevanović), K., (2007), Construction of the Lagrange mechanics of the hereditary systems, Minisymposium Opening Minisymposia Lecture of the International Summer School APM – Advanced Problem in Mechanics- Integrity of Dynamical Systems, Saint Petersburg 2007., in Booklet of Abstracts - IDND 2007 – Analytical Dynamics of Discrete Hereditary System, Shanghai 2007, pp. 63-84.

Hedrih (Stevanović), K., (2007), *Tensor equations of the dynamics of the discrete systems with hereditary and creep light elements*, Conference on Differential Geometry, Lagrange and Hamilton Spaces. Dedicated to Acad. Radu Miron at his 80<sup>th</sup> anniversary, 2007, A.I.Cuza, University, Faculty of Mathematics, Iasi, Romania.. Book of Abstracts, pp. 18-22.

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Hedrih (Stevanović), K., (2007), *Energy Transfer in Hybrid System Dynamics*, Invited Participation, 6<sup>th</sup> Recent German-Greek-Polish Symposium, Recent Advances in Mechanics, September 17-21 2007, Alexandroupolis, Greece , Book of Abstracts, pp. 7-8.

## 2006.

Hedrih (Stevanović), K. (2006), DYNAMICS OF THE AXIALLY MOVING SANDWICH MULTI BELT SYSTEM, International Conference "Actual Problems of Applied Mathematics and Mechanics", devoted 80-

anniversary from birthday Ac. Rvachev V.L., on October 23-26,2006 in Kharkov., Član naučnog odbora konferencije i sa radom.

Hedrih (Stevanović), K. (2006), TENSOR EQUATIONS OF THE DYNAMICS OF THE DISCRETE SYSTEMS WITH HEREDITARY AND CREEP LIGHT ELEMENTS, 9<sup>th</sup> International Conf. of TENSOR 2006., THE 9<sup>th</sup> INTERNATIONAL CONFERENCE OF TENSOR SOCIETY ON DIFFERENTIAL GEOMETRY, FUNCTIONAL&COMPLEX, INFORMATICS AND THEIR APPLICATIONS, *Japan, Sept. 4-8, 2006.Tensor Society. 30.minutno predavanje po pozivu.*

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Katica R. (Stevanović) Hedrih, ENERGY OSCILLATIONS IN THE SUBSYSTEM DYNAMICS OF THE HYBRID SYSTEM (OSCILACIJE ENERGIJE U DINAMICI PODSISTEMA HIBRIDNOG SISTEMA), *To the Memory of my Professors Tatomir P. Andjelic and Danilo P. Raskovic First Heads of the Department of Mechanics at Mathematical Institute SASA , Jubilarni seminar . "60 godina Matematičkog instituta SANU" a 40-to minutno predavanje po pozivu, publikovan Apstrakt.*

Katica R. (Stevanović) Hedrih, *Theoretical and Applied Mechanics of the Rigid and Solid Bodies. Mechanics of Materials (2006-2010) (Teorijska i primenjena mehanika krutih i čvrstih tela. Mehanika materijala.), savremeni problemi, prikaz rezultata projekta ON144002 i Matematički institut SANU, Jubilarni seminar - "60 godina Matematičkog instituta SANU" a 30-to minutno predavanje po pozivu, publikovan Apstrakt.*

## 2005.

Katica (Stevanović) Hedrih, *Transversal vibrations of the axially moving sandwich belts , Invited Lecture – 40 minutes, ISRAMES December 2-4, 2005. Kalyani, West Bengal, India.The International Symposium on "Recent Advances in Mathematical Sciences and Earth Sciences" 2nd to 4th December 2005. Department of Mathematics, University of Kalyani.*

*Katica (Stevanović) Hedrih: Measurements of dynamical systems integrity and fracture mechanics, Invited plenary lecture, ISUMEL 2005 Lviv, Ukraine, 7-й МІЖНАРОДНИЙ СІМПОЗІУМ УКРАЇНСЬКИХ ІНЖЕНЕРІВ-МЕХАНІКІВ У ЛЬВОВІ, (МСУІМЛ — 7), 18 — 20 травня 2005 р., Присвячений 160-річчю Національного університету „Львівська політехніка”*

## VIII\* Član naučnog odbora internacionalnih aucnih skupova ili organizator minisimpozijuma

*(Member of Scientific Commitee of interantional scientific meetings and organizer of Minisymposia included in the Program of interantional scientific meetings )*

## 2010.

\* M11-Minisymposia Kinetics, Control and Vibrorheology at ICDVC-2010- The Third International Conference on Dynamics, Vibration and Control, 12-14 May 2010, Hangzhou,, China, Chinese Society of Theoretical and Applied Mechanics, 2010. <http://saa.zju.edu.cn/icdvc2010/>

Član Naučnog odbora i organizator Minisimpozijuma

*Member of Scientific Commitee of interantional scientific meeting and organizer of Minisymposia included in the Program.*

\*The 3rd INTERNATIONAL CONFERENCE "NONLINEAR DYNAMICS - 2010", at the NATIONAL TECHNICAL UNIVERSITY, "KHARKOV POLYTECHNICAL INSTITUTE", KHARKOV, UKRAINE, the 3rd ND-KhPI 2010 , the Nonlinear Dynamics Conference, from 21 until 24 September, 2010

Član Naučnog odbora.

*Member of Scientific Committee of international scientific meeting.*

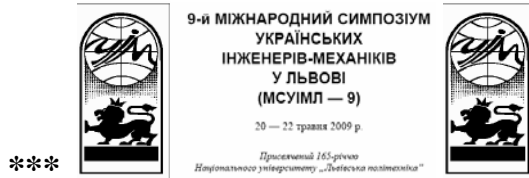
\* "3rd Conference on Nonlinear Science and Complexity" (NSC10), Cankaya University, Ankara, Turkey in the period of 26 - 29 July, 2010.

<http://nsc10.cankaya.edu.tr/index.php>

Član Naučnog odbora.

*Member of Scientific Committee of international scientific meeting.*

## 2009.



9th International Symposium Ukrainian Mechanical Engineers Lvov 2009 – ISUMEL 2009, Ministarstvo obrazovanja i nauke Ukraine, Lvov Polztechnique, Naukoviz žurnal "Mashonoznanstvo", ISBN 078-966-06-8.

Član Naučnog odbora i učesnik sa plenarnim predavanjem.

*Member of Scientific Committee of international scientific meeting and Plenary Lecturer.*

\*10<sup>th</sup> Conference on Dynamical Systems – Theory and Applications, Proceedings, DSTA Lodz 2009, Lodz, December 7-10, 2009, Poland, Department for Automatic and Biomechanics, Lodz, (see Proceedings - ISBN 978-83-929120-4-0, Vol. I and II).

Član Naučnog odbora.

*Member of Scientific Committee of international scientific meeting.*

\* Minisymposium MS-24-Kinetics, Control and Vibrorheology - KINCONVIB - 2009, European Society of Mechanics, Instituto Superior Tecnico - Lisbon and Mechanical Engineering Faculty in Niš - Project ON144002 - Seminar Nonlinear Dynamics - Milutin Milanković and MATHEMATICAL INSTITUTE SANU, Project ON144002, 2009.

**ISBN 978-86-80587-94-3**      **COBISS.SR – ID 169182988**      **BarCod 9-788680-58794-3**

Organizator minisimpozijuma.

*Organizer of Minisymposia included in the Program.*

## 2008.

\*The Euromech Colloquium 498 Nonlinear Dynamics of Composite and Smart Structure (NDCS) - Nonlinear Dynamics and Chaos of Composite and Smart Structures (NDCS), May 21-23, 2008, Kazimierz Dolny, POLAND. Lublin 2008, pp. 29-39.

Član Naučnog odbora i plenarno predavanje po pozivu.

*Member of Scientific Committee of international scientific meeting and Invited Lecture-Key note Lecture.*



## 2007.

\* **APM Saint Petersburg 2007** pp., Minisymposium, The International Summer School APM – Advanced Problem in Mechanics, Saint Petersburg 2007., pp. 133-156.

APM 2007 – *Minisymposium Integrity of Dynamical Systems – organized by Katica (Stevanović) Hedrih, Summer School. APM 2007 Advanced Problems in Mechanics, Russia, St. Petersburg June 20 - 28, 2007. Institute for Problems in Mechanical Engineering of the Russian Academy of Sciences, Izdavač Mašinski fakultet u Nišu, p. 379. ISBN 86-80587-67-2 COD 9 7886 80587677, BarCod 9 7886 80587677*

**ISBN 86-80587-67-2 COD 9 7886 80587677, BarCod 9 7886 80587677**

Organizator minisimpozijuma po pozivu.

*Invited organizer of Minisymposia included in the Program.*

\* First International Congress of Serbian Society of Mechanics, Editors: D. Šumarac and D. Kuzmanović, Srpsko društvo za mehaniku, 10-13, April, 2007, pp. 79-84.  
<http://www.ssm.org.yu/congress2007/authors.html>

Član Naučnog odbora i plenarno predavanje po pozivu.

*Member of Scientific Committee of interantional scientific meeting and Invited Lecture-Key note Lecture.*

\* **IDND 2007 – Analytical Dynamics of Discrete Hereditary Systems – Organized by Katica (Stevanović) Hedrih, Izdavač Mašinski fakultet u Nišu zam - Minisymposia - Analytical mechanics of the hereditary discrete systems**

Second International Symposium on Nonlinear Dynamics, 27-30 Oct., 2007, Shanghai, Donhua University, China, p-198. ISBN 978 – 86 – 80587 – 72 – 1 COBISS.SR – ID 144265740. BarCod 9 788680 56772 1  
<http://www.2007isnd.com/>

**ISBN 978 – 86 – 80587 – 72 – 1 COBISS.SR – ID 144265740. BarCod 9 788680 56772 1**

Organizator minisimpozijuma po pozivu.

*Invited organizer of Minisymposia included in the Program.*

\* *Minisymposium - Integrity of Dynamical Systems- ECF16, Organized by Katica (Stevanović) Hedrih, invited organizer of Minisymposia **IDS-ECF - the 16th European Conference of Fracture**, Greece 2006, Centre for Nonlinear Dynamics and Active Structures, Faculty of Mechanical Engineering University of Niš and Democritus University of Thrace, Xanthi, Greece, 2006. p. 324. ISBN 86-80587-57-5. BarCod 9 788680 587578. COBIS. SR - ID 130756620. UDK 531:01 /048); 530:182(048); 530:42 (048); 53:005.745 (100).*

**ISBN 86-80587-57-5.**

**BarCod 9 788680 587578. COBIS. SR - ID 130756620**

Organizator minisimpozijuma po pozivu.

*Invited organizer of Minisymposia included in the Program.*

## 2006.

Hedrih (Stevanović), K. (2006), DYNAMICS OF THE AXIALLY MOVING SANDWICH MULTI BELT SYSTEM, International Conference "Actual Problems of Applied Mathematics and Mechanics", devoted 80-anniversary from birthday Ac. Rvachev V.L, on October 23-26, 2006 in Kharkov.,

Član Naučnog odbora.

*Member of Scientific Committee of interantional scientific meeting.*

## 2005.

Katica (Stevanović) Hedrih, *Transversal vibrations of the axially moving sandwich belts , Invited Lecture – 40 minutes, ISRAMES December 2-4, 2005. Kalyani, West Bengal, India. The International Symposium on "Recent Advances in Mathematical Sciences and Earth Sciences" 2nd to 4th December 2005. Department of Mathematics, University of Kalyani.*

Član Naučnog odbora.

Member of Scientific Committee of international scientific meeting.

*Katica (Stevanović) Hedrih: Measurements of dynamical systems integrity and fracture mechanics, Invited plenary lecture, ISUMEL 2005 Lviv, Ukraine, 7-й МІЖНАРОДНИЙ СІМПОЗІУМ УКРАЇНСЬКИХ ІНЖЕНЕРІВ-МЕХАНІКІВ У ЛЬВОВІ, (МСУІМЛ — 7), 18 — 20 травня 2005 р., Присвячений 160-річчю Національного університету „Львівська політехніка”*

Član Naučnog odbora.

Member of Scientific Committee of international scientific meeting.

## IX. Učešće u vodećem naučnom kongresu IUTAM ICTAM u oblasti teorijske i primenjene mehanike u svetu (period 2005-2010)

Kongres Internacionalne unije teorijske i primenjene mehanike **IUTAM ICTAM** se održava jednom u četiri godina i selekcija radova je veoma stroga. Oko 50% se odbija, a mali broj dobije priliku da usmeno predstavi svoje rezultate, u većini su to poster i sa 3 minuta prikaza.

U okviru **IUTAM ICTAM** Adelaide 2008, *Katica R. (Stevanović) Hedrih* održala je “**Session Lecture**” u trajanju od 20 minuta uključujući i diskusiju, u okviru sekcije Oscilacije struktura - **SM19** :: **Structural vibrations**, kojom su predsedavali Co-chairs: *Marian Wiercigroch* (UK) and *Pedro Ribeiro* (Portugal).

Kategorizacija učešća u ICTAM sa orlnim kratkim predavanjem može se smatrati velikim priznanjem naučne rezultate, posebno, kada istraživač dolazi iz male zemlje, koja nije velesila u nauci, kakva je Srbije.

Naziv predavanja je:

*Katica R. (Stevanović) Hedrih (August 29, 2008, Fri-11:20-B)*

**Phenomenological mapping method and mathematical analogy of hybrid system dynamics**, XXII International Congress of Theoretical and Applied Mechanics Abstracts Book, Edited by J. Dernier, M.D. Fim and T. Mattner, Adelaide 2008, p. 317, ISSN 978-0-9805142-0-9, p. 317, and CD-ROM ISSN 978-0-9805142-1-6, pp. 10135, 1-2..  
(vidi WEB [ictam2008.adelaide.edu.au](http://ictam2008.adelaide.edu.au)).

**X\* U okviru projekta ON144002 radi seminar Nonlinear Dynamics - Milutin Milankovic na Mašinskom fakultetu. Vidi seriju publikaciju: Booklet of Abstracts - Minisymposium and WEB <http://www.mi.sanu.ac.rs/seminars/seminar16.htm>**

## XI\* Rukovodilac projekata u periodu 2000-2010:

**Project Leader Katica (Stevanović) Hedrih**

\* *ON1616 Realni problemi mehanike (2001-2005)*

\* *ON1616 Real Problem of Mechanics (2001-2005)*

Institution Coordinator: *Mathematical Institute Serbian Academy of Sciences and Arts.*

Project Leader: *Katica (Stevanović) Hedrih*

Researchers: *41.*

Researcher months: *approximately 98 months.*

Deo doktorske teze uradio Ljubiša Perić a radion na doktorskoj tezi mr Dragan Jovanović.

\* *ON1828 Dinamika i upravljanje aktivnih konstrukcija (2001-2005)*

\* *ON1828 Dynamics and Control of active Structures (2001-2005)*

Institution Coordinator: *Faculty of Mechanical Engineering University of Niš*

Project Leader: *Katica (Stevanović) Hedrih*

Researchers: 21

Researcher months: *approximately months.*

Deo doktorske teze *uradio Ljubiša Perić a doktorsku tezu radio mr Dragan Jovanović.*

**\* Projekt ON144002 Teorijska i primenjena mehanika krutih i čvrstih tela. Mehanika materijala.**

**\* Project ON144002 -Theoretical and Applied Mechanics of the Rigid and Solid Bodies.**

*Mechanics of Materials (2006-2010)*

Support: *Ministry of Sciences and Environmental Protection of Republic of Serbia*

Institution Coordinator: *Mathematical Institute Serbian Academy of Sciences and Arts.*

Project Leader: *Katica (Stevanović) Hedrih*

Researchers: 38.

Researcher months: *approximately 136 months.*

*U okviru istraživanja na projektu doktorsku disertaciju završ i odbranio mr Dragan Jovanović.*

Magistarske teze uradili i odbranili Julijana Simonović i Srdjan Jović. Sada rade istraživanja za izradu doktorata mr Julijana Simonović, mr Ljiljana Veljović i mr Srdjan Jović (mentor prof dr Vladimir Raičević).

### **XIII\* Mentor odbranjenih doktorskih disertacija i magistarskih teza u periodu 2005-2010.**

Mentor doktorske disertacije *dr Dragan Jovanović:*

**Jovanović D.,** (2009), *Potencijalna energija i stanje napona u materijalu sa prslinom, (Potential energy and stress state in material with crack)*, Doktorska disertacija, (odbrana 10 novembra 1009), Mašinski fakultet u Nišu, str.237.

Mentor magistarske teze *Mr Julijane Simonovic*

**Simonović J.,** (2008), *Dinamika mehaničkih sistema složenih struktura,* magistarski rad odbranjen 8 maj 2008. Mašinski fakultet u Nišu, str. 249.

Seriya konsultacije u izradi magistarske teze istraživaču na projektu ON144002 mr Srdjanu Joviću:

**Јовић С.,** (2009). *Енергијска анализа динамике виброударних система,* магистарски рад, одбрањен 06. Новембра 2009. Факултет техничких наука у Косовској Митровици Универзитета у Приштини, стр. 239.  
u saradnji sa mentorom magistarske teze *prof dr Vladimirom Raičevićem,*

### **XIVI\* Članstvo u redakcijama časopisa, uredništvima, naučnim društvima**

**Editorial of Journals:**

**1\* Editor in Chief of the Following Journals:**

*Facta Universitatis* (1990-2001) with 13 Series .

<http://facta.junis.ni.ac.rs/>

*Facta Universitatis Series Mechanics, Automatic Control and Robotics,* University of Niš (1991- 2008)

<http://facta.junis.ni.ac.rs/macar/macar.html>

ISSN 0354 – 2009 M24=3 IF =0,371

**2\* Associate Editor (2004-)**

*Mathematical Problems in Engineering,* Hindawi Publishing Corp. <http://www.hindawi.com/>

(<http://www.hindawi.com/journals/mpe/aip.972873.html>)

<http://www.hindawi.com/journals/mpe/aip.6.html>

<http://www.hindawi.com/journals/mpe/editors.html>

<http://www.hindawi.com/13168039.html>

ISSN 1024-123x M23=3 IF =0.553

**3\* Member of Editorial Board of the Following Journals:**

*International Journal of Nonlinear Sciences and Numerical Simulations*, ©Freund Publishing House Ltd., (2000-)

<http://www.cs.uky.edu/~jzhang/nsns.html>

<http://www.ijnsns.com/>

[http://www.freundpublishing.com/International\\_Journal\\_Nonlinear\\_Sciences\\_Numerical%20Simulation/Math.htm](http://www.freundpublishing.com/International_Journal_Nonlinear_Sciences_Numerical%20Simulation/Math.htm)

ISSN 1565-1339

M21=8

IF= 8.479

Scientific Technical Review, Vojske Srbije, (2005-) YU ISSN 1820-0206

<http://www.vti.mod.gov.yu/ntp/index.htm>

YU ISSN 1820-0206

M51=2

IF =0,040

*Journal of the Serbian Society for Computational Mechanics (2006- )*

[www.sscm.kg.ac.rs/jsscm/](http://www.sscm.kg.ac.rs/jsscm/)

**4\* Referee of Following Journals and Information Data-Base:**

Archive of Applied Mechanics - Manuscript Central Account Info (SY-23)-Springer, (4 recenzije samo u 2006)

Nonlinear Dynamics, Springer više recenzija

Workshop Preprints/Proceedings No 2006-2 IFAC workshop on Fractional Differentiation and its Applications FDA 06, Porto (desetak recenzija)

The European Union Control Association (32 recenzija u 2006)

ESIS European Conference of fracture 2006 (31 recenziju u 2006)

Zentralblatt fur Mathematik und ihre Grenzgebiete Berlin (desetak recenzija u 2006)

Facta Universitatis Series Mechanics, Automatic Control and Robotics, University of Niš (1990-)

*Mathematical Problems in Engineering*, Hindawi Publishing Corp. <http://www.hindawi.com/>

Neurosciences letters, Elsevier, Journal of Sound and Vibrations, Elsevier,

European Polymer Journal, Elsevier,

FME Transaction, Faculty of Mechanical Engineering University of Belgrade,

Material Letters, Elsevier,

Journal Nonlinear Analysis - Theory, Methods and Applications, Series B: Real-world Applications, Pergamon Press,

Signal Processing, Elsevier,

Journal of Porous Materials, Springer

ENOC 2005, EuroMech

Journal of Nonlinear Mechanics

Nonlinear Dynamics

and other.

**XV\* Članstvo u akademijama nauka i naučnim društvima u kojima se obavlja izbor članova tajnim glasanje na osnovu naučnih rezultata**

**Member of Academy of Sciences and Scientific Societies with elections on the basis of scientific results:**

\* Ukrainian Higher Education Academy of Sciences - Akademija nauka visokih skola i univerziteta Ukrajine ( od 1996-)



[www.anvsu.org.ua](http://www.anvsu.org.ua)

\* Naučno društvo Srbije - Serbian Scientific Society ( 2008- )



Naučno društvo Srbije

Serbian Scientific Society

<http://www.rcub.bg.ac.rs/~nds/>

<http://www.rcub.bg.ac.rs/~nds/indexe.html>

\* Akademija nelinearnih nauka – Academy of Nonlinear Sciences - Moscow (1997- )

\* Južnoslovenska akademija nelinearnih nauka u Srbiji JANN -  
SouthSlavian Academy of Nonlinear Sciences – SANS Belgrade (1997- )  
<http://www.masfak.ni.ac.rs/sitegenius/topic.php?id=786>

\* Naučni sekretar JANN – Scientific Secretary of SANS (1998-20010)

#### XVI\* Member of Professional-Scientific Societies:

American Academy of Mechanics AAM  
Member of GAMM – Germany (since 1972)  
Member of Tensor Society - Japan  
Member of International ASME – International American Society of Mechanical Engineers USA (od 2000 - )  
Member of European Society for Mechanics – EuroMech  
Member of M.C.Chaki Centre for Mathematics and Mathematical Sciences – Calcutta, India  
Member of SSM-JDM  
Member of Serbian Society of Computational Mechanics

[www.sscm.kg.ac.rs/jsscsm/](http://www.sscm.kg.ac.rs/jsscsm/)

Member of Society of Nonlinear dynamics in Human Factors – Adelaide , Australia.

#### XVII\* Citati ( Subject: Citation ) (2005-2010)

Najmanje dvadesetak citata, u periodu 2006-2010, u časopisima sa ISI liste, a više od 150 u radovima publikovanim u domaćim časopisima i doktoraskim i magistarskim disertacijama autora iz Srbije.

##### \* Citati u časopisima sa ISI liste (izbor)

Na primer:

\* Hedrih (Stevanović) K., Filipovski A., (2002), *Longitudinal Vibration of a Fractional Derivative Order Rheological Rod with Variable Cross Section*, Facta Universitatis, Series Mechanics, Automatic Control and Robotics, Vol. 3 No. 12, 2002. pp.327-350. YU ISSN 0534-2009.

<http://facta.junis.ni.ac.yu/facta/macar/macar2002/macar2002-02.html>

##### \* Cited (quoted) in:

Jakšić N., Boltežar M., (2005), Viscously damped transverse vibrations of a moving string, Journal of Mechanical Engineering – Strojniški vestnik, vol.51. No.9/05 Issue 485, pp. 560-569. ISSN 0039-2480. **ISI List**

\*\*

Hedrih (Stevanovic') K.: Interpretation of the transfer of energy from high-frequency to low-frequency modes by averaging asymptotic method Krilov-Bogolybov-Mitropolsky. In.: Proc. of the Second International Conference "Asymptotics in Mechanics", pp. 97-104. Saint-Petersberg State Marine Technological University, Saint-Petersberg (1997)

Hedrih (Stevanovic') K.: Multifrequency forced vibrations of thin elastic shells. In: CD Proc. of the Fifth EUROMECH Nonlinear Dynamics Conference, pp. 2417-2426. Eindhoven University of Technology (2005)

*Cited (quoted) in:*

Kozmin A., Mikhlin Yu. and C. Pierre, Transient in a two DOF nonlinear Systems, Nonlinear Dynamics, 2006; Nonlinear Dynamics, Volume 51, Numbers 1-2 / January, 2008 , DOI: 10.1007/s11071-007-9198-1

##### \* Citati na moje radove nalaze se i u sledećim publikovanim radovima:

Q. Li and Y. H. Chen, Why traction-free? Piezoelectric crack and Coulombic traction, Journal Article , *Archive of Applied Mechanics, Volume 78, Number 7 / July, 2008* DOI: 10.1007/s00419-007-0180-7

Pei-Wei Zhang, Zhen-Gong Zhou and Lin-Zhi Wu, Coupled field state around three parallel non-symmetric cracks in a piezoelectric/piezomagnetic material plane, Journal Article. *Archive of Applied Mechanics, Volume 79, Number 10 / October, 2009* , DOI: 10.1007/s00419-008-0270-1

Yufeng Xing and Bo Liu, Closed form solutions for free vibrations of rectangular Mindlin plates, Journal Article, *Acta Mechanica Sinica, Volume 25, Number 5 / October, 2009* , DOI: 10.1007/s10409-009-0253-7

Yufeng Xing and Bo Liu, New exact solutions for free vibrations of rectangular thin plates by symplectic dual method, Journal Article, *Acta Mechanica Sinica*, Volume 25, Number 2 / April, 2009, DOI: 10.1007/s10409-008-0208-4  
Journal Article

Q. Li and Y. H. Chen, Why traction-free? Piezoelectric crack and Coulombic traction, *Archive of Applied Mechanics*, Volume 78, Number 7 / July, 2008, DOI: 10.1007/s00419-007-0180-7

**\* Citati u delima domaćih autora:**

Veliki broj citata u sledećim disertacijama:

**Jovanović D.**, (2009), *Potencijalna energija i stanje napona u materijalu sa prslinom*, (*Potential energy and stress state in material with crack*), (odbrana 10 novembra 1009), Doktorska disertacija, Mašinski fakultet u Nišu, str.237.

**Simonović J.**, (2008), *Dinamika mehaničkih sistema složenih struktura*, magistarski rad odbranjen 8 maj 2008. Mašinski fakultet u Nišu, str. 249.

**Јовић С.**, (2009). *Енергијска анализа динамике виброударних система*, магистарски рад, одбрањен 06. Новембра 2009. Факултет техничких наука у Косовској Митровици Универзитета у Приштини, стр. 239.

**Mirko Blagojević** (2008), Naponsko i deformaciono stanje elemenata cikloreduktora pri dinamičkom opterećenju, Mašinski fakultet u Kragujevcu, str.224..

**\* Jedan broj citata na moje radove se može naći u radovima publikovanim u sledećim časopisima:**

\* Scientific Technical Review, Vojske Srbije, (2005-) YU ISSN 1820-0206  
<http://www.vti.mod.gov.yu/ntp/index.htm>  
YU ISSN 1820-0206 M51=2 IF =0,040

\* *Facta Universitatis Series Mechanics, Automatic Control and Robotics*, University of Niš (1991- 2008). <http://facta.junis.ni.ac.rs/macar/macar.html>  
ISSN 0354 – 2009 M24=3 IF =0,371

\* FME Transactions - Scientific Journal published by Faculty of Mechanical Engineering. Faculty of Mechanical Engineering, University of Belgrade  
<http://www.mas.bg.ac.rs/transactions/index.html>  
YU ISSN 1451-2092 M51=2

**XVIII\* Nagrade i priznanja u periodu 2005-2010**

Medallion (Plague)“*Archimed*” and Charter 2007 of Scientific-Technical Institute of Serbian Army for scientific work.

Medallion (Plague) and Charter 2008 of Cankaya University, Ankara, Turkey for Scientific advances in IFAC FDA Workshop.

**XIX\* Recenzije za inostrane fondacije i ministarstva nauke (Referee for aboard foundation of sciences and Ministry of Sciences other countries)**



Recenzija sadržaja projekta registrovanog pod oznakom:

**Project proposal No. 101/09/1481 submitted in the current round of GA CR Call for Proposals.**  
iz osnovnih nauka na poziv Češke fondacije za nauku (CSF - GACR - application for 2009 - 101/09/1481, Subject: CSF - Czech Science Foundation, "CSF - Czech Science Foundation" <[info@gacr.cas.cz](mailto:info@gacr.cas.cz)>) prema pozivu d 3 jula 2008 godine.

U potpisu poyiva je:

Hana Jirmanova

Head of Department of Technical Sciences

Email: [hana.jirmanova@gacr.cas.cz](mailto:hana.jirmanova@gacr.cas.cz)

On behalf of the **Czech Science Foundation (GA CR)**, the major funding body in the Czech Republic that supports all scientific areas of basic research including the international projects, to ask you whether you would be prepared to evaluate a project proposal No. 101/09/1481 submitted in the current round of GA CR Call for Proposals.

## **XX\* Predavanja na sminarima u Matematičkom institutu SANU u periodu 2005-2010.**

### **1\* Mechanics Colloquium - Odelenje za mehaniku Matematickog institute SANU**

SREDA, 17. mart 2010. u 18 sati:

*Katica (Stevanovic) Hedrih, Matematicki institut SANU Beograd*

**TRIGGER OF COUPLED SINGULARITIES IN NONLINEAR DYNAMICS OF A HEAVY MASS PARTICLE ALONG ROTATE ROUGH CIRCLE**

SREDA, 14. oktobar 2009. u 18 sati:

*Katica R. (Stevanovic) Hedrih, Masinski fakultet, Nis*

**VISIBILITY OF NONLINEARITY**

UTORAK, 14. oktobar 2008. u 14 sati:

*Prof. Katica (Stevanović) Hedrih, Mašinski fakultet Niš*

**PHENOMENOLOGICAL MAPPING METHOD AND MATHEMATICAL ANALOGY OF HYBRID SYSTEM DYNAMICS**

SREDA, 5. decembar 2007. u 18 sati:

*Katica (Stevanović) Hedrih, Mašinski fakultet, Niš*

**PREDSTAVLJANJE REZULTATA PROJEKTA ON 144002**

**Projekt ON144002 Teorijska i primenjena mehanika krutih i cvrstih tela. Mehanika materijala. (2006-2010)**

SREDA, 17. oktobar 2007. u 18 sati:

*Katica (Stevanovic) Hedrih, Masinski fakultet, Nis*

**Pojmovi nelinearne dinamike i Aleksandr Mikhailovich Lyapunov (1857 ~V 1918) A.M.Lyapunov**

SREDA, 16. maj 2007. u 18 sati:

*Katica (Stevanovic') Hedrih, Ma~Zinski fakultet, Ni~Z*

**Novi prikazi klasicne dinamike rotora (ili Novi pogled u Kinetiku rotora)**

SREDA, 17. maj 2006. u 18 sati:

*Katica (Stevanovic) Hedrih, Julijana D. Simonovic (Masinski fakultet, Nis)*

**SLOBODNE TRANSVERZALNE OSCILACIJE ELASTICNO SPREGNUTIH KRUNIH PLO?A**

SREDA, 12. april 2006. u 18 sati:

*K. S. Hedrih*

**Transversal vibrations of the axially moving sandwich band and string (Transverzalne oscilacije aksijalno pokretne sendvic trake i strune)**

SREDA, 01. mart 2006. u 18 sati:

*Katica (Stevanovic) Hedrih*

**Nelinearna dinamika - Interdisciplinarni pristup**

SREDA, 26. oktobar 2005. u 18 sati:

*Katica (Stevanović) Hedrih*

**Transversal Vibration of a Parametrically Excited Beam: Influence of Rotatory Inertia and Transverse Shear on Stochastic Stability of Deformable Forms and Processes**

SREDA, 21. septembar 2005. u 18 sati:

*Katica (Stevanović) Hedrih*

**Dostignuća Nelinearne dinamike**

SREDA, 08. jun 2005. u 18 sati:

*Katica Stevanovic-Hedrih,*

**Memorijalno predavanje povodom 20. godina od smrti [prof. Danila Raskovica](#)**

**Prof. dr ing dipl. math. Danilo P. Raskovic (1910-1985), upravnik Odeljenja za mehaniku Matematickog instituta SANU u 1962. godini.**

SREDA, 25. maj 2005.:

16:00-16:40, Katica Stevanovic-Hedrih,

**Mere integriteta dinamičkih sistema.**

SREDA, 02. mart 2005. u 18 sati:

*Katica Stevanovic Hedrih*

**VIŠEFREKVENTNE NELINEARNE OSCILACIJE TANKE ELASTICNE LJUSKE SA POZITIVNOM GAUSS-OVOM KRIVINOM I KONACNIM DEFORMACIJAMA**

(Predavanje je posvećeno sećanju na profesora dr Ing. dipl. Math. Danila P. Raskovica (10. septembar 1910-29. januar 1985), jednog od Upravnika Odeljenja za mehaniku Matematickog instituta SANU (1962), a povodom 20. godina od smrti.)

SREDA, 01. decembar 2004. u 18 sati:

*Katica Stevanovic Hedrih, Spasoje Gadzic*

**O JEDNOM MODELU DINAMIKE KRUTIH TELA VELIKIH BRZINA**

## **2\* Seminar Nonlinear dynamics - Milutin Milankovic - Project ON144002**

Cetvrtak, 8. oktobar 2009. u 11,00 h na Masinskom fakultetu u Nisu, u svećanoj sali 401.

*Katica R. (Stevanovic) Hedrih*

**Vibrations, Energy and Powers of Force Works of a Material Particle Motion along Rough Line with Friction of Coulomb Type**

Cetvrtak, 15. oktobar 2009. u 11,00 h na Masinskom fakultetu u Nisu, u svećanoj sali 401.

*Katica R. (Stevanovic) Hedrih*

**Vibro-impact system dynamics: Heavy material particle oscillations along rough circle with radial two side impact limiter of the elongations**

Cetvrtak, 22. oktobar 2009. u 11,00 h na Masinskom fakultetu u Nisu, u svećanoj sali 401.

*Katica R. (Stevanovic) Hedrih*

**Considering Transfer of Signals through Hybrid Fractional Order Homogeneous Structure**

Cetvrtak, 29. oktobar 2009 u 11,00 h na Masinskom fakultetu u Nisu, u svećanoj sali 401.

*Katica R. (Stevanovic) Hedrih*

### **Optimal Control in Engineering systems with trigger of coupled singularities**

Četvrtak, 12. februar 2009. u 12.00 h na Mašinskom fakultetu u Nišu, u Laboratoriji L 307.  
Katica R. (Stevanović) Hedrih

**„Beseda o MEHANICI, mojim profesorima, kolegama i studentima“**  
Nastavak besede i diskusija.

Četvrtak, 5. februar 2009. u 12.00 h na Mašinskom fakultetu u Nišu, u Laboratoriji L 307.  
Katica R. (Stevanović) Hedrih

**„Beseda o MEHANICI, mojim profesorima, kolegama i studentima“**  
(„Onn Mechanics, as well as on my Professors, Colleagues and Students“)  
povodom 445 godina od rođenja Galileo Galilei (15 February 1564 – 8 January 1642) i 130 godina od rođenja Milutina Milankovića (1879 - 1958), posvećeno profesorima Draginji Nikolić, Danilu Raskoviću, Tatomiru Andjeliću i Yuriju Mitropoljskom.

Sreda, 3. decembar 2008. u 18,00 h

Katica R. (Stevanović) Hedrih

**MAIN CHAINS AND EIGEN MODES OF THE FRACTIONAL ORDER HYBRID MULTI PENDULUM SYSTEM DYNAMICS**

ČETVRTAK, 6. DECEMBRA 2007. godine sa početkom u 11.00 časova

Katica (Stevanović) Hedrih

**Mehanika krutog tela i Leonhard EULER**  
**Rigid body dynamics and Leonhard Euler (1707-1783)**

ČETVRTAK, 5. APRILA 2007. godine sa početkom u 13.00 časova

Katica (Stevanović) Hedrih

**Hibridni sistemi i hibridne dinamike: Teorija i primene**  
**Hybrid Systems and Hybrid Dynamics: Theory and Applications**

### **3\* Seminar for Geometry, education and visualization with applications**

ČETVRTAK, 06.05.2010. u 17 sati, sala 301f, MI

Katica Stevanovic Hedrih

**Vektori položaja materijalnih tacaka reonomnog sistema i njihovi tangentni triedri i N-jedri vektorskih baza u razlicitim sistemima krivolinijskih koordinata**

ČETVRTAK, 12.11.2009. u 17 h Matematički fakultet u Beogradu

Katica (Stevanović) Hedrih

**Coriolis-ova sila inercije u dinamici mehanickog sistema i transformacije koordinata iz Descartes-ovog u generalisani sistem ortogonalnih krivolinijskih koordinata**  
(predavanje je posveceno akademiku Milevi Prvanovic, povodom 80-tog rođendana)

### **4\* Seminar for the History and Philosophy of Mathematics and Mechanics**

UTORAK, 06. april 2010. u 12:15 sati

Prof. Dr Katica R. Stevanovic-Hedrih, Matematički institut SANU, Beograd

**KOORDINATNI SISTEMI I KOORDINATE VEKTORA I SILE INERCIJE**

UTORAK, 16. mart 2010. u 12:15 sati

Prof. Dr Katica R. Stevanović-Hedrih, Matematički institut SANU, Beograd

**POVODOM: VEKTOR, ŠTA JE TO?**

UTORAK, 20. oktobar 2009. u 12:15 sati

Prof. Dr Katica Stevanović-Hedrih, Mašinski fakultet, Univerzitet u Nišu

## **FORMALIZAM TRANSFORMACIJE KOORDINATA, DINAMIČKI (MEHANIČKI) SISTEMI I SILE INERCIJE**

UTORAK, 18. novembar 2008. u 12:15 sati

*Prof. dr Katica Stevanović-Hedrih, Mašinski fakultet, Univerzitet u Nišu*  
**MEHANIKA KRUTOG TELA I LEONARD OJLER**

UTORAK, 24. mart 2009. u 12:15 sati

*Prof. Dr Katica Stevanović-Hedrih, Mašinski fakultet, Univerzitet u Nišu*  
**GALILEO GALILEI I KINETIKA**

## **5\* Seminar on Applied Mathematics**

Utorak, 24.11.2009. u 14:15. sala 301f. MI SANU:

*Katica R. (Stevanović) Hedrih*

**THE OPTIMAL CONTROL IN ENGINEERING NONLINEAR SYSTEMS WITH TRIGGER OF COUPLED SINGULARITIES**

Utorak, 17.02.2009. u 14:15. sala 305. MI BG:

*Katica (Stevanović) Hedrih, Mašinski fakultet, Niš*

**MAIN CHAINS AND EIGEN MODES OF THE FRACTIONAL ORDER HYBRID SYSTEM VIBRATIONS**

## **XX\* Gostovanje na nasim seminarima inostranih profesora po pozivu na inicijativu K. Hedrih u periodu 2006-2010.:**

March 28, 2009 at 11,30h

**Valery V. Kozlov**, Real member and vice-president of Russian Academy of Science, Steklov Mathematical Institute RAS, Moscow, Russia

*Opening Lecture Seminar Nonlinear Dynamics – Milutin Milankovic*

**В.В. Козлов: СПЕКТРАЛЬНЫЕ СВОЙСТВА КОНЕЧНОМЕРНЫХ ОПЕРАТОРОВ И ЗАДАЧА О ГИРОСКОПИЧЕСКОЙ СТАБИЛИЗАЦИИ**

**Valery V. Kozlov: Spektralna svojstva konačnodimenzionalnih operatora i zadatak giroskopske stabilizacije**

SREDA, 11. novembar 2009. u 18 sati:

*E.E. Gdoutos, Office of Theoretical and Applied Mechanics of the Academy of Athens School of Engineering, Democritus University of Thrace, GR-671 00 Xanthi, Greece E-mail: egdoutos@civil.duth.gr*

**FAILURE MECHANISMS OF COMPOSITE SANDWICH STRUCTURES**

SREDA, 7. maj 2008. u 18 sati:

*Prof. Giuseppe Rega, Dipartimento di Ingegneria Strutturale e Geotecnica, Sapienza Università di Roma*  
**CONTROL OF BIFURCATION, CHAOS AND BASIN INTEGRITY: THEORETICAL ISSUES AND APPLICATION**

PETAQ, 23. NOVIMBRA 2007. godine sa početkom u 11,00 časova

*Academician Radu Miron, Faculty of Mathematics, University "A.I.Cuza" Iasi, Iasi, Romania*  
**UNIVERSITATEA „ALEXANDRU IOAN CUZA”, FACULTATEA DE MATEMATICĂ**

*Bulevardul Carol I, nr. 11 / 700506 – Iași, R O M Â N I A, E-mail: radu.miron@uaic.ro*  
*održiće predavanje pod nazivom*

**Lagrangian and Finslerian Mechanics of Nonconservative Mechanical Systems**

U PETAK, 23. NOVEMBRA 2007. godine sa početkom u 12.00 časova

**Camellia Frigioiu**, University "Dunarea de Jos", Department of Mathematics  
Str. Domneasca nr 47, Galati - 800008, ROMANIA, [Camelia.Frigioiu@ugal.ro](mailto:Camelia.Frigioiu@ugal.ro)

### **The Dynamical Systems of Rheonomic Finslerian Mechanical Systems**

U TORAK, 12. DECEMBRA 2006. godine sa početkom u 14.00 časova

**Alexander P. Seyranian** D.Sc, Ph.D, Leading Research Fellow, Institute of Mechanics,  
Moscow State Lomonosov University, održaće predavanje pod nazivom

### **MULTIPARAMETER STABILITY THEORY WITH MECHANICAL APPLICATIONS**

U CETVRTAK, 1. JUNA 2006. godine sa pocetkom u 12.00 casova

**J.T. Katsikadelis**, Academy of Athens, Office of Theoretical and Applied Mechanics & School of Civil  
Engineering, National Technical University of Athens, Greece.

### **The BEM for Nonlinear Vibrations of Plates with Variable Stiffness and Mass Properties**

**ON174001 - Dynamics of hybrid systems with complex structures. Mechanics of materials. (2011-2014)**

**ON174001 – Dinamika hibridnih sistema slozenih struktura. Mehanika materijala . (2011-2014)**

**Support:** *Ministry of Education, Sciences and Technology of Republic of Serbia*

**Institution Coordinator:** *Mathematical Institute Serbian Academy of Sciences and Arts.*

**Project Leader:** *Katica (Stevanović) Hedrih*

**Researchers:** 38.

### **Report – Research Results in 2011 and 2012.**

## **List of References – Researchers:**

### **List of References in 2011**

## **Katica R. (Stevanovic) Hedrih**

1\* Hedrih (Stevanović) R. Katica, (2010), Ceo život posvećen mehanici, inženjerstvu i matematici, Danilo P. Rašković(28 avgust 1910-29 januar 1985), Povodom 100 godina od rođenja služnog Užičanina, časopis Istorijskog arhiva Užica, Istorijaska baština, 2010, br 10, str. 155-192.

Istorijski arhiv Užica, Istorijaska baština

2\* Hedrih (Stevanović) K., Optimal control in nonlinear system with no ideal constraints, Commun Nonlinear Sci Numer Simulat, journal homepage: [www.elsevier.com/locate/cnsns](http://www.elsevier.com/locate/cnsns), CNSNS 1579 No. of Pages 13, Model 3G  
[Optimal control in nonlinear system with no ideal constraints](#), *Communications in Nonlinear Science and Numerical Simulation*, *In Press, Accepted Manuscript*, Available online 6 May 2010,  
Katica R. (Stevanović) **Hedrih**

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Frigioiu, C.<sup>a</sup>, Hedrih, K.<sup>b</sup>, Bîrsan, I.G.<sup>c</sup>

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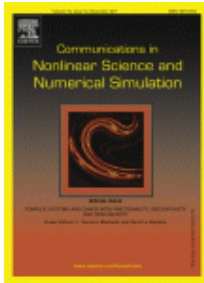
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**Hedrih, Katica (Stevanovic); Raicevic, Vladimir; Jovic, Srdjan**

**Phase trajectory portrait of the vibro-impact forced dynamics of two heavy mass particles motions along rough circle**

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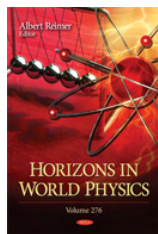
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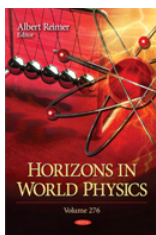
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21\* Hedrih (Stevanović) Katica, (2012), Tangent space extension of the position vectors of a discrete rheonomic mechanical system, *Bull. Cal. Math. Soc.*, **104**, (2) 81- 102 (2012)

22\* Hedrih (Stevanović) Katica, (2012 ili 13), Vector method based on mass moment vectors and vector rotators applied to rigid-body multi-coupled rotations around no intersecting axes, invited and accepted by guset Editor Jan Awrejcevicz and submitted for possible publishing in specual Issue of International Journal of Structural Stability and Dynamic, ( wait Editorial drcision of Editor in Chief of Journal). ISSN 0219-4554.

23\* Hedrih (Stevanović) K., (2012), APPROXIMATIONS OF NONLINEAR DIFFERENTIAL EQUATION SOLUTIONS, Two pages paper, CD-Proceedings of **23<sup>rd</sup> International Congress of Theoretical and Applied Mechanics, (ICTAM Beijing 2012)**, 19-24 august 2012, SM16 Vibrations and control of structures, **International Union of Theoretical and Applied Mechanics**. SM16-053 pp. SM16-053:1-2, <http://www.ictam2012.org/>, ISBN 978-16022-3-7

24\* Hedrih (Stevanović) K., (2012), APPROXIMATIONS OF NONLINEAR DIFFERENTIAL EQUATION SOLUTIONS, Abstract book of **23<sup>rd</sup> International Congress of Theoretical and Applied Mechanics**, Editors: Yilon Brll, Jianxian Wang and Daining Fang, **(ICTAM Beijing 2012)**, 19-24 august 2012, SM16 Vibrations and control of structures, Seminar Session, **International Union of Theoretical and Applied Mechanics** . SM16-053, p. 79. <http://www.ictam2012.org/>, ISBN 978-16022-3-7

25\* Hedrih A., (2012), FREQUENCY ANALYSIS OF KNOT MASS PARTICLES IN OSCILLATORY SPHERICAL NET MODEL OF MOUSE *ZONA PELLUCIDA*, Two pages paper, CD-Proceedings of CD-Proceedings of **23<sup>rd</sup> International Congress of Theoretical and Applied Mechanics, (ICTAM Beijing 2012)**, 19-24 august 2012, **SM01 Biomechanics and biomaterials, Lecture Session**, SM01-049, <http://www.ictam2012.org/>, ISBN 978-16022-3-7

26\* Hedrih A., (2012), FREQUENCY ANALYSIS OF KNOT MASS PARTICLES IN OSCILLATORY SPHERICAL NET MODEL OF MOUSE *ZONA*

*PELLUCIDA* Abstract book of **23<sup>rd</sup> International Congress of Theoretical and Applied Mechanics**, Editors: Yilon Brill, Jianxian Wang and Daining Fang, (**ICTAM Beijing 2012**), 19-24 avgust 2012., **SM01 Biomechanics and biomaterials, Lecture Session**, SM01-049, p. 209. <http://www.ictam2012.org/>

27\* Hedrih (Stevanović) K., (2012), Free Nonlinear Dynamics of a Heavy Mass Particle along Rotating Rough urvilinear Lines with Amontons-Coulomb's Type Friction and Different Rough Contact Surface Realizations, **Invited lecture** for Minisymposium **ESMC MS-10 "Dynamics of the Solids Systems with Friction"**, Program of 8th European Solid Mechanics Conference in Graz, Austria during July 9 - 13, 2012. ESMC Graz 2012, 9-13 July , 2012, MS-10.2, p. 62 (<http://www.esmc2012.tugraz.at/>.)

28\* Hedrih (Stevanović) K., (2012), Free Nonlinear Dynamics of a Heavy Mass Particle along Rotating Rough urvilinear Lines with Amontons-Coulomb's Type Friction and Different Rough Contact Surface Realizations, **Invited lecture** for Minisymposium **ESMC MS-10 "Dynamics of the Solids Systems with Friction"**, Two pages paper in CD Proceedings of 8th European Solid Mechanics Conference in Graz, Austria during July 9 - 13, 2012. ESMC Graz 2012, 9-13 July , 2012, MS-10.2, Paper 7. pp. MS-10.2, p7: 1-2. (<http://www.esmc2012.tugraz.at/>.)

**Predsedavajući sesijom Minisimpozijuma MS-10.2 "Dynamics of the Solids Systems with Friction", of 8th European Solid Mechanics Conference in Graz, Austria during July 9 - 13, 2012. ESMC Graz 2012, 9-13 July , 2012, MS-10.2,**

29\* Hedrih (Stevanović) K. and **Stamenković Matija**, (2012), Deformable Body Oscillations on Layer with Visco-Elastic and Inertia Properties, Program of 8th European Solid Mechanics Conference in Graz, Austria during July 9 - 13, 2012., ESMC Graz 2012, 9-13 July , 2012, PS, p. 159. (<http://www.esmc2012.tugraz.at/>)

30\* Hedrih (Stevanović) K. and **Stamenković Matija**, (2012), Deformable Body Oscillations on Layer with Visco-Elastic and Inertia Properties, Two pages paper in CD Proceedings of 8th European Solid Mechanics Conference in Graz, Austria during July 9 - 13, 2012., ESMC Graz 2012, 9-13 July , 2012, PS, Paper 5 (<http://www.esmc2012.tugraz.at/>)

31\* Hedrih (Stevanović) K., (2012), **DICTIONARY OF THE BASIC TERMS, METHODS AND PHENOMENA OF NONLINEAR DYNAMICS, Plenty Lecture**, Proceedings of 11<sup>th</sup> International Conference of Fundamental and Applied Aspects of Physical Shemistry, **PHYSICAL CHEMISTRY 2012**, Belgrade. 24-28 September 2012, Vol. I, pp. 13-33. <http://www.socphyschemserb.org/>  
ISBN 978-86-82475-2-79

Član Naučnog odbora The 11<sup>th</sup> International Conference of Fundamental and Applied Aspects of Physical Chemistry, PHYSICAL CHEMISTRY 2012, Belgrade. 24-28 September 2012. <http://www.socphyschemserb.org/>

32\* Hedrih (Stevanović) K., (2012), Angular velocities and accelerations of the basic vectors of a kinetic position vector tangent space in different curvilinear coordinate systems, 30 minutes lecture, Book of Abstracts of XVII Geometrical Seminar, Zlatibor September 3-8, 2012, p. 76. ISBN 978-86-7589-86-7

<http://poincare.matf.bg.ac.rs/%7Egeometricalseminar/>

33\* Hedrih (Stevanović) K., (2012), Тригер спрегнутих сингуларитета, Програм за први дан, са апстрактима научног скупа **Математика и примене**, Београд, 25. и 26. мај 2012, национални скуп са међународним учешћем, у организацији Математичког факултета Универзитета у Београду.

<http://www.matf.bg.ac.rs/lat/skupovi-u-zemlji/>

34\* Хедрих (Стевановић К., (2012), Михаило Петровић и фасцинантна нелинеарна динамика, 30-минутно предавање по позиву, **МАЈМЕСЕЦМАТЕМАТИКЕ - СРПСКИ МАТЕМАТИЧАРИ**, у организацији Ректората Универзитета у Београду и Српска академија наука и уметности, Ректорат Универзитета у Београду, Студентски трг 1, Свечана сала, 28. мај 2012.

### III\*

## Serbian Scientific Society

### Symposium Nonlinear Dynamics – Milutin Milanković

<http://afrodita.rcub.bg.ac.rs/~nds/indexe.html>

Multidisciplinary and Interdisciplinary Applications

(SNDMIA 2012), Belgrade, October 1-5, 2012.

(Eighth Serbian Symposium in area of Non-linear Sciences)

supported by Project ON174001 (2011-2014)

coordinated through

Department of Mechanics at Mathematical Institute SANU

### Co-organizers scientists from

Serbian Society of Mechanics,  
Institute „Mihajilo Pupin“ Belgrade,  
Institute „Vinča“,  
The Society of Physical Chemists of Serbia

Faculty of Physical Chemistry University of Belgrade and  
Faculty of Technical Sciences Kosovska Mitrovica, University of Pristina with allocated  
place in Kosovska Mitrovica.

У оквиру овог скупа одржала сам једну беседу на отварању, као један од два  
главна организатора, једни пленарно предавање и јесно саопштење. Бесда је најављена  
под називом:

*Address to Participant of Symposium: Hedrih (Stevanović) K. SYMPOSIUMS ON NONLINEAR  
MECHANICS IN SERBIA, ICNO AND ENOC*

док је пленарно предавање одежано у следећем термину:

**October 5, 2012 at 12,00h-12,40h, Plenary Lecture**

**Chairs:** H. Yabuno, Pavel Krasilnikov and Marina V. Shitikova

**PL-13. ID-81. PHENOMENOLOGICAL MAPPING AND MATHEMATICAL ANALOGY IN  
NONLINEAR DYNAMICAL SYSTEMS, K. (Stevanović) Hedrih<sup>1,1</sup>** Mathematical Institute SANU,  
Department of Mechanics, and Faculty of Mechanical Engineering University of Niš, Serbia,

Прво једноауторско саопштење сам представила самаЧ

**October 4, 2012 at 13,40h-15,00h, Contributed Lectures**

**CL-36. ID-80. STOCHASTIC PARAMETRICALLY EXCITED HEREDITARY SANDWICH  
MULTI BEAM DYNAMICAL SYSTEMS, K. (Stevanović) Hedrih<sup>1</sup>** Mathematical Institute SANU,  
Department of Mechanics, and Faculty of Mechanical Engineering University of Niš, Serbia.

Док је коауторско саопштење под називом:

**CL-37. ID-79. HYBRID SYSTEM DYNAMICS ON LAYER WITH NONLINEAR ELASTIC AND  
INERTIA PROPERTIES, K. (Stevanović) Hedrih<sup>1</sup>, M. Stamenković<sup>2</sup>, N. Nešić<sup>2, 1</sup>** Mathematical Institute  
SANU, Department of Mechanics, and Faculty of Mechanical Engineering University of Niš, Serbia,<sup>2</sup> Mathematical  
Institute SANU, Department of Mechanics, Kneza Mihaila 36/III, Serbia,

успешно саопштла деуги коаутор **Марија Stamenković.**

Двостранични апстрактни радова су публиковани у публикацији Симпозијума и преглед са  
одговарајућим библиографским подацима је дат у следећем приказу истих:

Hedrih (Stevanović) K., (2012), PHENOMENOLOGICAL MAPPING AND  
MATHEMATICAL ANALOGY IN NONLINEAR DYNAMICAL SYSTEMS, **Plenary Lecture**,  
Booklet of Abstracts of Symposium Nonlinear Dynamics – Milutin Milanković, Multidisciplinary and  
Interdisciplinary Applications (SNDMIA 2012), Belgrade, October 1-5, 2012. (Eighth Serbian Symposium  
in area of Non-linear Sciences), Editors: Katica R. (Stevanović) HEDRIH andf Žarko Mijajlović, Serbian  
Scientific Society, 2012, pp. 38-39. (<http://afrodita.rcub.bg.ac.rs/~nds/indexe.html>)

*Hedrih (Stevanović) K. SYMPOSIUMS ON NONLINEAR MECHANICS IN SERBIA, ICNO  
AND ENOC, Address to Participant of Symposium, Booklet of Abstracts of Symposium Nonlinear  
Dynamics – Milutin Milanković, Multidisciplinary and Interdisciplinary Applications (SNDMIA 2012),  
Belgrade, October 1-5, 2012. (Eighth Serbian Symposium in area of Non-linear Sciences), Editors:  
Katica R. (Stevanović) HEDRIH andf Žarko Mijajlović, Serbian Scientific Society, 2012, pp. 172-178.  
(<http://afrodita.rcub.bg.ac.rs/~nds/indexe.html>)*

Hedrih (Stevanović) K., (2012), **STOCHASTIC PARAMETRICALLY EXCITED HEREDITARY  
SANDWICH MULTI BEAM DYNAMICAL SYSTEMS**, Contributed Lecture, Booklet of Abstracts of  
Symposium Nonlinear Dynamics – Milutin Milanković, Multidisciplinary and Interdisciplinary  
Applications (SNDMIA 2012), Belgrade, October 1-5, 2012. (Eighth Serbian Symposium in area of Non-  
linear Sciences), Editors: Katica R. (Stevanović) HEDRIH andf Žarko Mijajlović, Serbian Scientific  
Society, 2012, pp. 137-138..

(<http://afrodita.rcub.bg.ac.rs/~nds/indexe.html>)

K. (Stevanović) Hedrih, M. Stamenković, N. Nešić (2012), HYBRID SYSTEM DYNAMICS ON LAYER WITH NONLINEAR ELASTIC AND INERTIA PROPERTIES, Contributed Lecture, Booklet of Abstracts of Symposium Nonlinear Dynamics – Milutin Milanković, Multidisciplinary and Interdisciplinary Applications (SNDMIA 2012), Belgrade, October 1-5, 2012. (Eighth Serbian Symposium in area of Non-linear Sciences), Editors: Katica R. (Stevanović) HEDRIH and Žarko Mijajlović, Serbian Scientific Society, 2012, pp. 139-140. (<http://afrodita.rcub.bg.ac.rs/~nds/indexe.html>)

Била сам модератор Округлог стола на тему Етика научника, који се одржао веома успешно по оцени и домаћих и иностраних учесника.

**October 4, 2012 at 13,00h-13,40h, Round Table**

**Invitation for Chairs and Contribution Discussions:** Albert Luo, Hiroshi Yabuno, Pavel Krasilnikov, Mihai Zavrlevski, Marina V. Shitikova, Ljiljana Kolar Anić, Slobodan Anić, Ilija Čupić, Žarko Mijajlović, K. (Stevanović) Hedrih I drugi.

**Round Table: "Ethic of Scientists and Evaluation of Scientific Research Results".**

\* **Kratak opis realizacije naučnog programa Simpozijuma** (u prilogu realizovani naučni program Simpozijuma)

Naučni program Simpozijuma Nonlinear Dynamics – Milutin Milanković je uspešno realizovan u toku od svih pet dana počevši od 1 oktobra (od 8,30h do 19h svakog dana) i zaključno sa programom 5 oktobra 2012, koji se završio sa programom zatvaranja i naučnom diskusijom prisutnih učesnika. Mesto održavanja velika sala Matematičkog instituta SANU.

Održano je 11 plenarnih predavanja iz različitih oblasti nelinearne dinamike i jedno specijalno o kulturnoj baštini Srbije. Sedam plenarnih predavača je bilo iz inostranstva (po jedan iz Japana, U.S.A., dva iz Rusije, Izraela, Nemačke, Litvanije). Održan je uspešno Okrugli sto o Etici naučnika i jedna panel diskusija o Nelinearnoj dinamici na zatvaranju Simpozijuma. Održane su tri specijalne sekcije iz oblasti nelinearne dinamike iz Fizike, Fizičke hemije i Dinamike mehanickih sistema, kao i 11 predavanja po pozivu iz oblasti nelinearne dinamike bio sistema, mehanike fluida, analitičke mehanike i dr. Saopštenja su takodje održavana po programu. Autori 88 dvostranicnih apstrakta radova, koji su uključeni u Booklet of Abstracts su iz Srbije, Rusije, Japana, U.S.A., Izraela, Nemačke, Litvanije, Ukrajine, Kine, Španije, Indije, Kine, Katara.

Opšta ocena učesnika je da je Simpozijum izuzetno uspešno realizovan. Učesnici su se izuzetno povoljno izjasnili o visokom naučnom nivou realizovanog naučnog programa simpozijuma, a posebno o naučnoj atmosferi stvorenoj diskusijama i naučnim komunikacijama među učesnicima po održanim plenarnim predavanjima, predavanjima po pozivu, kao i saopštenjima. Ocena je da je Okrugli sto pravi izbor i sadržajno veoma uspešno realizovan.

Ocena je da bi trebalo nastaviti sa organizacijom i narednih Simpozijuma iz ovog ciklusa Nonlinear Dynamics interdisciplinarnog i multidisciplinarnog sadržaja i sa učesnicima po pozivu iz inostranstva. Konceptija naučnog programa je takodje uspešno osmišljena i uspešno realizovana.

Publikovan je Booklet of Abstracts – Symposium **Nonlinear Dynamics – Milutin Milanković** koji sadrži dvostranicne apstakte plenarnih predavanja, predavanja po pozivu i saopštenja., ukupno 88 apstrakata i priloge. Publikacija je katalogizirana i CIOP Narodne biblioteke Srbije i nasi sledeće identifikacione brojeve:

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Department of Mechanics, and Faculty of Mechanical Engineering University of Niš, Serbia,

Booklet of Abstracts - **Symposium Nonlinear Dynamics – Milutin Milanković**, Multidisciplinary and Interdisciplinary Applications, (SNDMIA 2012), Belgrade, October 1-5, 2012., (Eigth Serbian Symposium in area of Non-linear Sciences), Serbian Scientific Society. Str. 38-39.

<http://afrodita.rcub.bg.ac.rs/~nds/indexe.html>, ISBN 978-86-7746-344-1, COBISS.SR – ID

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978-86-7746-344-1:

[http://www.mi.sanu.ac.rs/projects/booklet\\_of\\_abstracts.pdf](http://www.mi.sanu.ac.rs/projects/booklet_of_abstracts.pdf)

First Editor in Chief of Booklet of Abstracts - **Symposium Nonlinear Dynamics – Milutin Milanković**, Multidisciplinary and Interdisciplinary Applications, (SNDMIA 2012), Belgrade, October 1-5, 2012., (Eigth Serbian Symposium in area of Non-linear Sciences), Serbian Scientific Society. Str. 1-193.

<http://afrodita.rcub.bg.ac.rs/~nds/indexe.html>, ISBN 978-86-7746-344-1, COBISS.SR – ID

193221132, Barcod 978-86-7746-344-1: [http://www.mi.sanu.ac.rs/projects/booklet\\_of\\_abstracts.pdf](http://www.mi.sanu.ac.rs/projects/booklet_of_abstracts.pdf)

**Циклус предавања Одељења природно-математичких наука Научног друштва Србије**

**НАУЧНИ ХОРИЗОНТИ  
ПРИРОДНОМАТЕМАТИЧКЕ НАУКЕ - ЈУЧЕ, ДАНАС И СУТРА**

Предацање под насловом: Хедрих (Стевановић) К., (2012), О ТАНГЕНТНИМ ПРОСТОРИМА ВЕКТОРА ПОЛОЖАЈА МАТЕРИЈАЛНИХ ТАЧАКА РЕОНОМНОГ СИСТЕМА И ЊИХОВИМ КИНЕТИЧКИМ ДЕФОРМАЦИЈАМА, предавање, **НАУЧНИ ХОРИЗОНТИ - ПРИРОДНОМАТЕМАТИЧКЕ НАУКЕ - ЈУЧЕ, ДАНАС И СУТРА**, Циклус предавања Одељења природно-математичких наука Научног друштва Србије, Понедељак, 30. април 2012. године. <http://afrodita.rcub.bg.ac.rs/~nds/indexe.html>

**Семинари Математичког интитута САНУ**



## Семинар механике Одељења за механику Математичког института САНУ

<http://www.mi.sanu.ac.rs/seminars/seminar12.htm>  
<http://www.mi.sanu.ac.rs/colloquiums/mechcoll.htm>

### **SREDA, 11. april 2012. u 18 sati:**

*Проф. др Катица Р. (Стевановић) Хедрих*, руководилац пројекта ОИ 174001 и управник Одељења за механику

**Предацање под насловом:** Хедрих (Стевановић) К., (2012), Вектори момената маса, вектори ротатори и њихова примена на системе више спрегнутих тела који изводе спрегнуте ротације, предавање, „Семинар механике Одељења за механику Математичког института САНУ, среда 11 април 2012 у 18 часва (замена предавања због одсутности предавача, који није најавио спреченост да одржи предавање, види Записник Семинара механике Одељења за механику) .

<http://www.mi.sanu.ac.rs/colloquiums/mechcoll.htm>

Предавање одржано на основу садржаја и резултата из публикованих радова:

Hedrih (Stevanović K., (2012), Mass moment vectors and vector rotators and their applications to the rigid body multi-coupled rotations, (realized as Plenary Lecture, Certificate), Selected papers, CCMECH-7, 7<sup>th</sup> INTERNATIONAL SYMPOSIUM ON CLASSICAL AND CELESTIAL MECHANICS (CCMECH'2011), October 23 – 28, 2011, Edited by Leszek Gadamski, Pavel Krasilnikov and Alexander Prokopenya. The Russian Academy of Sciences, A. A. Dorodnicyn Computing Centre of RAS, Moscow State University, Moscow State Aviation Institute, and Collegium Mazovia in Siedlce (Poland), pp. 44-62. ISBN 978-83-63169-20-6.

Hedrih (Stevanović) Katica, (2012 ili 13), Vector method based on mass moment vectors and vector rotators applied to rigid-body multi-coupled rotations around no intersecting axes, invited and accepted by guset Editor Jan Awrejcevicz and submitted for possible publishing in special Issue of International Journal of Structural Stability and Dynamic, ( wait Editorial drcision of Editor in Chief of Journals). ISSN 0219-4554

### **Sreda, 09. maj 2012. u 18 sati:**

*Проф. др Катица Р. (Стевановић) Хедрих*, Математички институт САНУ Београд и  
Машињски факултет Универзитета у Нишу (Пројекат ОИ174001)

Предацање под насловом: Хедрих (Стевановић) К., (2012), Линеаризације и апроксимације са применама у механици: Методе, претпоставке, прве аналитичке апроксимације и грешке (Linearizations and approximations with applications in mechanics: Methods, assumptions, first analytic approximations and errors), предавање, Семинар механике Одељења за механику Математичког института САНУ, среда 9 маја 2012 у 18 часва (замена предавања због одсутности предавача, који је најавио спреченост да одржи предавање, види Записник Семинара механике Одељења за механику) .

<http://www.mi.sanu.ac.rs/colloquiums/mechcoll.htm>

## Семинари Математичког института САНУ Семинар за филозофију и историју математике, механике и астрономје

<http://www.mi.sanu.ac.rs/seminars/seminar12.htm>

**UTORAK, 22. maj 2012. u 12:15 sati**

***Prof. Dr Katica R. (Stevanović) Hedrih, matematički institut SANU, Beograd***  
**FASCINANTNA NELINEARNA DINAMIKA TEŠKE MATERIJALNE TAČKE;  
APSTRAKCIJA REALNIH SISTEMA I OŽIVLJAVANJE MATEMATIKE**

**Предацање под насловом:** Хедрих (Стевановић) К., (2012), FASCINANTNA NELINEARNA DINAMIKA TEŠKE MATERIJALNE TAČKE; APSTRAKCIJA REALNIH SISTEMA I OŽIVLJAVANJE MATEMATIKE, предавање, Семинар за филозофију и историју математике, механике и астрономје, Математичког института САНУ, уторак, 22 мај 2012 у 12 часва.  
<http://www.mi.sanu.ac.rs/seminars/programs/seminar12.maj2012.htm>

Predavanje povodom 15 godina članstva u akademiji nauka visokih škola i univerziteta ukrajine (od 1996)

Rezime: Predavanjem se prikazuju fenomeni fascinantne nelinearne dinamike teške materijalne tačke koja se kreše po rotirajućoj krivoj liniji - krugu (paraboli, cikloidi, elipsi). Zavisno od međusobnog položaja mimoilaznih osa oko kojih se izvode spregnute rotacije prikazuju se nelinearne diferencijalne jednačine i odgovarajući fazni portreti. Kroz analizu svojstava i značenja stacionarnih tačaka i trigera spregnutih singulariteta, kao i bifurkacija stacionarnih tačaka varijacijom parametara sistema prikazuje se oživljavanje matematičkih metoda i diferencijalnih jednačina do tzv. "žive matematike".

Fenomenološkim preslikavanjem i matematičkom analogijom, po ugledu na ideje Mihajla Petrovića, pokazuje se da nekoliko nelinearnih diferencijalnih jednačina, kojima se opisuje fascinantna nelinearna dinamika teške materijalne tačke, predstavljaju matematičku apstrakciju opisa dinamike rotora sa spregnutim debalansima, žirorotora, ili krutih tela koja izvode spregnute rotacije. ukazuje se na pojam konzervativnog i nekonzervativnog sistema i sistema sa trenjem njihovih zajedničkih trigera spregnutih singulariteta. Za sisteme sa trenjem ukazuje se na bifurkaciju singulariteta iz trigera spregnutih singulariteta i pojavu jednostranih singulariteta.

**UTORAK, 23. oktobar 2012. u 12:15 sati**

***Katica R. (Stevanovic) Hedrih, Matematički institut SANU, Beograd***  
**JUBILEJ "OPŠTE TEORIJE STABILNOSTI" A. M. LJAPUNOVA**

**Предацање под насловом:** Хедрих (Стевановић) К., (2012), JUBILEJ "OPŠTE TEORIJE STABILNOSTI" A. M. LJAPUNOVA, предавање, Семинар за филозофију и историју математике, механике и астрономје, Математичког института САНУ, уторак, 23 октобра 2012 у 12 часва.  
<http://www.mi.sanu.ac.rs/seminars/programs/seminar12.oct2012.htm>

Rezime: Proteklo je 120 godina od prvog objavljivanja, 1892. godine, "Opšte teorije stabilnosti" Aleksandra Mihailovi Ljapunova (6. jun 1857 - 3. novembar 1918). Povodom tog jubileja predavanje je usmeren. na osnovne postavke "Opšte teorije stabilnosti" Ljapunova, osnovne pojmove i njihove definicije, kao i na njihovu interdisciplinarnu i multidisciplinarnu primenu, u skoro svim oblastima nauka, a posebno u razvoju oblasti nelinearne dinamike. Za mnogobrojne ključne reci, kao to su

Ljapunovljeva stabilnost, Ljapunovljeve funkcije prvog i drugog reda, Ljapunovljev funkcional, Ljapunovljev eksponent, Ljapunovljeva centrala granicna teorema, Ljapunovljeva jednačina, Ljapunovljev fraktal, Ljapunovljevo vreme i Ljapunov-Malkinova teorema, biti prikazane osnovne definicije i primene i biti ukazano na njihov značaj u savremenim naučnim istraživanjima u raznim oblastima nauka.

## Семинари Математичког института САНУ

### Семинар Математичке методе механике

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Предавање под насловом: Хедрих (Стевановић) К., (2012), О ТАНГЕНТНИМ ПРОСТОРИМА ВЕКТОРА ПОЛОЖАЈА МАТЕРИЈАЛНИХ ТАЧАКА РЕОНОМНОГ СИСТЕМА И ЊИХОВИМ КИНЕТИЧКИМ ДЕФОРМАЦИЈАМА, предавање, Семинар Математичке методе механике, Математички институт САНУ, Понедељак, 30. април 2012. године.  
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Mathematical Methods of Mechanics and Applications and Project OI 174001

Matematicke metode mehanike u primeni

Projekat OI 174001 Dinamika hibridnih sistema slozenih struktura (2011-2014)

Seriya predavanja za istrazivace pripravnike i doktorante iz oblasti Kinetike, Elastodinamike, Analiticke mehanike, Primene tenzorskog racuna u mehanici, Teorije oscilacija i Nelinearne dinamike

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**Katica (Stevanovic) Hedrih**

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VECTOR METHOD BASED ON MASS MOMENT VECTORS  
AND VECTOR ROTATORS APPLIED TO RIGID-BODY  
MULTI-COUPLED ROTATIONS AROUND NON  
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- III. Finite -Time Stability of Fractional Time Delay System 37
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- V. Modeling of Human Skin Using Distributed Order Fractional Derivative Model-Frequency Domain 79
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Interdisciplinary and multidisciplinary sciences  
4th -7th of June 2013, Hotel BREZA- Vrnjačka Banja, Serbia  
Organizer: Katica R. (Stevanovic) Hedrih  
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**Plenary Lectures and Semi-Plenary Lectures and Invited Participant.**

\* 8th INTERNATIONAL SYMPOSIUM ON CLASSICAL AND CELESTIAL MECHANICS (CCMECH'8), September 25 – 29, 2013, Siedlce, Poland, ( The Russian Academy of Sciences, A. A. Dorodnicyn Computing Centre of RAS, Moscow State University, Moscow State Aviation Institute, Warsaw University of Life Sciences, and Collegium Mazovia in Siedlce (Poland) will hold the Eighth International Symposium on Classical and Celestial Mechanics (CCMECH'2013) at Collegium Mazovia in Siedlce, Poland).

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\* THE 13TH INTERNATIONAL CONFERENCE OF TENSOR SOCIETY ON DIFFERENTIAL GEOMETRY AND ITS APPLICATIONS, AND INFORMATICS BESIDES., *The 86th Anniversary of Radu MIRON'S Birth*. September 3rd (Tuesday) to September 7th (Saturday) in 2013. Faculty of Mathematics, Alexandru Ioan Cuza University and Mathematical Institute "O.Mayer" in Iași Romania And Tensor Society, Japan,

<http://www.math.uaic.ro/~tensorconference2013/>

Hedrih (Stevanović) K., (2013), Generalized function of fractional order dissipation of system energy and extended Lagrange differential equation in matrix form, *Dedicated to 86th Anniversary of Radu MIRON'S Birth. 30 minutes* Plenary Lecture, Abstracts of THE 13TH INTERNATIONAL CONFERENCE OF TENSOR SOCIETY ON DIFFERENTIAL GEOMETRY AND ITS APPLICATIONS, AND INFORMATICS BESIDES., *The 86th Anniversary of Radu MIRON'S Birth*. September 3rd (Tuesday) to September 7th (Saturday) in 2013. Faculty of Mathematics, Alexandru Ioan Cuza University and Mathematical Institute "O.Mayer" in Iași Romania And Tensor Society, Japan, 2013, p.3. (paper submitted for publishing in the journal Tensor of Tensor Society, Japan.)

**Chairman of the sessions or Plenary Lectures at Scientific meetings in 2013.**

#### **Chairman of the Plenary Lectures**

\* 8th INTERNATIONAL SYMPOSIUM ON CLASSICAL AND CELESTIAL MECHANICS (CCMECH'8), September 25 – 29, 2013, Siedlce, Poland, ( The Russian Academy of Sciences, A. A. Dorodnicyn Computing Centre of RAS, Moscow State University, Moscow State Aviation Institute, Warsaw University of Life Sciences, and Collegium Mazovia in Siedlce (Poland) will hold the Eighth International Symposium on Classical and Celestial Mechanics (CCMECH'2013) at Collegium Mazovia in Siedlce, Poland).

<http://agora.guru.ru/display.php?conf=CCMECH7>, <http://www.msz.gov.pl/en>

\* **Fourth Serbian Congress of Theoretical and Applied Mechanics**

(<http://www.ssm.org.rs/Congress2013/authors.html>)

\* THE 13TH INTERNATIONAL CONFERENCE OF TENSOR SOCIETY ON DIFFERENTIAL GEOMETRY AND ITS APPLICATIONS, AND INFORMATICS BESIDES., *The 86th Anniversary of Radu MIRON'S Birth*. September 3rd (Tuesday) to September 7th (Saturday) in 2013. Faculty of Mathematics, Alexandru Ioan Cuza University and Mathematical Institute "O.Mayer" in Iași Romania And Tensor Society, Japan,  
<http://www.math.uaic.ro/~tensorconference2013/>

**Cairman of the Sessions**

\* **4th International Conference on Nonlinear Dynamics**, Sevastopol, Ukraine, 19-22 June, 2013, [http://kpispu.org.ua/en/ND2013\\_conference](http://kpispu.org.ua/en/ND2013_conference)

\* 12TH CONFERENCE on DYNAMICAL SYSTEMS THEORY AND APPLICATIONS, December 2-5, 2013. Łódź, Poland.

\* **Mini Symposium Nonlinear Dynamics – Milutin Milankovic**

Interdisciplinary and multidisciplinary sciences  
4th -7th of June 2013, Hotel BREZA- Vrnjačka Banja, Serbia  
Organizer: Katica R. (Stevanovic) Hedrih

**Uredjivanje naucnih publikacija u 2013**

SERBIAN SCIENTIFIC SOCIETY

<HTTP://AFRODITA.RCUB.BG.AC.RS/~NDS/>

<HTTP://AFRODITA.RCUB.BG.AC.RS/~NDS/INDEXE.HTML>

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YU ISSN 0350-2910

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Special Issue **Nonlinear Dynamics S2 (2013)**

Dedicated to **Milutin Milanković (1879- 1958)**

*Guest Editors:*

*Katica R. (Stevanović) Hedrih and Žarko Mijajlović*

**Clan redakcija naucnih casopisa:**

\* **Mathematical Problem in Engineering**, Hindawi Publishing Corp

ISSN 1024-123x

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Editorial Board

<http://www.hindawi.com/journals/mpe/editors.html>

Associate Editor (2004-)

\* **Scientific Technical Review Vojske Srbije**

YU ISSN 1820-0206

<http://www.vti.mod.gov.rs/ntp/index.htm>

\* **TENSOR**, ISSN 0040-3604, Tensor Society (Tokyo).

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### Clan Akademija i naucnih drustava

\* Clan Naucnog drustva Srbije (2008)

<http://afrodita.rcub.bg.ac.rs/~nds/>

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Akademik Akademije nauka visokih skola I univerziteta Ukrajine (od 1996)

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\* Calan **GAMM (1962)**

Gesellschaft für Angewandte Mathematik und Mechanik

<https://www.gamm-ev.de/>

\* Int. ASME (American Society of Mechanical Engineers (od 2000)).

<https://my.asme.org/>

\* Clan Srpskog drustva za mehaniku

<http://www.ssm.org.rs/>

### Recenzije

**Nonlinear Dynamics**

**Non-Linear Mechanics,**

**Mathematica Problem in Engineering**

**Communication in Nnlinear Science and Numerical Simulations**

**Iranian Journal of Science and Technology**

**i drugi....**

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Matematički institut SANU

Odeljenje za mehaniku

PLAN RADA ZA OKTOBAR 2013.

Sreda 9.10.2013. 18 casova, sala 301f

Katica R. (Stevanovic) Hedrih, Matematički institut SANU Beograd i Masinski  
fakultet Univerziteta u Nisu

DISCRETE FRACTIONAL ORDER SYSTEM DYNAMICS



**Abstract:** A theory of free vibrations of discrete fractional order system with finite number of degrees of freedom is founded in matrix form. Fractional order system with finite number of degrees of freedom is defined by three matrices: matrix of mass inertia coefficients, matrix of system rigidity coefficients, matrix of the fractional order properties elements. By using matrix method a mathematical description of fractional order discrete system free vibrations is determined in form of coupled fractional order differential equations. Corresponding solutions in analytical form for special case of the matrix of fractional order properties elements are determined in forms of polynomial series along time. For that case eigen characteristic numbers and corresponding system of eigen main coordinates as well as independent eigen fractional order modes are determined. Some graphical illustrations of these eigen main fractional order modes are presented on the basis of numerical data. A function of viscoelastic creep fractional order dissipation of system energy and generalized forces of system with no ideal viscoelastic creep fractional order dissipation of system energy for generalized coordinates are introduced and defined. Extended Lagrange differential equations second order for fractional order system dynamics in matrix form are introduced. A theorem is formulated. By use presented matrix method, as special cases of the fractional order chain system are considered. Also, for a fractional order double DNA helix chain, the two corresponding main eigen chains as well as eigen modes are presented.

Математички институт САНУ

**Seminar za istoriju i filozofiju matematike, mehanike i astronomije**

УТОРАК, 8. октобар 2013. у 12:15 сати

Проф. Др Катица (Стевановић) Хедрих, Математички институт САНУ

**ЗАКОНИ, ПРИНЦИПИ И ТЕОРЕМЕ ДИНАМИКЕ. ФИЗИЧКИ И МАТЕМАТИЧКИ ОСНОВИ**

Резиме: Приказују се основни закони, принципи и теореме динамике. указује се на физичке и математичке основе једначина динамике. Приказује се извођење Lagrange-ових једначина друге врсте различитим принципима и даје уопштење истих за различите механичке системе. Анализира се математички формализам који се често јавља, а нема утемељење у реалним механичким системима. Дају се примери извођења једначина осцилација деформабилних тела варијационим принципом и принципом динамичке

УТОРАК, 5. новембар 2013. у 12:15 сати

Prof. Dr Katica (Stevanović) Hedrih, Matematički institut SANU

## BESEDA O MIHAILU PETROVIĆU, ELEMENTIMA MATEMATIČKE FENOMENOLOGIJE I NELINEARNOJ DINAMICI

Rezime: U ovom radu se predstavlja sadržaj besede o Mihailu Petroviću i nelinearnoj dinamici, održane na Univerzitetu u Beogradu u okviru "Majskih dana matematike" pod nazivom "Srpski matematičari", a u organizaciji Rektorata Univerziteta u Beogradu i Srpske akademije nauka i umetnosti. Ključna ideja predavanja je da se prikažu ideje Mihaila Petrovića u savremenoj nauci, usmeravajući pažnju na njegovo, po oceni Milutina Milankovića, najznačajnije delo "Matematička fenomenologija", kao i njen značaj i vidljivost kroz savremene naučne tokove sadržane u rezultatima otkrića kompleksnih fenomena nelinearne dinamike. Takođe, u sadržaju besede se našao i prikaz materijalizacije njegovih ideja i matematičkog znanja kroz patente koje nam je ostavio u nasleđe. Slavljen od matematičara, promovisani su samo njegovi rezultati iz matematike, a nepravедno zapostavljeni njegovi rezultati primene i multidisciplinarnosti. U ovoj besedi, načinjen je još jedan pokušaj da se savremenicima i mladim generacijama obrati pažnja i na Mihajla Petrovića, fizičara, inženjera inovatora i praktičara, a pre svega vizionara integracije naučnih saznanja iz različitih naučnih oblasti redukcijom broja modela dinamika. Ideje o fenomenološkom preslikavanju su svakako najznačajnije. I danas se nalaze u savremenim naučnim istraživanjima, a po mišljenju predavača imaju isti značaj za dalji razvoj i integraciju različitih naučnih znanja, samerljiv sa značajem koju ima teorija stabilnosti Ljapunova..

### informacija iz 2013

Вестник научно-технического развития  
[www.vntr.ru](http://www.vntr.ru)

№ 9 (25), 2009 г.

Национальная Технологическая Группа  
[www.ntgcom.com](http://www.ntgcom.com)

#### VECTOR METHOD: KINETIC PARAMETERS ANALYSIS AND IMPACTS TO BEARINGS OF THE COUPLED ROTOR DYNAMICS *dedicated in memory of Academician Konstantin Vasiljevich Frolov (1932-2007)*

**Katica R. (Stevanovic) HEDRIH**

*Faculty of Mechanical Engineering University of Niš Mathematical Institute SANU  
Serbia, Niš*

Katica R. (Stevanovic) HEDRIH, VECTOR METHOD: KINETIC PARAMETERS ANALYSIS AND IMPACTS TO BEARINGS OF THE COUPLED ROTOR DYNAMICS. *dedicated in memory of Academician Konstantin Vasiljevich Frolov (1932-2007)*, Вестник научно-технического развития, Национальная Технологическая Группа, № 9 (25), 2009 г. pp. 42 -59. [www.vntr.ru](http://www.vntr.ru) , [www.ntgcom.com](http://www.ntgcom.com), [www.vntr.ru](http://www.vntr.ru) [www.ntgcom.com](http://www.ntgcom.com)

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**Katica (Stevanovic) Hedrih**

**Rukovodilac projekta ON174001 (period 2011-2014 godina) MPN RS koordiniranog u MI SANU po članu 24 AKT-a Ministarstva prosvete, nauke I tehnoloskog razvoja Republike Srbije**

(u zvanju redovni profesor Masinskog fakulteta Univerziteta u Nisu, sa 44 gorine radnog staza, ostvarenog na Masinskom fakultetu u Nisu (1967-2009) I Matematičkom institutu SANU (2009-2011))

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Akadenik Akademije nelinearnih nauka Moskva (od 1997)

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Laureat nadržade "Arhimed" VTI VS RS za naučni rad (2007)

Laureat dve plakete Cankaya Univerziteta iz Ankare u oblasti primene izvoda necelog reda (2008) I oblasti nelinearne dinamike (2010)

Mentor većeg beođa unikatnih diplomskih radova iz oblasti mehanike, većeg beođa mgistarskih I većeg beođa doktorskih disertacija uspesno odbranijenih!

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**Prof. dr Katica R. (Stevanović) Hedrih,**

**Doctor of Technical Sciences**

Scientific Research Professor - Full Professor of University

Project Leader OI174001 (2011-2014)

Department of Mechanics

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<http://www.masfak.ni.ac.rs/sitegenius/topic.php?id=409>

Hedrih (Stevanović) K., Simonović J., (2010), “*Models of Hybrid Multi-Plates Systems Dynamics*”, The International Conference-Mechanical Engineering in XXI Century, Niš, Serbia, 25-26 September 2010, Proceedings, pp.17-20.

Hedrih (Stevanović) K., (2012), Triger sparegnutih singulariteta, Abstract plenarnog predavanja, Zbornik radova, III Simpozijum Matematika I primene 25 I 26 maj 2012, Matematički fakultet Univerziteta u Beogradu, str. 179

### informacija iz 2013

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[www.vntr.ru](http://www.vntr.ru)

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Katica R. (Stevanovic) HEDRIH, VECTOR METHOD: KINETIC PARAMETERS ANALYSIS AND IMPACTS TO BEARINGS OF THE COUPLED ROTOR DYNAMICS. *dedicated in memory of Academician Konstantin Vasiljevich Frolov (1932-2007)*, Вестник научно-технического развития, Национальная Технологическая Группа, № 9 (25), 2009 г. pp. 42 -59. [www.vntr.ru](http://www.vntr.ru) , [www.ntgcom.com](http://www.ntgcom.com), [www.vntr.ru](http://www.vntr.ru) [www.ntgcom.com](http://www.ntgcom.com)

### Pripremljeni radovi za stampu na recenziji:

Katica (Stevanović) R Hedrih, Andjelka N Hedrih, Phenomenological mapping and dynamical absorptions in chain systems with multiply degree of freedom, Journal of Vibration and Control (under the review)

Katica R. (Stevanović) Hedrih, Ana Ivanović-Šašić, Ljiljana Kolar-Anić, Željko Čupić, Phenomenological mappings and analogy between linear/nonlinear, free/forced vibrations of two degrees of freedom system dynamics, Acta Polytechnica Hungarica (under the review)

Katica R. (Stevanović) Hedrih, Marija B. Stamenković, Vector rotator analysis in multi body multi coupled rotations about no intersecting axes (under the review)

Katica R. (Stevanović) Hedrih, J. Tenreiro Machado, (2013), Discrete fractional order system vibrations, *Preprint submitted to International Journal Non-Linear Mechanics (January 6, 2014)*

Katica R. (Stevanović) Hedrih and Andjelka Hedrih, Petrović's theory of elements of mathematical phenomenology and phenomenological mapping applied to system nonlinear dynamics, ENOC 2014

Katica R. (Stevanović) Hedrih, Julijana Simonović, Ana Ivanović-Šašić, Ljiljana Kolar-Anić, Željko Čupić and Andjelka Hedrih, Elements of mathematical phenomenology and qualitative /mathematical analogies on the basis of generalized Lissajous curves, ENOC 2014

Katica Hedrih, Predrag Kozić – Ratko Pavlović: O uzajamnom Uticaju harmonika u nelinearnim sistemima sa malim parametrom, Zbornik radova Matematičkog instituta, Nova Serija, knjiga 4 (13), 1984, pp.91-102,; Recueil des travaux de L'Institute Mathematique, Nouvelle Serie, tome 4 (13), 1984, pp.91-102,

## Spisak referenci u 2014 Katica (Stevanović) R. Hedrih

Katica R (Stevanović) Hedrih and Andjelka N. Hedrih, Phenomenological mapping and dynamical absorptions in chain systems with multiple degrees of freedom, Journal of Vibration and Control 1077546314525984, first published on March 19, 2014 as doi:10.1177/1077546314525984

### Pripremljeni radovi za štampu na recenziji:

Katica R. (Stevanović) Hedrih, (2014), Elements of mathematical phenomenology in dynamics of multi-body system with fractional order discrete continuum layers, Dedicated to Centennial jubilee of Russian Academician Yury N. Rabotnov, Special issue of International Journal of Mechanics, (Paper submitted in January 2014), Journal indexed in SCOPUS (<http://www.naun.org/cms.action?id=2828>). (prihvaceno za štampu).

Andjelka N. Hedrih and Katica R. (Stevanović) Hedrih, (2014), Analysis of energy state of discrete fractional order spherical net of mouse *zona pellucida* before and after fertilization, Special issue of International Journal of Mechanics, Dedicated to Centennial jubilee of Russian Academician Yury N. Rabotnov, (Paper submitted in January 2014), Journal indexed in SCOPUS (<http://www.naun.org/cms.action?id=2828>). (prihvaceno za štampu).

Katica (Stevanović) R Hedrih, Andjelka N Hedrih, Phenomenological mapping and dynamical absorptions in chain systems with multiply degree of freedom, Journal of Vibration and Control (under the review) (prihvaceno za štampu) doi:10.1177/1077546314525984

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Katica R. (Stevanović) Hedrih, Marija B. Stamenković, Vector rotator analysis in multi body multi coupled rotations about no intersecting axes (under the review)

Katica R. (Stevanović) Hedrih, J. Tenreiro Machado, (2013), Discrete fractional order system vibrations, *Preprint submitted to International Journal Non-Linear Mechanics (January 6, 2014)*

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Katica R. (Stevanović) Hedrih, Julijana Simonović, Ana Ivanović-Šašić, Ljiljana Kolar-Anić, Željko Čupić and Andjelka Hedrih, Elements of mathematical phenomenology and qualitative /mathematical analogies on the basis of generalized Lissajous curves, ENOC 2014



ZAMM · Z. angew. Math. Mech. 73 (1993) 4–5, T 153–T 156

Akademie Verlag

HEDRIH (STEVANOVIĆ), K.

## Some Vectorial Interpretations of the Kinetic Parameters of Solid Material Lines

MSC (1980): 73B20, 53A17, 53A45, 70C10, 73A05

This paper introduces the vector  $J_n^{(N)}$  of the material line mass inertia moment at the point  $N$  for the axis oriented by the unit vector  $n$ ; the vector is used for interpretation of the material line kinetic characteristics. The change of the vector of the material line mass inertia moment is determined in the transition from one space point to another when the axis remains its orientation which represents the Huygens-Steiner theorem translated for the defined material line mass inertia moment vector. Then the change of the vector of the material line mass inertia moment is defined at the given point in the case of the axis changing its orientation in the way analogous to the Cauchy equations in the elasticity theory. Then the interpretation of the main inertia directions are derived as well as of the main inertia asymmetry are defined. The relation between the axis deviation load vector by the material line mass inertia moment for the octahedron axis and the inertia asymmetry axis is analysed.

Further interpretation of the kinetic characteristics of the material line by means of the material line mass inertia moment vector and by means of the material line mass static (linear) moment vector for the axis and the point refers to the description of the motion quantity moment (angular momentum) and kinetic energy as the function of the vectors and the momentary annular velocity and the referential point velocity. Special cases of the material line rotation around the fixed axis and the fixed point are extra analysed. The deviation part of the material line mass inertia moment vector for the fixed bearings is specially analysed as well as for the rotation axis in view of the appearance of the dynamic pressure upon the bearings. The kinetic vector rotator is introduced.

The conditions for dynamic balancing by means of the static moment vector and of the deviation load vector of the rotation axis by the material line mass inertia moment are shown. This paper also introduces the notations of vectors of linear and square sector moment of material lines for pole and axis and sector pole.

### New notations

Notations of the vectors of zero, linear and square moment mass of material lines for pole and axis are pointed out in this paper as well as the notations of vectors of linear and square sector moment mass of material lines for pole and axis and sector pole:

$$M_n^{(A)} = \int_L n \, dm = Ln\sigma, \quad S_n^{(A)} = \int_L [n, \varrho] \, dm = \int_L [n, \varrho] \sigma(s, t) \, ds,$$

$$J_n^{(A)} = \iiint_V [\varrho, [n, \varrho]] \, dm = \int_L [\varrho, [n, \varrho]] \sigma(s, t) \, ds,$$

$$L_n^{\Omega_B} = \sigma \int_L [n, \Omega_B] \, ds = [n, K_n^{\Omega_B}], \quad K_n^{\Omega_B} = \sigma \int_L [\Omega_B, [n, \Omega_B]] \, ds,$$

$$L_n^{(A)\Omega_B} = \sigma \int_L [\varrho, [n, \Omega_B]] \, ds, \quad L_n^{\Omega_B(A)} = \sigma \int_L [\Omega_B, [n, \varrho]] \, ds.$$

### Material line mass zero moment vector, mass linear moment vector and material line mass inertia moment vector at the point for the axis

The set of material points forms the material system. When the mass is continuously distributed in a certain part of the line, then there is an infinite number of material points and the system forms a continuous material line. The line region filled with the continuously distributed mass represents a material line.

In order to study the dynamics of the rigid and solid material line the geometry of mass plays an important part. In the references there is a conclusion that it is not necessary to know all the details about the mass distribution and the internal structure of the masses in order to study the material line motion under the action of the force and the properties necessary for the study of the rigid material line motion as a material system are the dynamic properties of the rigid material line. The values determining the dynamic properties are called the dynamic parameters of the rigid material line. According to the given references these parameters are taken to be: Mass  $M$  of the rigid material line; the position vector  $\varrho_C$

of the mass center of the material line, the point  $C$  with respect to a certain point  $O$  and  $\mathbf{J}^{(C)}$  the inertia tensor of the material line for the point  $C$  which is determined by six scalar dynamic parameters. In this way in the general case for the dynamic rigid material line characteristic ten independent scalar dynamic parameters are required.

Since our aim is to consider a possibility of the interpretation of the dynamic parameters of the rigid and solid material line in a modified shape we are going to set as a reference the pole  $O$  as well as the axis oriented by the unit vector  $\mathbf{n}$ . Considering that in the general case the line motion of the rigid material can be represented by one rotation around the momentary axis, that is, by the translation of the center velocity and the rotation around the axis through the given center we are led to the idea to define the line dynamic parameters of the rigid material by means of the pole  $O$  as the referential point through the position on the axis parallel to the momentary rotation axis.

Therefore we define:

1° The vector  $\mathbf{M}_n^{(A)}$  of the material line mass for the point  $A$  and the axis oriented by the unit vector  $\mathbf{n}$ :

$$\mathbf{M}_n^{(A)} = \int_L \mathbf{n} \, dm = L\mathbf{n}\sigma, \quad (1)$$

which does not depend on the mass distribution in the material line, that is, on the density  $\sigma$ . For all the space points and parallel axes it has the same value and it changes only with the axis orientation change. It is determined only by the mass quantity and the axis orientation.

2° The vector  $\mathbf{S}_n^{(A)}$  of the linear moment of the material line mass for the point  $A$  and the axis through this point oriented by the unit vector  $\mathbf{n}$  in the form

$$\mathbf{S}_n^{(A)} = \int_L [\mathbf{n}, \boldsymbol{\rho}] \, dm = \int_L [\mathbf{n}, \boldsymbol{\rho}] \sigma(s, t) \, ds, \quad (2)$$

where  $\boldsymbol{\rho}$  is the position vector of the elementary material line mass  $dm$  with respect to the pole  $A$ ,  $\mathbf{n}$  is the unit orientation axis vector through the pole  $A$ . The vector  $\mathbf{S}_n^{(A)}$  can be considered as the static moment of the material line mass for the axis oriented by the unit vector  $\mathbf{n}$  for the point  $A$ . If we denote the position vector of the material line mass center by  $\boldsymbol{\rho}_C$  with respect to the pole then it is valid for the vector  $\mathbf{S}_n^{(A)}$  of the linear moment for the point  $A$  and the axis oriented by the unit vector  $\mathbf{n}$ :

$$\mathbf{S}_n^{(A)} = M[\mathbf{n}, \boldsymbol{\rho}_C] = [\mathbf{n}, \mathbf{M}^{(A)}]. \quad (3)$$

3° The vector  $\mathbf{J}_n^{(A)}$  of the material line mass inertia moment at the point  $A$  for the axis oriented by the unit vector  $\mathbf{n}$  in the form

$$\mathbf{J}_n^{(A)} = \iiint_V [\boldsymbol{\rho}, [\mathbf{n}, \boldsymbol{\rho}]] \, dm = \int_L [\boldsymbol{\rho}, [\mathbf{n}, \boldsymbol{\rho}]] \sigma(s, t) \, ds \quad (4)$$

can also be considered as the material line mass square moment vector at the pole  $A$  for the axis through the pole oriented by the vector  $\mathbf{n}$ . The vector  $\mathbf{J}_n^{(A)}$  of the material line mass inertia moment at the point  $A$  for the axis oriented by the unit vector  $\mathbf{n}$  can be decomposed into three components: the one collinear with the axis,  $J_n^{(A)}$ , and the two other ones  $D_{nv}^{(A)}$  and  $D_{nu}^{(A)}$  in the directions normal to the orientation axis  $\mathbf{n}$ . The collinear component represents the axial moment of the material line mass inertia for the axis oriented by the unit vector  $\mathbf{n}$  through the pole  $A$ . The other two components represent the deviational moments of the material line mass for a couple of normal axes  $\mathbf{n}$  and  $\mathbf{u}$ , that is,  $\mathbf{n}$  and  $\mathbf{v}$ :

$$\mathbf{J}_n^{(A)} = J_n \mathbf{n} + D_{nv} \mathbf{v} + D_{nu} \mathbf{u}. \quad (5)$$

This definition, expression for the material line mass inertia moment vector at the point  $A$  for the axis oriented by the unit vector  $\mathbf{n}$ , can be obtained starting from the expression for the axial moment of the material line mass inertia for the axis oriented by the vector  $\mathbf{n}$  drawn through the point  $A$  and for the deviational moments of the material line mass for the couples of the orthogonal axes  $(\mathbf{n}, \mathbf{v})$  and  $(\mathbf{n}, \mathbf{u})$  according to ref. [1].

The rigid material line mass deviation moment vector at the point  $A$  for the axis  $\mathbf{n}$  is

$$\mathbf{D}_n^{(A)} = - \int_L \mathbf{T}(\mathbf{T}, \boldsymbol{\rho}) (\mathbf{n}, \boldsymbol{\rho}) \sigma \, ds = \mathbf{T} \int_L ([\mathbf{T}, \boldsymbol{\rho}], [\mathbf{n}, \boldsymbol{\rho}]) \sigma \, ds. \quad (6)$$

### Interpretation of the Pappus-Guldin theorems

Let us define the vector  $\mathbf{R}_n^{(0)}$  of the rotation of the vector  $\mathbf{S}_n^{(0)}$  of the linear moment of the material line mass for the point  $O$  and the axis through this point oriented by the vector  $\mathbf{n}$  around the same axis as

$$\mathbf{R}_n^{(0)} = 2\pi \mathbf{S}_n^{(0)}. \quad (7)$$

In this definition we have defined the rotation vector  $\mathbf{R}_n^{(0)}$  as the "circle circumference" of the diameter equal to the vector  $\mathbf{S}_n^{(0)}$  of the linear moment of the material line mass for the same axis. Now by definition the vector  $\mathbf{S}_n^{(0)}$  of the

linear moment of the body mass for the point 0 and the axis oriented by the unit vector  $n$  of the form (2) it is easy to interpret both Papos-Guldin theorems from the expression (7):

1° Interpretation of the first Papos-Guldin's theorem:

$$R_n^{(0)L} = 2\pi[n, \varrho_c] L = Pn_c. \tag{8}$$

2° Interpretation of the second Papos-Guldin's theorem:

$$R_n^{(0)A} = 2\pi[n, \varrho_c] A = Vn_c. \tag{9}$$

**The Huygens-Steiner theorem generalized to the material line mass inertia moment vector for the axis through the referential point**

The Figure 1 shows the material line and two referential points-poles 0 and A and two parallel axes through them oriented by the unit vector  $n$ . The same Figure also shows the elementary mass denoted by  $dm$  at the point N of the rigid material line and  $\varrho$  and  $r$ , the position vectors of that point with respect to the pole 0, that is, A, as well as the position vector  $\varrho_A$  of the pole A with respect to 0.

Now it is necessary to determine the change of the material line mass inertia vector  $J_n^{(0)}$  for the point 0 and the axis oriented by the unit vector  $n$  and its relation to the vector  $J_n^{(A)}$  of the material line mass inertia moment for the point A and the axis oriented by the same unit vector  $n$ .

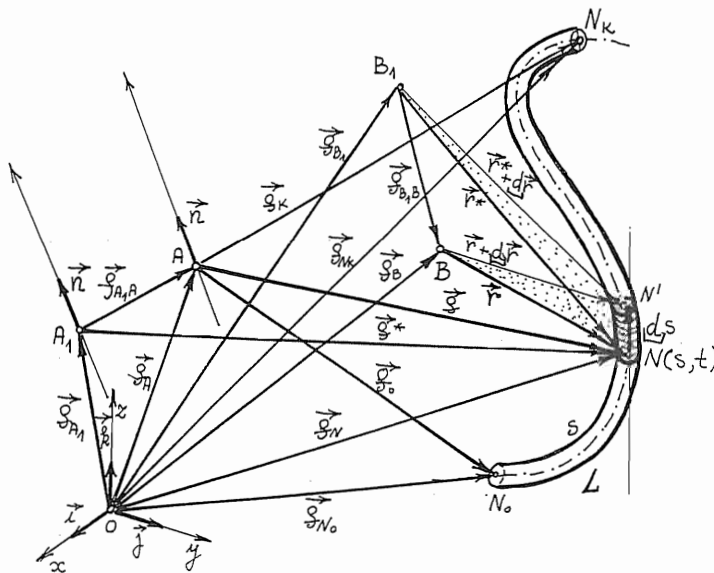


Fig. 1

This means we are interested in the change of the material line mass inertia moment vector to a certain axis which moves from one point to another retaining its orientation. By using the expression (4) defining the inertia moment vector for a certain point and axis we can write

$$J_n^{(0)} = J_n^{(A)} + [\varrho_A, S_n^{(A)}] + [M_C^{(A)}, [n, \varrho_A]] + [\varrho_A, [n, \varrho_A]] M. \tag{10}$$

We see that all the members in the last expression have the same structure. In the last expression the vector  $r_c$  is the position vector of the mass center with respect to the pole A.

In the case when the pole A is the center C of the material line mass the vector  $r_c$  is equal to zero, whereas the vector  $\varrho_A$  turns into  $\varrho_c$  so that the last expression (10) can be written in the form

$$J_n^{(0)} = J_n^{(C)} + [\varrho_c, [n, \varrho_c]] M. \tag{11}$$

This expression represents the generalized Huygens-Steiner theorem with respect to the vector  $J_n^{(0)}$  of the material line mass inertia moment for the axes oriented by the unit vector  $n$  passing through the mass center and any other point.

The part  $[\varrho_c, [n, \varrho_c]] M$  from the expression (11) represents the position part and we are going to call it the inertia position moment vector for the point 0 and the axis oriented by the unit vector  $n$ .

### The change of the material line mass inertia moment for the point and the axis at the axis orientation change through the referential point

The material line mass inertia moment vector  $J_n^{(0)}$  for the point 0 and the axis passing through it oriented by the unit vector  $n$  is equal to

$$J_n^{(0)} = J_x^{(0)} \cos \alpha + J_y^{(0)} \cos \beta + J_z^{(0)} \cos \gamma. \quad (12)$$

The last expression is analogous to the equation, which is known as the Cauchy equation in the elasticity theory.

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### Ein modellgestütztes Verfahren zur Fehlererkennung bei mechanischen Komponenten von Industrierobotern

MSC (1980): 62N05, 70F10, 73-05, 70B15

Die Erkennung von Fehlern in den mechanischen Komponenten ist eine der wichtigen Aufgaben der Roboterdiagnose. Außer der Methode der Signalanalyse besteht noch die Möglichkeit, Fehler mit Hilfe der Modellkenntnisse der Roboter-Mechanik durch regelungstechnische Schätzverfahren zu detektieren. Es wird hier ein modellgestütztes Verfahren vorgestellt. Dieses Verfahren basiert auf einem dynamischen Mehrkörpermodell des Roboters mit Berücksichtigung des Reibungseffektes und der Elastizität in den Antriebsstäben. Die Kenngrößen, deren Änderungen das Fehlverhalten des Roboters kennzeichnen, werden u. a. durch den an jeder Roboterachse implementierten Nichtlinearitäten-Beobachter ermittelt. Durch den Vergleich zwischen den aus dem Modell berechneten idealen und den aktuell geschätzten Zuständen des Roboters werden dann die möglichen Fehler erkannt.

#### Auswahl der Kenngrößen aus dynamischen Modellen

Es werden Roboter mit rotatorischen Freiheitsgraden betrachtet. Jede Achse des Roboters wird hierbei von einem Gleichstrom-Motor über ein einstufiges Getriebe mit der Übersetzung  $n_i$  angetrieben, dessen Nachgiebigkeit als lineare Drehfeder  $k_i$  modelliert wird, siehe Bild 1. Wird der auf die Getriebeübersetzung bezogene Motorwinkel mit  $p_i$  ( $p_i = \theta_i/n_i$ ) und die Lagekoordinate des Roboterarmes mit  $q_i$  bezeichnet, so läßt sich das dynamische Modell [1] des Roboters beschreiben als

$$M(q) \ddot{q} + h(q, \dot{q}) + K(q - p) = 0, \quad (1)$$

$$J\ddot{p} + f - K(q - p) = \tau, \quad (2)$$

wobei  $J$  und  $M(q)$  jeweils die Massenmatrizen der Motoren und der Ausleger bezeichnen. In  $h(q, \dot{q})$  sind die Zentrifugal- und Corioliskräfte sowie die Gewichte der Ausleger zusammengefaßt. Die Antriebsmomente  $\tau$  werden an den Motorachsen

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## THE ANALOGY BETWEEN THE STRESS STATE MODEL, THE STRAIN STATE MODEL AND THE MASS INERTIA MOMENT STATE MODEL

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**Abstract.** The paper introduces the notation of the total specific deformation vector  $\delta_n^{(N)}$  for the line element drawn from the point  $N$  of the deformable body in natural configuration in the direction of the unit vector  $\vec{n}$  and the notation of the mass inertia moment vector  $\vec{J}_n^{(N)}$  for the axis oriented by the unit vector  $\vec{n}$  and for the pole  $N$ .

The paper introduces the notation of the total specific deformation vector  $\delta_n^{(N)}$  for the line element drawn from the point  $N$  of the deformable body in natural configuration in the direction of the unit vector  $\vec{n}$  and the notation of the mass inertia moment vector  $\vec{J}_n^{(N)}$  for the axis oriented by the unit vector  $\vec{n}$  and for the pole  $N$ .

A comparative analogy is drawn between the total stress vector  $\vec{p}_n^{(N)}$  at the point  $N$  of the deformable body for the plane with the normal  $\vec{n}$  and the vector  $\delta_n^{(N)}$  of the total specific deformation (strain) for the line element in the direction of the unit vector  $\vec{n}$  drawn from the point  $N$ , as well as the vector  $\vec{J}_n^{(N)}$  of the mass inertia moment of the body for the axis oriented by the unit vector  $\vec{n}$  through the point  $N$ . The analogy between the following notions is pointed out: the stress state model and the strain state model in the Theory of Elasticity as well as the mass inertia moment state model of the rigid body in the given point.

The paper further also points out the identity of the mathematical models for the determination of the principal stresses directions, principal strain directions and principal inertia axes as well as an analogy between the plane of the shearing

stresses extreme values, the line elements directions between which the extreme values of the sliding deformation and the inertial asymmetry for which the greatest values of the centrifugal moments of the rigid body mass occur.

This paper defines the kinetic vector fixed to a certain point  $N$  and axis passing through the given rigid body point. This vector is: the vector  $\vec{J}_n^{(N)}$  of the body mass inertia moment for the point  $N$  and the axis oriented by the unit vector  $\vec{n}$ . The change of the vector of the body mass inertia moment in the transition from one rigid body point to another is not determined in this paper.

### 1. THE DEFINITION FOR THE BODY MASS INERTIA MOMENT VECTOR

Since our aim is to consider a possibility of the interpretation of the rigid body mass kinetic parameters in a modified shape we are going to set as a reference the pole  $N$  as well as the axis oriented by the unit vector  $\vec{n}$ . Considering that in the general case the rigid body motion can be represented by the translation of the mass center velocity and the rotation around the axis through the given center we are led to the idea to define the rigid body dynamic parameters by means of the pole  $N$  as the referential point through which we put an axis parallel to the momentary rotation axis.

There fore we define the following vector  $\vec{J}_n^{(N)}$  of the body mass inertia moment at the point  $N$  for the axis oriented by the unit vector  $\vec{n}$  in the form:

$$\vec{J}_n^{(N)} = \iiint_V [\vec{\rho}, [\vec{n}, \vec{\rho}]] dm \quad (1)$$

where  $\vec{\rho}$  is the position vector of the elementary body mass  $dm$  with respect to the pole  $N$ . The illustration is given in the Figure 1.

It can also be considered the body mass square moment vector at the pole  $N$  for the axis through the pole oriented by the vector  $\vec{n}$ . The vector  $\vec{J}_n^{(N)}$  of the body mass inertia moment at the point  $N$  for the axis oriented by the unit vector  $\vec{n}$  can be decomposed into three components: the colinear with the axis  $J_n^{(N)}$  and the two other ones  $D_{nv}^{(N)}$  and  $D_{nu}^{(N)}$  in the directions normal to the orientation of axis  $\vec{n}$ . The colinear component represents the axial moment of the body mass inertia for the axis oriented by the unit vector  $\vec{n}$  through the pole  $N$ . The other two components represent the deviational moments of the body mass for a couple of normal axes  $\vec{n}$  and  $\vec{u}$ , that is,  $\vec{n}$  and  $\vec{v}$ :

$$\vec{J}_n^{(N)} = J_n^{(N)} \vec{n} + D_{nv}^{(N)} \vec{v} + D_{nu}^{(N)} \vec{u} \quad (2)$$

The definition - expression for the body mass inertia moment vector at the point  $N$  for the axis oriented by the unit vector  $\vec{n}$  can be obtained starting from the expression for the axial body mass inertia moment for the axis oriented by the vector  $\vec{n}$  drawn through the point  $N$  and for the deviational body mass moments



The rigid body mass deviation moment vector at the point N for the axis  $\vec{n}$ .

$$\vec{D}_n^{(N)} = \vec{v} \iiint_V ([\vec{n}, \vec{\rho}], [\vec{v}, \vec{\rho}]) dm + \vec{u} \iiint_V ([\vec{n}, \vec{\rho}], [\vec{u}, \vec{\rho}]) dm \quad (8)$$

$$\vec{D}_n^{(N)} = - \iiint_V \vec{T} (\vec{T}, \vec{\rho}) (\vec{n}, \vec{\rho}) dm = \vec{T} \iiint_V ([\vec{T}, \vec{\rho}], [\vec{n}, \vec{\rho}]) dm \quad (8^*)$$

By means of the previous expressions the expression (6) for the vector  $\vec{J}_n^{(N)}$  of the body mass inertia moment at the point N for the axis oriented by the unit vector  $\vec{n}$  we can write the following:

$$\vec{J}_n^{(N)} = \iiint_V [\vec{\rho}, [\vec{n}, \vec{\rho}]] dm \quad (1^*)$$

and that's how we have come to the expression identical to the expression (1). The illustration is given in the Figure 2.

## 2. THE CHANGE OF THE BODY MASS INERTIA MOMENT FOR THE POINT AND THE AXIS AT THE AXIS ORIENTATION CHANGE THROUGH THE REFERENTIAL POINT

Let's now define the vectors  $\vec{J}_x^{(N)}$ ,  $\vec{J}_y^{(N)}$  and  $\vec{J}_z^{(N)}$  of the body mass inertia moments at the point N and for the coordinate axes  $N_x$ ,  $N_y$  and  $N_z$ . These vectors can be expressed in the form:

$$\vec{J}_x^{(N)} = \iiint_V [\vec{\rho}, [\vec{i}, \vec{\rho}]] dm = J_x \vec{i} + D_{xy} \vec{j} + D_{xz} \vec{k} \quad / \cdot \cos \alpha \quad (9)$$

$$\vec{J}_y^{(N)} = \iiint_V [\vec{\rho}, [\vec{j}, \vec{\rho}]] dm = D_{yx} \vec{i} + J_y \vec{j} + D_{yz} \vec{k} \quad / \cdot \cos \beta \quad + \quad (10)$$

$$\vec{J}_z^{(N)} = \iiint_V [\vec{\rho}, [\vec{k}, \vec{\rho}]] dm = D_{zx} \vec{i} + D_{zy} \vec{j} + J_z \vec{k} \quad / \cdot \cos \gamma \quad (11)$$

If we denote the sences cosine of the unit vector  $\vec{n}$  with  $\cos \alpha$ ,  $\cos \beta$  and  $\cos \gamma$  when the unit vector defines the orientation of the axis passing through the point N, then we can successively multiply the expressions from (9) to (11) and we obtain them by adding:

$$\begin{aligned} \vec{J}_x^{(N)} \cos \alpha + \vec{J}_y^{(N)} \cos \beta + \vec{J}_z^{(N)} \cos \gamma = \\ = \iiint_V [\vec{\rho}, [\vec{i} \cos \alpha + \vec{j} \cos \beta + \vec{k} \cos \gamma, \vec{\rho}]] dm = \iiint_V [\vec{\rho}, [\vec{n}, \vec{\rho}]] dm \quad (12) \end{aligned}$$

From the previous expression we conclude that the body mass inertia moment vector  $\vec{J}_n^{(N)}$  for the point N and the axis passing through it oriented by the unit

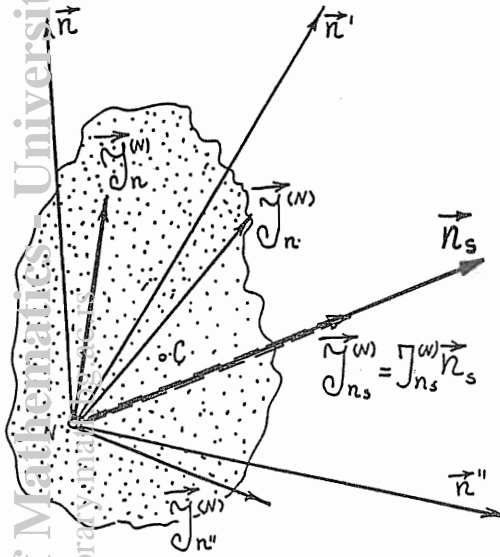


FIGURE 3.

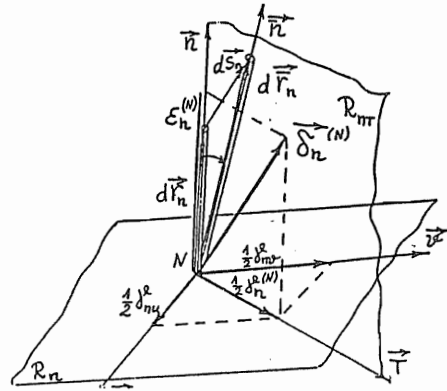


FIGURE 4.

vector  $\vec{n}$  is equal to:

$$\vec{J}_n^{(N)} = \vec{J}_x^{(N)} \cos \alpha + \vec{J}_y^{(N)} \cos \beta + \vec{J}_z^{(N)} \cos \gamma \quad (13)$$

The last expression is analogous to the equation for determining the total stress vector  $\vec{p}_n^{(N)}$  at the point N of the stressed body for the plane normal  $\vec{n}$  which is known as the Cauchy equation in the Elasticity Theory. Therefore we are going to call it the Cauchy equation giving the relation of the body mass inertia moment vector  $\vec{J}_n^{(N)}$  for an arbitrary axis oriented by the unit vector  $\vec{n}$  drawn through the point N and the vectors  $\vec{J}_x^{(N)}$ ,  $\vec{J}_y^{(N)}$  and  $\vec{J}_z^{(N)}$  of the body mass inertia moments at the same point for the coordinate axes.

### 3. MAIN INERTIA DIRECTIONS, MAIN INERTIA MOMENTS

By means of the vector  $\vec{J}_n^{(N)}$  of the rigid body inertia moment we can introduce a new definition of the main inertia axes. Through one pole N we can draw an infinite number of axes of orientation. Among them we are looking for the axis for which the vector  $\vec{J}_n^{(N)}$  of the body mass inertia moment had only one component colinear with the axis, that is, the one for which the vector  $\vec{D}_n^{(N)}$  of the deviation load of the axis by the body mass inertia moment is equal to zero. Using the analogy between the stress tensor matrices and the tensor matrices of mass inertia moments as well as the matrix interpretation as more appropriate for this case and by denoting the unit vector of the main inertia axis orientation with  $\vec{n}$  which is in accordance with the Fig. 3, we can write:

$$\{J_{n_s}^{(N)}\} = \mathbb{J}^{(N)}\{n_s\} = J_s^{(N)}\{n_s\} \tag{14}$$

$$\left(\mathbb{J}^{(N)} - J_s^{(N)}\mathbb{I}\right)\{n_s\} = \{0\} \tag{15}$$

so that the Hamilton equation for determining the main inertia moments:

$$f(J_s^{(N)}) = |\mathbb{J}^{(N)} - J_s^{(N)}\mathbb{I}| = 0 \tag{16}$$

$$f(J_s) = \begin{vmatrix} J_x - J_s & D_{yx} & D_{xz} \\ D_{xy} & J_y - J_s & D_{yz} \\ D_{xz} & D_{yz} & J_z - J_s \end{vmatrix} = 0 \tag{17}$$

$$f(J_s) = -(J_s^3 - J_1 J_s^2 + J_2 J_s - J_3) = 0 \tag{17*}$$

while for the senses cosines of the main inertia axes the following relations are obtained:

$$\frac{\cos \alpha_s}{K_{31}^{(s)}} = \frac{\cos \beta_s}{K_{32}^{(s)}} = \frac{\cos \gamma_s}{K_{33}^{(s)}} = C_s \tag{18}$$

$$\cos^2 \alpha_s + \cos^2 \beta_s + \cos^2 \gamma_s = 1 \tag{19}$$

$K_{31}^{(s)}$ ,  $K_{32}^{(s)}$  and  $K_{33}^{(s)}$  are co-factors of the third kind elements and the corresponding matrix column:

$$\begin{aligned} K_{31}^{(s)} &= \begin{vmatrix} D_{yx} & D_{xz} \\ J_y - J_s & D_{yz} \end{vmatrix} \\ K_{32}^{(s)} &= - \begin{vmatrix} J_x - J_s & D_{xz} \\ D_{xy} & D_{yz} \end{vmatrix} \\ K_{33}^{(s)} &= \begin{vmatrix} J_x - J_s & D_{yx} \\ D_{xy} & J_y - J_s \end{vmatrix} \end{aligned} \tag{20}$$

successively for the roots of the Hamilton equations  $J_1, J_2$  and  $J_3$  which are the main inertia moments and which represent the axial inertia moments for the main inertia moments. There are three roots and three orthogonal main axes at every point with respect to which the rigid body inertia moment vectors are determined. The Hamilton equation coefficients are the first, second and third invariants of the inertia  $J_1^{(N)}, J_2^{(N)}$  and  $J_3^{(N)}$ , and they are the first, second and third scalar of the body mass inertia tensor matrix. These are the invariants of the rigid body mass inertia state at the point N. The roots of the Hamilton equation are always real and positive.

By using the Viette formulae we can write the relation between the inertia state invariants at the given point and the main moments of the body mass inertia at the given point:

$$\begin{aligned} J_1^{(N)} &= J_1^{(N)} + J_2^{(N)} + J_3^{(N)} \\ J_2^{(N)} &= J_1^{(N)} J_2^{(N)} + J_1^{(N)} J_3^{(N)} + J_2^{(N)} J_3^{(N)} \\ J_3^{(N)} &= J_1^{(N)} J_2^{(N)} J_3^{(N)} \end{aligned} \tag{21}$$



#### 4. THE LINE ELEMENT TOTAL STRAIN VECTOR

The displacement vector corresponding to the pure deformation (as well as the change of the shape and volume) of the line element  $d\vec{r}_n = dr \vec{n}$  is defined as the deformation vector  $d\vec{s}_n$  (see Ref. /8/):

$$\{ds_{def}\} = \{ds_n\} = \mathcal{E}\mathcal{E}\{dr_n\} \quad (22)$$

Following the concept of analogous parameters in the models of the stress theory and the strain theory and by applying the formal approach we can introduce the vector  $\vec{\delta}_n = d\vec{s}_{def}/dr$  which is to be called the line element total strain vector in the direction of the unit vector  $\vec{n}$  drawn from the point N of the deformable body which is an analogous parameter to the vector  $\vec{p}_n^{(N)}$  of the total stress at the point N for the plane with the normal  $\vec{n}$ . The vector  $\vec{\delta}_n^{(N)}$  of the line element total strain (specific deformation) in the direction of the unit vector  $\vec{n}$  from the point N can be determined by the specific deformation tensor matrix of the following form:

$$\begin{aligned} \vec{\delta}_n^{(N)} &= \varepsilon_n \vec{n} + \frac{1}{2} \gamma_n T \vec{T} = \frac{1}{2} \varepsilon_n \vec{n} + \frac{1}{2} \gamma_{nu} \vec{u} + \gamma_{nv} \vec{v} = \delta_{nx} \vec{i} + \delta_{ny} \vec{j} + \delta_{nz} \vec{k} \\ \{\delta_n^{(N)}\} &= \mathcal{E}\mathcal{E}^{(N)}\{n\} \quad \vec{\delta}_n^{(N)} = \vec{\delta}_x^{(N)} \cos \alpha + \vec{\delta}_y^{(N)} \cos \beta + \vec{\delta}_z^{(N)} \cos \gamma \end{aligned} \quad (23)$$

so that the equations (23) correspond to the Cauchy's equations for the vector  $\vec{p}_n^{(N)}$  of the total stress at the point N of the deformable body for the plane with the unit vector  $\vec{n}$ .

For the line elements  $dx, dy$  and  $dz$  from the point N in the directions of the coordinate axes  $x, y$  and  $z$  we can define three vectors  $\vec{\delta}_x^{(N)}, \vec{\delta}_y^{(N)}$  and  $\vec{\delta}_z^{(N)}$  of the total specific deformation (total strain) as:

$$\begin{aligned} \vec{\delta}_x^{(N)} &= \varepsilon_x \vec{i} + \frac{1}{2} \gamma_{xy} \vec{j} + \frac{1}{2} \gamma_{xz} \vec{k} \\ \vec{\delta}_y^{(N)} &= \frac{1}{2} \gamma_{yx} \vec{i} + \varepsilon_y \vec{j} + \frac{1}{2} \gamma_{yz} \vec{k} \\ \vec{\delta}_z^{(N)} &= \frac{1}{2} \gamma_{zx} \vec{i} + \frac{1}{2} \gamma_{zy} \vec{j} + \varepsilon_z \vec{k} \end{aligned} \quad (24)$$

or

$$\{\delta_x^{(N)}\} = \begin{Bmatrix} \varepsilon_x \\ \frac{1}{2} \gamma_{xy} \\ \frac{1}{2} \gamma_{xz} \end{Bmatrix} \quad \{\delta_y^{(N)}\} = \begin{Bmatrix} \frac{1}{2} \gamma_{yx} \\ \varepsilon_y \\ \frac{1}{2} \gamma_{yz} \end{Bmatrix} \quad \{\delta_z^{(N)}\} = \begin{Bmatrix} \frac{1}{2} \gamma_{zx} \\ \frac{1}{2} \gamma_{zy} \\ \varepsilon_z \end{Bmatrix} \quad (24^*)$$

thus corresponding to the following stress theory vectors  $\vec{p}_x^{(N)}, \vec{p}_y^{(N)}$  and  $\vec{p}_z^{(N)}$  of the total stress for the coordinate planes through the same point N.

For an arbitrary line element  $d\vec{r}_n$  drawn from the point N in the direction can be divided into two components, one in the direction of the vector  $\vec{n}$  and the other in the direction perpendicular to the unit vector  $\vec{n}$ .

Figure 4. shows the line element  $d\vec{r}_n$  drawn from the point N in the direction of the unit vector  $\vec{n}$  in the body natural configuration as well as the same element  $d\vec{r}_n$

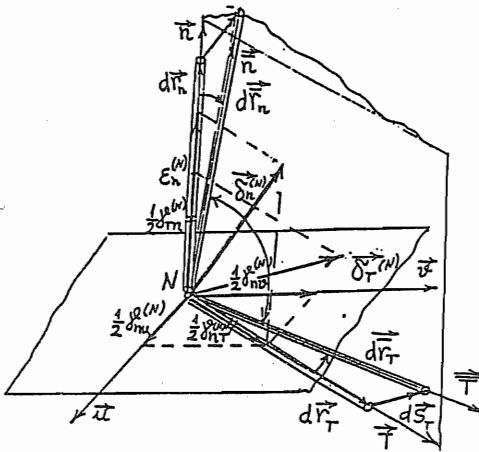


FIGURE 5.

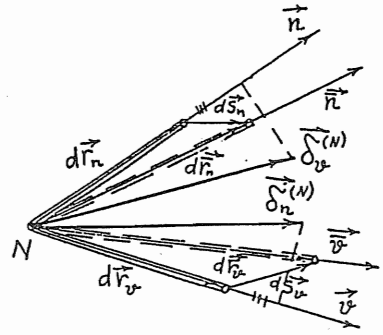


FIGURE 8.

in the forced configuration of the deformed deformable body drawn from the same point for the sake of comparison. The displacement vector  $ds_n^{(N)}$  corresponding to the pure deformation is also shown. In the same figure the vector  $\delta_n^{(N)}$  of the total strain (total specific deformation) is shown its projections being  $\epsilon_n^{(N)}$  on the direction of the unit vector  $\vec{n}$  as well as  $\gamma_n^{(N)}/2$  on the orthogonal direction  $\vec{T}$  with respect to the unit vector  $\vec{n}$  whereas on the orthogonal plane with respect to the unit vector  $\vec{n}$ . The plane  $R_n$  is the one in which the following vectors lie:  $d\vec{r}_n, \vec{n}, ds_n^{(N)}, \delta_n^{(N)}, \vec{T}$  and  $d\vec{r}_n$ .

The component  $\epsilon_n^{(N)}$  in the direction of the unit vector  $\vec{n}$  represents the dilatation of the observed line element from the direction determined by the unit vector  $\vec{n}$  whereas the component  $\gamma_n^{(N)}/2$  in the direction determined by the unit vector  $\vec{T}$  orthogonal to the unit vector  $\vec{n}$  represents the turning of the line element with respect to the natural configuration within the plane  $R_{nT}$  determined by the unit vector  $\vec{n}$  and the specific deformation vector of the given line element. This is approximately half of the change of the right angle between the line elements in the direction of the unit vector  $\vec{n}$  and its coupled direction determined by the unit vector  $\vec{T}$  of the projection direction of the total strain (specific deformation) vector  $\delta_n^{(N)}$  on the plane orthogonal to the line element unit vector in the direction of the unit vector  $\vec{n}$ . The Figure 5. gives the sketch of the coupled line elements in the forced and natural configuration as well as their specific deformations vectors with respective parameters denoted. The same figure will also be used for further analysis.

If we now project the component  $\gamma_n^{(N)}/2$  on the two orthogonal directions  $\vec{u}$  and  $\vec{v}$  in the plane  $R_n$ , we shall obtain two sliding (shear) components  $\gamma_{nu}^{(N)}/2$  and

$\gamma_{\vec{n}\vec{v}}^{(N)}/2$ , that is, half of the change of the right angle between the line elements in the directions determined by the unit vector  $\vec{n}$  and the unit vector  $\vec{v}$ , that is,  $\vec{v}$ . In other words, we shall obtain the right angle changes of the basic line element with respect to the directions  $\vec{u}$  or  $\vec{v}$ . In further comparison of the analogous parameters of the stress theory and the deformation theory it should be pointed out that the total stress vector  $\vec{p}_n^{(N)}$  is related to the point and the plane with normal  $\vec{n}$  as well as to the orthogonal direction indirectly, whereas the total strain (specific deformation) vector  $\vec{\delta}_n^{(N)}$  is related to the point and line determined by the unit vector  $\vec{n}$  and indirectly to the orthogonal plane  $R_n$  and the coupled direction  $\vec{T}$  within it. The coupled direction  $\vec{T}$  belonging to the deformation theory finds its correspondent in the coupled plane perpendicular to the plane  $R_n$  and in the shear stress  $\tau_T^{(N)}$  within that plane within which, according to the rule of shear stress conjugativity, the stress of the same intensity as  $\tau_n^{(N)}$  occurs, which falls into the direction  $\vec{T}$ , since  $\tau_n^{(N)} = \tau_T^{(N)}$ , that is,  $\tau_{nT}^{(N)} = \tau_{Tn}^{(N)}$ .

Further analysis helps us perceive that the two orthogonal planes  $R_n$  and  $R_v$  with the normal unit vectors  $\vec{n}$  and  $\vec{v}$  in which the conjugated shear stresses  $\tau_{nv}^{(N)}$  and  $\tau_{vn}^{(N)}$  occur correspond to the two orthogonal directions determined by the unit vectors  $\vec{n}$  and  $\vec{v}$  of the line elements between which the right angle change is determined, i.e., the specific deformation (sliding/shear)  $\gamma_{nv}^{(N)}/2$  and  $\gamma_{vn}^{(N)}/2$  which represent the same angle.

## 5. THE PRINCIPAL STRAIN DIRECTIONS

Let's analyze the approach in the stress theory to the determination of the principal strain direction. From the point N of the deformable body in natural configuration we can draw an infinite number of line elements  $d\vec{r}_n = \vec{n}dr$  and in forced configuration of the deformed stressed body we can define for each of them the displacement vector  $d\vec{s}_{n\text{def}}$  corresponding to the pure deformation and the corresponding vector  $\vec{\delta}_n^{(N)}$  of the line element specific deformation in the direction of the respective unit vector  $\vec{n}$  which in the general case has two components. Besides the very well known definition that the principal dilatation directions are characterized by the presence of dilatation, by the absence of sliding and by absence of the right angle change between the three principal orthogonal directions they can also be defined now as those in which the total strain (specific deformation) vector  $\vec{\delta}_n^{(N)}$  is colinear with the corresponding line element direction in natural configuration so that the line element retains its direction. Figure 6. gives a geometrical representation of the principal direction determined by the unit vector  $\vec{n}_s$  as well as the corresponding representation in the stress theory.

The plane perpendicular to one principal dilatation direction in natural configuration of the deformable body includes at least two mutually orthogonal elements between which the right angle does not change during the body transition to forced configuration, in other words, no sliding occurs between them. These are the two

remaining principal dilatation directions. Those line elements remain in this plane even in forced configuration although in the general case the remaining line elements in this plane in natural configuration drawn from the same point in forced configuration do not have to stay there (See Fig. 6).

## 6. THE SLIDING EXTREME VALUES OF THE ORTHOGONAL LINE ELEMENTS

Let's consider now an analogy between the shear stresses extreme values in orthogonal planes through one point and the sliding extreme values of the orthogonal line elements drawn from the same point of the body.

By using the analogy between the shear stresses  $\tau_{nv}^{(N)}$  and sliding  $\gamma_{nv}^{(N)}$  we can conclude that shear stresses extreme values correspond to the line elements sliding extreme values. Since we have determined the shear stresses extreme values planes by the angles of  $\pm 45^\circ$  with respect to the principal stress directions, therefore, the line elements directions which the greatest slidings as specific deformations occur for, that is, between the pairs undergoing the greatest right angles changes, can be determined with respect to the principal dilatations. Therefore, these are the line elements determined by the directions forming an angle of  $\pm 45^\circ$  with respect to the principal dilatations directions and these changes of the right angles are equal to the difference between the principal dilatations. There are three pairs of such line elements and six directions of the line elements. We can write that:

$$\gamma_{I_{ab}} = \pm(\varepsilon_2 - \varepsilon_3) \quad \gamma_{II_{ab}} = \pm(\varepsilon_1 - \varepsilon_3) \quad \gamma_{III_{ab}} = \pm(\varepsilon_1 - \varepsilon_2) \quad (25)$$

(2) The dilations corresponding to these slidings for these line elements in given point N are:

$$\varepsilon_{I_{ab}} = \frac{1}{2}(\varepsilon_2 + \varepsilon_3) \quad \varepsilon_{II_{ab}} = \frac{1}{2}(\varepsilon_1 + \varepsilon_3) \quad \varepsilon_{III_{ab}} = \frac{1}{2}(\varepsilon_1 + \varepsilon_2) \quad (26)$$

Figure 7. shows the line elements directions which the greatest extreme sliding (shear) values occur for.

If  $\varepsilon_1$  and  $\varepsilon_2$  are the greatest and the smallest dilatations then  $\gamma_{III_a III_b}$  is the greatest sliding, that is, the greatest change of the right angle between these line elements of the pair  $III_a, III_b$ . Therefore, the pair of the two orthogonal directions determining the line elements between which the greatest shear occurs, that is, the right angle change lies in the plane defined by the principal dilatations directions which are the greatest and the smallest dilatations halving the angle between them.

It should be noted that sliding is related to the line element direction and to the given plane in which this line element lies or otherwise for two orthogonal directions and the change of the right angle between them.

In the Figure 7. we can see the pairs of the directions  $I_a$  and  $I_b$ ,  $II_a$  and  $II_b$ ,  $III_a$  and  $III_b$  of the drawn line elements from the observed point of the deformable body which are mutually orthogonal in the configuration of the natural state of the body, and with respect to the forced configuration between which the extreme changes of

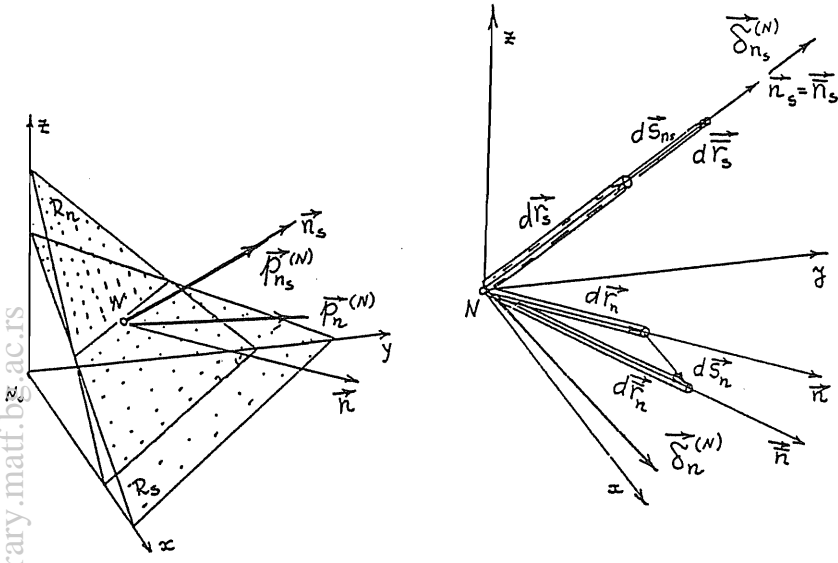


FIGURE 6.

the right angles occur comparing to the other pairs of the orthogonal line elements being drawn from the same point. Therefore, during the transition of the body from the natural into the forced configuration the extreme sliding value is between such pairs of the line elements.

If the two principal dilatations are mutually equal, then there is only at least one more pair of the orthogonal line elements between which there is no right angle change, that is, there is no sliding, but which lie in the plane of the principal dilatations directions being the pair of the directions forming an angle of  $\pm 45^\circ$  with respect to these two directions. This leads us to conclude that the remaining principal direction is the axis of the deformation symmetry at the observed point of the body in natural configuration.

If the two principal dilatations at the observed point of the body are the same regarding their absolute values whereas different in sign (shortening - lengthening), then from this point the two orthogonal line elements can be drawn between which the extreme value of the specific deformation lies, that is, of sliding (shear), that is, of the right angle change. Therefore, these line elements are without dilatations, that is, without any change in length. These are directions of the line elements with the pure shear (pure sliding).

If between these line elements with pure shear we perceive a surface element whose edges follow the directions of these line elements, then such line element does not undergo any surface change during the deformable body transition from the natural into the forced configuration whereas the volumetric element designed above it in the third dimension in the direction of the remaining principal dilatation has a volumetric dilatation equal to this principal dilatation.

## 7. EXTREME VALUES OF THE MASS DEVIATION MOMENTS

For determining the mass deviation moments extreme values we shall use this analogy which exists between the stress tensor matrices, the relative deformation tensor and the body mass inertia tensor as well as between the vector  $\vec{p}_n^{(N)}$  of the total stress at a certain body point for the plane with the normal  $\vec{n}$ , the vector  $\vec{\delta}_n^{(N)}$  of the total relative deformation of the line element drawn from the observed point in the direction of the unit vector  $\vec{n}$  and the vector  $\vec{J}_n^{(N)}$  of the body mass inertia moment at the observed pole for the axis oriented by the unit vector  $\vec{n}$ .

On the basis of the given analogy the following conclusion are drawn though without proofs: on the basis of the analogy between the mass deviation moments extreme values for a couple of orthogonal axes (that is, of the mass centrifugal moments) and yield stress extreme values in the orthogonal planes that pass in pairs through one single stress direction and form an angle of  $\pm 45^\circ$  with the other two we conclude that the mass deviation moments extreme values appear for the axes pairs  $I_a$  and  $I_b$ ,  $II_a$  and  $II_b$ ,  $III_a$  and  $III_b$  that pass in pairs through the main body mass inertia axis through the given point and form angles of  $\pm 45^\circ$  with the other two main inertia axes. For these pairs of the defined axes the mass deviation moments (the mass centrifugal moments) are equal to the semi-difference between the two main (axial) moment of the body mass inertia and for each axis in the corresponding pair the axial inertia moments are equal to the semi-sum of the two corresponding main moments of the body mass inertia for the given point. For the geometrical interpretation the Figure can be used. The pairs of these coupled axes are the inertia asymmetry axes since for them the mass centrifugal moments are extreme values and the axial inertia moments for both the axes in pair are mutually equal. The concept of "asymmetry" can be accepted since for symmetry axes the mass centrifugal moment is equal to zero and for these axes the body mass centrifugal moment is of extreme value so that this leads to the conclusion about the asymmetry of the material body inertia properties. On the basis of the given analogy and for the axes according to the Fig. 7. we can write the values of the mass deviation moments and the body mass axial inertia moments for these axes:

$$\begin{aligned}
 D_{I_a I_b}^{(N)} &= \pm \frac{J_2^{(N)} - J_3^{(N)}}{2} & J_{I_a}^{(N)} &= J_{I_b}^{(N)} = \frac{J_2^{(N)} + J_3^{(N)}}{2} \\
 D_{II_a II_b}^{(N)} &= \pm \frac{J_1^{(N)} - J_3^{(N)}}{2} & J_{II_a}^{(N)} &= J_{II_b}^{(N)} = \frac{J_1^{(N)} + J_3^{(N)}}{2} \\
 D_{III_a III_b}^{(N)} &= \pm \frac{J_2^{(N)} - J_1^{(N)}}{2} & J_{III_a}^{(N)} &= J_{III_b}^{(N)} = \frac{J_2^{(N)} + J_1^{(N)}}{2}
 \end{aligned} \tag{27}$$

These conclusions can be proved by means of the defined vector  $\vec{J}_n^{(N)}$  of the rigid body mass inertia moment and the vector  $\vec{D}_n^{(N)}$  of the axis deviation load oriented by the unit vectors of the defined axes with the extreme values of the rigid body mass deviation moments for the referential point.



## 8. THE BASIC RULE OF THE DEFORMATION ANALYSIS

By introducing the total strain (specific deformation) vector  $\vec{\delta}_n^{(N)}$  of the line element in the direction of the unit vector  $\vec{n}$  we can deduce the rule of the deformation analysis analogous to the stress analysis rule which comes to the rule of the shear stress conjugativity for the case of the orthogonal planes. Therefore, we should notice two line elements drawn from the point  $N$  of the deformable body in natural configuration in the direction of the unit vector  $\vec{n}$  and  $\vec{v}$  which in the general case form an arbitrary angle as it is shown in the Figure 8. The corresponding vectors  $\vec{\delta}_n^{(N)}$  and  $\vec{\delta}_v^{(N)}$  of the total strain (specific deformations) for these line elements are

$$\{\delta_n^{(N)}\} = \mathcal{E}\mathcal{E}^{(N)}\{n\} \quad \{\delta_v^{(N)}\} = \mathcal{E}\mathcal{E}^{(N)}\{v\} \quad (28)$$

If the former is multiplied scalarly by the unit vector  $\vec{v}$  and the latter by the unit vector  $\vec{n}$  and if we compare the results, we will obtain the following:

$$pr_{\vec{v}}\vec{\delta}_n^{(N)} = pr_{\vec{n}}\vec{\delta}_v^{(N)} \quad (v)\{\delta_n^{(N)}\} = (n)\{\delta_v^{(N)}\} \quad (29)$$

Hence we conclude that the projection of the vector  $\vec{\delta}_n^{(N)}$  of the total strain (specific deformation) of the line element drawn from the point  $N$  in the direction of the unit vector  $\vec{n}$  on the direction of the unit vector  $\vec{v}$  is equal to the projection of the vector  $\vec{\delta}_v^{(N)}$  of the total strain (specific deformation) of the line element drawn from the same point  $N$  of the deformable body in the direction of the unit vector  $\vec{v}$  on the direction of the unit vector  $\vec{n}$  for the same deformation state at the point  $N$ .

This is the basic rule of the deformation analysis. For the case of the orthogonal directions  $\vec{n}$  and  $\vec{v}$  and therefore for the orthogonal line elements, the product

$$\frac{1}{2}\gamma_{nv}^{(N)} = (v)\{\delta_n^{(N)}\}, \quad \text{that is,} \quad \frac{1}{2}\gamma_{vn}^{(N)} = (n)\{\delta_v^{(N)}\} \quad (30)$$

represents the line element sliding  $\gamma_{nv}^{(N)}/2$ , that is,  $\gamma_{vn}^{(N)}/2$ , that is, half of the change of the right angle between the line elements. Hence, it follows from the expression (29) that:

$$\frac{1}{2}\gamma_{nv}^{(N)} = \frac{1}{2}\gamma_{vn}^{(N)} \quad (31)$$

that is, that the line element sliding in the direction of the unit vector  $\vec{n}$  in the plane  $(\vec{n}, \vec{v})$  is equal to the line element sliding in the direction of the unit vector  $\vec{v}$  in the plane  $(\vec{v}, \vec{n})$ .

## 9. THE BASIC RULE OF THE STATE ANALYSIS OF THE BODY MASS INERTIA MOMENT

On the basis of the analogy with the basic rule of the stress analysis, that is, the deformation analysis in the Elasticity Theory there is the basic rule of the state

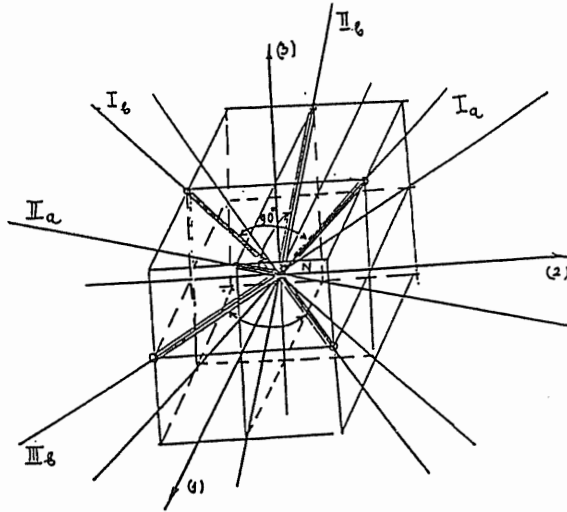


FIGURE 7A.

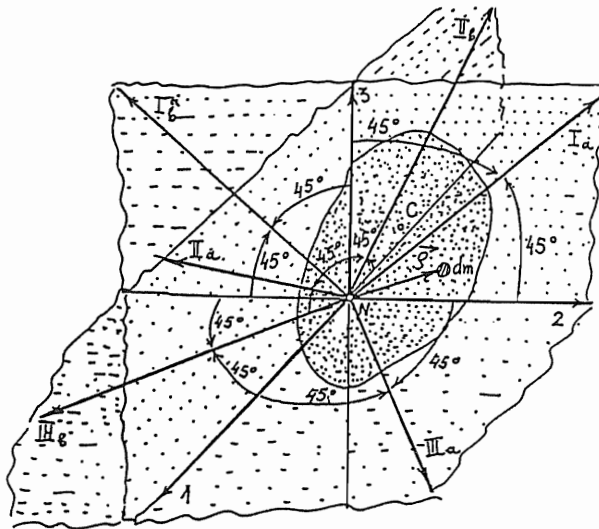


FIGURE 7B.

analysis of the body mass inertia moment with respect to a certain pole  $N$  in the form:

$$pr_{\vec{v}} \vec{J}_n^{(N)} = pr_{\vec{n}} \vec{J}_{\vec{v}}^{(N)} \quad (32)$$

which says that the projection of the vector  $\vec{J}_n^{(N)}$  of the rigid body mass inertia moment for the point  $N$  and the axis oriented by the unit vector  $\vec{n}$  to the axis oriented by the unit vector  $\vec{v}$  is equal to the projection of the vector  $\vec{J}_{\vec{v}}^{(N)}$  of the

same rigid body mass inertia moment for the same point  $N$  and the axis oriented by the unit vector  $\vec{v}$  to the direction of the axis oriented by the unit vector  $\vec{n}$ . In the case when these two vectors  $\vec{n}$  and  $\vec{v}$  are the orthogonal axes orientation this rule comes to the equality of the body mass deviation moment for these axes.

## 10. CONCLUSION

The definitions: (1) of the vector  $\vec{J}_n^{(N)}$  of the mass inertia moment of the body for the axis oriented by the unit vector  $\vec{n}$  through the point  $N$ ; and (8) of the vector  $\vec{D}_n^{(N)}$  of the mass deviation moment at the point  $N$  for the axis oriented by the unit vector  $\vec{n}$ ; are my original contributions in this paper.

The equations (13), (29) and (32) as well as my original results, although these equations we can take as mathematical analogy with corresponding equations from the stress theory of the deformable bodies.

The complete analysis of the mass inertia moment state by the vector  $\vec{J}_n^{(N)}$  of the mass inertia moment of the body for the axis oriented by the unit vector  $\vec{n}$  through the point  $N$  represents the original way for definition and interpretation of kinetic parameters of the rigid bodies.

The analysis of the strain state of the elastic bodies by the vector  $\vec{\delta}_n^{(N)}$  of the total specific deformation (strain) for the unit vector  $\vec{n}$  drawn from the point  $N$  also is original way, but less original than previous results.

Everything that has been said leads us to conclude that there exists a very fruitful analogy based on the possibility to use mathematical models for the explanations of various parameters and the systems of physical and geometric quantities. Such an approach enables various simplifications.

## ACKNOWLEDGMENT

*I dedicate this paper to my dear and highly respected late Professor ph. D. Dipl. Math. Danilo Rašković, who introduced the vector interpretations into the University program of Mechanics, which he loved very much.*

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## ANALOGIJE MODELA STANJA NAPONA, STANJA DEFORMACIJE I STANJA MOMENTA INERCIJE MASE NAPREGNUTOG DEFORMABILNOG TELA

Katica (Stevanović) Hedrih

U radu se uvode pojmovi: vektora  $\delta_n^{(N)}$  totalne specifične deformacije za linijski element povučen iz tačke  $N$  u pravcu određenog jediničnog vektora  $i$  i vektora  $\tilde{J}_n^{(N)}$  momenta inercije masa tela za osu povučenu iz iste tačke  $i$  pomoću njih  $i$  vektora totalnog napona za ravan određene normale analiziraju modeli stanja napona, stanja deformacije i stanja momenata inercije masa u posmatranoj tački tela i ukazuje na identičnost matematičkih modela. Koristeći pojmove tenzora napona, tenzora momenata inercije i tenzora specifične deformacije ističe se analogija pojmova, fizičkih i geometrijskih veličina modela stanja napona, stanja deformacija i stanja inercije masa tela. Na osnovu te analogije izveden je niz zaključaka u teoriji deformacija i o momentima inercije masa tela.



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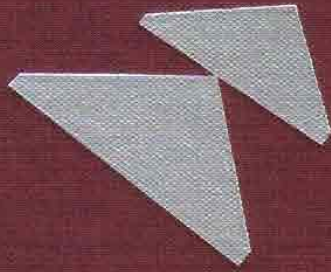
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# Application of Fractional Calculus for Dynamic Problems of Solid Mechanics: Novel Trends and Recent Results

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*The present state-of-the-art article is devoted to the analysis of new trends and recent results carried out during the last 10 years in the field of fractional calculus application to dynamic problems of solid mechanics. This review involves the papers dealing with study of dynamic behavior of linear and nonlinear 1DOF systems, systems with two and more DOFs, as well as linear and nonlinear systems with an infinite number of degrees of freedom: vibrations of rods, beams, plates, shells, suspension combined systems, and multilayered systems. Impact response of viscoelastic rods and plates is considered as well. The results obtained in the field are critically estimated in the light of the present view of the place and role of the fractional calculus in engineering problems and practice. This articles reviews 337 papers and involves 27 figures. [DOI: 10.1115/1.4000563]*

**Keywords:** fractional integrodifferentiation, free vibrations of viscoelastic systems with finite and infinite number degrees of freedom, impact response

## 1 Introduction

The authors' first state-of-the-art article [1] devoted to the application of fractional calculus in dynamic problems of solids was published in *Applied Mechanics Reviews* in January, 1997. 13 years have elapsed since its appearance. A rich variety of papers dealing with fractional calculus and its application to the problems of mechanics have appeared in scientific literature in this period, among them reviews [2–8] and monographs [9,10]. All technical articles in the field can be classified into two main groups:

- papers developing analytical approaches and methods
- papers utilizing numerical approaches and methods.

A list of papers from the *second group* is much longer than that of the *first group* since new analytical results are few and far between. Moreover, those papers fallen into the first group are mainly concerned with investigation of vibrations of 1DOF systems and fractional oscillators. *Fractional oscillator* is a notion that appears recently in the literature, principally in the field of physics, for an oscillator with the second derivative replaced by a fractional one of order less than 2, in so doing Riemann–Liouville, Grünvald–Letnikov, Caputo, or Riesz definitions for the general fractional differintegral have been utilized. But for mechanical and civil engineering applications, the introduction of a fractional derivative into inertial terms of equations of motion is neither attractive nor justified. In engineering practice, fractional derivatives are useful for describing viscoelastic features of advanced materials or dissipative forces in structural dynamics [1,3–7].

As for the second group, then in the majority of papers from this group, numerical methods are also applied to the simplest mechanical systems, such as oscillators and rods. Analysis of intricate mechanical systems is rather rare in occurrence.

Different numerical methods, such as finite-element and boundary element simulations, the method of finite differences with its modifications, and other numerical algorithms, are of frequent use

for integration of equations of motion of fractionally damped structures in the time-domain as well as in the Laplace or Fourier domain. Some authors have utilized Grünvald–Letnikov definition for the fractional differintegral, while others preferred to develop various iterative algorithms for its evaluation. In regard to the methods of numerical treatment of integrodifferential equations of fractional order utilizing in various problems of mechanics, then the interesting reader can find their wide overview in Refs. [4,11–17] with references therein.

The present state-of-the-art article is devoted to the analysis of new trends and recent results carried out during the last years in the field of fractional calculus application to dynamic problems of solid mechanics and structural mechanics. When writing the second survey, the authors have been guided by the considerations that it should not repeat the first review [1], while it should be its logical continuation. Since all main definitions of a fractional derivative and fractional integral, as well as the detailed description of the simplest rheological models involving fractional derivatives, have been considered in Ref. [1], then we will not return to these questions here and refer the interesting reader to Ref. [1] or/and Refs. [2,8,9].

This review will focus on the papers dealing with study of dynamic behavior of linear and nonlinear 1DOF systems, systems with two and more DOF, as well as linear and nonlinear systems with infinite-number-degree-of-freedom: vibrations of rods, beams, plates, shells, suspension combined systems, and multilayered systems. Impact response of viscoelastic rods and plates will be considered as well. The results obtained in the field are critically estimated in the light of the present view of the place and role of the fractional calculus in engineering problems and practice.

Since this article is dedicated mainly to the audience of researchers and practicing engineers in the field of mechanical and civil engineering, then hereafter terms *fractional oscillator* and *fractionally damped structure* would mean application of fractional calculus representations for describing damping forces in governing equations of motion.

It might be well to point out that the analytical approaches and methods for studying the fractionally damped mechanical systems will be analyzed in more detail in the given paper. As for the

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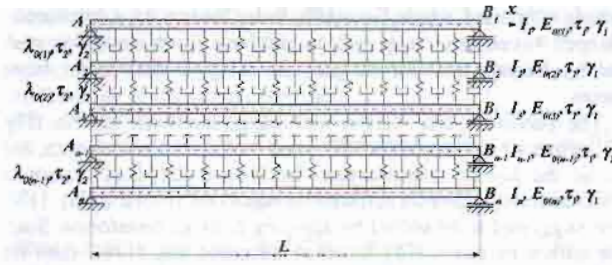


Fig. 23 Scheme of a multibeam system

equations describing the dynamic response of viscoelastic beams can be found in Ref. [69]. Zhu et al. [69] studied steady-state response of a simply supported fractionally damped beam under a simple harmonic excitation. The viscoelastic material of the beam is assumed to be homogeneous and isotropic, and its volume deformation is supposed to obey the elastic deformation law, while for pure shear deformation, it is assumed that the material obeys the three-dimensional fractional derivative standard linear solid model constitutive relations. The equations of motion were derived for a Timoshenko-type beam, and particular cases neglecting the rotary inertia and/or transverse shear deformations were discussed as well. Using the modal analysis approach, the solution was obtained for the beam's deflection and rotational angle

$$v(x,t) = \sum_{n=1}^{\infty} (A_n \sin \Omega t + B_n \cos \Omega t) \sin\left(\frac{n\pi x}{L}\right) \quad (173a)$$

$$\varphi(x,t) = \sum_{n=1}^{\infty} (C_n \sin \Omega t + D_n \cos \Omega t) \sin\left(\frac{n\pi x}{L}\right) \quad (173b)$$

where  $\Omega$  is the frequency of the excitation, and  $A_n, B_n, C_n,$  and  $D_n$  are some coefficients defined in Ref. [69].

Further the same authors suggested a numerical method for solving weakly singular Volterra integrodifferential equations arising in the above mentioned problem [71]. The analytical and numerical results were compared, and a good correspondence between them was reported.

**4.2.5 Solution in Terms of Series.** The decomposition method, when the solution is sought in the form of the series (27), was utilized by Liang and Tang [308] to solve Eq. (158) with the fractional derivative damping term of an arbitrary order  $0 < \gamma < 1$ , in so doing, the forcing function is assumed as the product of a specified space-dependent deterministic function and a time-dependent process. For particular case of a simply supported beam subjected to a unit impulse load, the general solution was written in the form of an infinite series similar to Eq. (30). The numerical example was presented for the case of the first mode approximation, which is equivalent to one fractional oscillator idealization of the beam. Calculations were done by truncating the infinite series (30) to 16 terms.

The approach for solving the fractional differential equation obtained for the generalized displacement function of a fractionally damped rod [294] was utilized by Hedrih [307] when considering free transversal vibrations of a two-layered straight beam, which layers were made of inhomogeneous continuously creeping materials simulated by fractional derivative Kelvin-Voigt model. In the case of the simply supported beam, the problem was reduced to the same equation of the fractional derivative Kelvin-Voigt oscillator as in Ref. [294], and, thus, its time series form solution coincides with that of Refs. [297,294].

**4.2.6 A Viscoelastic Beam With Nonhomogeneity Varying With Its Height.** One of the approaches for simulating multilayered structures is to consider a sandwich structure as a multibeam or

multiplate system, in which deformable elastic or viscoelastic bodies (beams or plates) are interconnected by distributed light viscoelastic constraint elements which have the ability to resist axial deformation under static and dynamic conditions [315].

Let us consider a discrete-continuum inhomogeneous vertical chain system (Fig. 23) involving a set of  $N$  viscoelastic beams with different material constants but with the same boundary contours and boundary conditions, which are interconnected by  $N - 1$  viscoelastic constraint layers with equal material constants. The number of degrees of freedom of such a multilayered structure is equal to  $N$ -infinity, where  $N$  is a number of deformable beams in the chain, in so doing, each Bernoulli-Euler beam admits the dynamic deflection  $v_i(x,t)$ . The origins of the corresponding  $N$  coordinate systems are  $N$  corresponding sets at the corresponding centers in the undeformed beams' middle surfaces, as shown in Fig. 23 and with parallel corresponding axes. The beams may be subjected to a transversal distributed external loads  $q_i(x,t)$  ( $i=1,2,\dots,N$ ) along corresponding beams' external surfaces.

The dynamic response of such a viscoelastic layer connected multiple beam system, or a sandwiched beam, can be described by the following system of the  $N$  governing coupled partial differential equations:

$$\widetilde{E}_i I_i \frac{\partial^4 v_i}{\partial x^4} + \rho_i A_i \ddot{v}_i = q_i + F_{i+1} - F_i \quad (i=1,2,\dots,N) \quad (174a)$$

$$F_1 = \widetilde{\lambda}_1 v_1, \quad F_i = \widetilde{\lambda}_i (v_i - v_{i-1}) \quad (i=2,3,\dots,N-1), \quad F_N = \widetilde{\lambda}_N v_N \quad (174b)$$

formulated in terms of  $N$  unknown transversal displacements  $v_i(x,t)$ , where  $F_i$  is the reaction of the  $i$ th viscoelastic layer, Young's modulus  $\widetilde{E}_i$  of the  $i$ th beam and the coefficient of rigidity of the connecting viscoelastic layer  $\widetilde{\lambda}$  are the following Kelvin-Voigt type operators of the fractional order:

$$\widetilde{E}_i = E_{0(i)}(1 + \tau_1^{\gamma_1} D^{\gamma_1}), \quad \widetilde{\lambda}_j = \lambda_{0(j)}(1 + \tau_2^{\gamma_2} D^{\gamma_2}) \quad (174c)$$

and  $E_{0(i)}$  and  $\lambda_{0(j)}$  are prolonged magnitudes of coefficients of rigidity for the  $i$ th beam and  $j$ th layer, respectively,  $\tau_1, \gamma_1$  and  $\tau_2, \gamma_2$  are the retardation time and fractional parameter for the beams and layers, respectively.

Note that adding the  $N$ th layer to this system allows one to consider the dynamic response of a multilayered beam on a viscoelastic foundation in the same manner as in Sec. 4.2.4.

Supposing the solution of Eq. (174a)-(174c) in the modal form

$$v_i(x,t) = \sum_{n=1}^{\infty} \varphi_n(x) T_{(i)n}(t), \quad i=1,2,\dots,N \quad (175)$$

substituting Eqs. (175), (174b), and (174c) into Eq. (174a), multiplying each equation by  $\varphi_k(x)$ , after integrating along the beams' length  $L$ , and taking into account orthogonality conditions and corresponding equal boundary conditions of the beams, we are led to the  $n$ -family of systems containing coupled only  $N$ -ordinary fractional-order differential equations for the determination of unknown generalized displacement functions  $T_{(i)n}(t)$  ( $i=1,2,\dots,N, n=1,2,\dots,\infty$ ),

$$\begin{aligned} \ddot{T}_{(i)n} + \omega_{(i)n}^2 (1 + \tau_1^{\gamma_1} D^{\gamma_1}) T_{(i)n} + \frac{\lambda_{0(i)} + \lambda_{0(i+1)}}{\rho_i A_i} (1 + \tau_2^{\gamma_2} D^{\gamma_2}) T_{(i)n} \\ - \frac{\lambda_{0(i+1)}}{\rho_i A_i} (1 + \tau_2^{\gamma_2} D^{\gamma_2}) T_{(i+1)n} - \frac{\lambda_{0(i)}}{\rho_i A_i} (1 + \tau_2^{\gamma_2} D^{\gamma_2}) T_{(i-1)n} = P_{(i)n}(t) \end{aligned} \quad (176)$$

where



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**THE DISSIPATION FUNCTION OF  
A NONCONSERVATIVE SYSTEM OF MASS PARTICLES.**

By Katica (Stevanović) HEDRIH.

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## THE DISSIPATION FUNCTION OF A NONCONSERVATIVE SYSTEM OF MASS PARTICLES.

*On occasion of the Anniversary of "Akitsugu Kawaguchi's 100 years birth",  
who is the Founder of Tensor Society.*

By Katica (Stevanović) HEDRIH.

**Abstract.** The paper presents the determination of a class of generalized Rayleigh's dissipation functions, which correspond to dissipative force proportional to  $p$ -step of the velocity of the material particles, as well as corresponding extend generalized relation between the generalized Rayleigh's dissipation function and the rate of system energy dissipation (degradation) for the systems with holonomic rheonomic and/or scleronomic constraints.

**Introduction.** The description of mechanics of a system of material particles would be unrealistic if the absence of dissipative or frictional forces would be assumed. In many physical systems these forces, when present, are proportional to particle velocities and can therefore be derived as a dissipation function (see Ref. [2]<sup>1</sup>, [8]).

Book *Theory of Sound* by Lord Rayleigh [2], [8], is one of the old classic monograph of physics literature. This treatise contains a wealth of theorem and physical illustrations on all of the aspects of vibration theory, and is very concurrent. Rayleigh himself was responsible for introduction of the *dissipation function* into vibration theory.

In the classical monographs F. Gantmaher [1] and H. Goldstein [2] are treatises, which contain fundamentals of the analytical mechanics. The series of papers by V. V. Rumyantsev contain current knowledge on analytical mechanics, and especially Ref. [9] present an introduction in the general theory of general and generalized Poincaré's and Chetaev's differential equations system based on a closed system of infinitesimal operators. These equations include both the motion equations in independent and dependent, holonomic and nonholonomic coordinates for holonomic and nonholonomic mechanical systems with finite number of degrees of freedom. In this sense Poincaré-Chetaev-Rumyantsev's equations [14] are general equations of analytical dynamics.

In monographs [11], [12] V. A. Vujičić gave a modification of the analytical mechanics of rheonomic systems, with the aim to include the influence of nonstationary constraints into the laws of motion. In his approach, rheonomic coordinate is chosen

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1) Numbers in brackets refer to the references at the end of the paper.



as a function derived from rheonomic constraints. On this basis, an extended system of Lagrangian equations was formulated with an additional equation corresponding to rheonomic coordinate. In the paper by Vujičić and Hedrih [13] the rheonomic constraints generalized force in the extension of the Lagrange's system of differential equations of motion of the first and the second kind is introduced. In the paper by K. Hedrih [3] the power of the rheonomic constraints change is introduced.

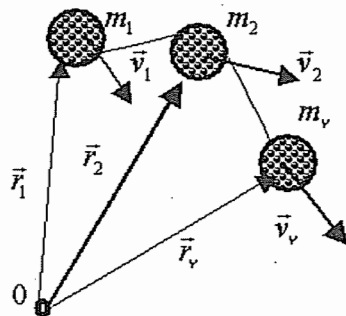
In the paper Dj. Mušicki [5], [6] formulated a new parametric formulation of mechanics and based on the separation of the double role of time (independent variable and a parameter) with the aid of a family of varied paths. These results are extended to arbitrary rheonomic systems with variable mass. Also, the same general principles of mechanics and the energy relations for such systems are studied.

In the university book by D. P. Rašković [8] the Lagrange's equations of the motion of mass particles nonconservative system expressed by using Rayleigh's dissipation function which corresponds to the dissipative force proportional to the velocity of the material particle, based on the Theory of Sound by Lord Rayleigh. In the Ref. [8], [2], for nonconservative system of mass particles nonconservative system with holonomic scleronomic constraints with dissipative force proportional to the velocity of the material particle, we can find relation between system energy and Rayleigh's dissipation function. This formulation is: Duplicate of the Rayleigh's dissipation function is the rate of system energy dissipation (degradation).

J. J. Stoker in the Ref. [10] presented example of the heavy material particle pendulum nonlinear dynamics in the turbulent field damping with corresponding phase portrait and constant energy curves.

References [8] and [10] and Rayleigh's dissipation function which corresponds to the dissipative force proportional to the velocity of the material particle are inspiration for me to define a new class of generalized Rayleigh's dissipation functions which correspond to the dissipative force proportional to  $p$ -step of the velocities of the material particles, as well as corresponding extend generalized relation between the generalized Rayleigh's dissipation function and the rate of system energy dissipation (degradation).

**§ 1. Kinetic and potential energy.** Now, we will consider a discrete system of  $N$  material particles with masses  $m_\nu$ ,  $\nu = 1, 2, 3, \dots, N$ , which positions are defined by corresponding position vectors in the forms of vector functions  $\vec{r}_\nu(q^k, t)$ ,  $\nu = 1, 2, 3, \dots, N$ ;  $k = 1, 2, 3, \dots, n = 3N - s$  where  $s$  is number of holonomic rheonomic constraints  $f_\alpha(\vec{r}^j, t) = 0$ ,  $\alpha = 1, 2, 3, \dots, s$ . By  $q^k$ ,  $k = 1, 2, 3, \dots, n = 3N - s$  are denoted generalized coordinates. By using form of the one of the rheonomic constraints we can introduce rheonomic coordinate [11] in the form of  $q^0 = g(t)$ . By introducing other rheonomic constraints, position radius vectors of material particles we can express with respect to the extended system of the generalized coordinates  $q^k$ ,  $k = 1, 2, 3, \dots, n = 3N - s$  with rheonomic coordinate  $q^0$ . Extended system of generalized coordinates have  $n + 1$  generalized coordinates:  $q^k$ ,  $k = 0, 1, 2, 3, \dots, n$ ,  $n = 3N - s$  and the position vectors of the material particles  $m_\nu$ ,  $\nu = 1, 2, 3, \dots, N$  we can express in the form:  $\vec{r}_\nu(q^0, q^1, q^2, \dots, q^n)$ .



Velocities of the material particles  $m_\nu$ ,  $\nu = 1, 2, 3, \dots, N$  of the system is:

$$\vec{v}_\nu = \sum_{i=1}^n \frac{\partial \vec{r}_\nu}{\partial q^i} \dot{q}^i + \frac{\partial \vec{r}_\nu}{\partial q^0} \dot{q}^0.$$

Kinetic energy of motion of the material particles system is:

$$E_k = \frac{1}{2} \sum_{\nu=1}^N m_\nu (\vec{v}_\nu, \vec{v}_\nu) = \frac{1}{2} \sum_{i=0}^n \sum_{j=0}^n A_{ij} \dot{q}^i \dot{q}^j,$$

where, for consideration of a special class of rheonomic systems,  $q^0 = \Omega t$  is rheonomic coordinate, which corresponds to the rotation angle,  $\Omega$  is angular velocity, and introduced notations for coefficients of system inertia-functions  $A_{ij}$  are:

$$A_{ij} = \sum_{\nu=1}^N m_\nu \left( \frac{\partial \vec{r}_\nu}{\partial q^i}, \frac{\partial \vec{r}_\nu}{\partial q^j} \right), \quad i, j = 0, 1, 2, 3, \dots, n.$$

Potential energy expression is:

$$E_p = E_p(\vec{r}_1, \vec{r}_2, \vec{r}_3, \dots, \vec{r}_\nu, \dots, \vec{r}_N, q^0) = E_p(q^1, q^2, q^3, \dots, q^i, \dots, q^n, q^0).$$

For the system equilibrium position the following conditions must be satisfied:  $(\frac{\partial E_p}{\partial q^i})_{q^i=q^i0} = 0$ . The generalized conservative system forces which have potential can write:

$$Q_i = -\frac{\partial E_p}{\partial q^i}, \quad i = 0, 1, 2, 3, \dots, n.$$

**§ 2. Dissipative forces and Rayleigh's dissipative functions.** If the friction forces  $\vec{F}_{w,\nu}$ ,  $\nu = 1, 2, 3, \dots, N$ , are present to the material particles  $m_\nu$ ,  $\nu = 1, 2, 3, \dots, N$  in rest conditions, and are different them zero, than these forces are dry friction forces. These friction forces can be sliding friction or rolling friction forces. If a material particle is constrained to move on a stationary surface and the force of constraint is not perpendicular to the surface, than the sliding friction force are

present. The friction is essentially a macroscopic phenomenon [15]. Phenomena related to dry friction appear in poorly lubricated or non-lubricated contact surfaces of bodies in relative motion. The classical model of a system with dry friction forces develop between the base and the body contact surface, which can be modelled by a material particle moving on a slider. Friction forces naturally appear between two bodies in motion.

If the dissipative friction forces,  $\vec{F}_{w,\nu}(\vec{v}_\nu) \neq 0$ ,  $\nu = 1, 2, 3, \dots, N$ , are present to the material particles  $m_\nu$ ,  $\nu = 1, 2, 3, \dots, N$  at the motion in the dissipative space, and in rest are equal to zero,  $\vec{F}_{w,\nu}(\vec{v}_\nu, t)|_{\vec{v}_\nu=0} = 0$ , than these forces are viscous friction forces or turbulent friction forces. The friction forces of the real constraints appear in the general case as a function of velocities and positions into dissipative space.

Let we define the dissipative forces  $\vec{F}_{w,\nu}(\vec{v}_\nu) \neq 0$ ,  $\nu = 1, 2, 3, \dots, N$ , which are present in material particles  $m_\nu$ ,  $\nu = 1, 2, 3, \dots, N$  during motion with velocities  $\vec{v}_\nu$ :

$$\vec{F}_{w,\nu} = \begin{cases} -b_\nu(\vec{v}_\nu, \vec{v}_\nu)^{p-1}\vec{v}_\nu \\ -b_\nu(\vec{v}_\nu, \vec{v}_\nu)^{p-1}|\vec{v}_\nu|\vec{v}_\nu \end{cases}, \quad p = 1, 2, 3, \dots,$$

where  $b_\nu$  and  $p$  are dissipative force coefficients.

Corresponding dissipative function:

$$\Phi(\vec{v}_1, \vec{v}_2, \dots, \vec{v}_N) = \begin{cases} \sum_{\nu=1}^N \frac{b_\nu}{2p} (\vec{v}_\nu, \vec{v}_\nu)^p \\ \sum_{\nu=1}^N \frac{b_\nu}{2p+1} (\vec{v}_\nu, \vec{v}_\nu)^p |\vec{v}_\nu| \end{cases}, \quad p = 1, 2, 3, \dots$$

Dissipative forces  $\vec{F}_{w,\nu}(\vec{v}_\nu) \neq 0$  can be expressed by derivative of the scalar dissipative function  $\Phi(\vec{v}_1, \vec{v}_2, \vec{v}_3, \dots, \vec{v}_\nu, \dots, \vec{v}_N)$  with respect to the  $\nu$ -th material particles velocities  $\vec{v}_\nu$  with opposite direction:

$$\vec{F}_{w,\nu}(\vec{v}_\nu) = -\frac{\partial \Phi(\vec{v}_1, \vec{v}_2, \vec{v}_3, \dots, \vec{v}_\nu, \dots, \vec{v}_N)}{\partial \vec{v}_\nu}, \quad \nu = 1, 2, 3, 4, \dots, N.$$

Generalized forces, which correspond to the dissipative forces, are denoted by  $Q_{w,k}$ ,  $k = 0, 1, 2, 3, \dots, n$ , and expressed by following relation:

$$\begin{aligned} \delta A^{\Sigma \vec{F}_{w,\nu}} &= \sum_{\nu=1}^N (\vec{F}_{w,\nu}, \delta \vec{r}_\nu) = \sum_{k=0}^n \left( \sum_{\nu=1}^N \vec{F}_{w,\nu}, \frac{\partial \vec{r}_\nu}{\partial q^k} \right) \delta q^k \\ &= \sum_{k=0}^n \left( \sum_{\nu=1}^N \vec{F}_{w,\nu}, \frac{\partial \vec{v}_\nu}{\partial \dot{q}^k} \right) \delta q^k = \sum_{k=0}^n Q_{w,k} \delta q^k, \\ Q_{w,k} &= \sum_{\nu=1}^N \left( \vec{F}_{w,\nu}, \frac{\partial \vec{r}_\nu}{\partial q^k} \right) = \sum_{\nu=1}^N \left( \vec{F}_{w,\nu}, \frac{\partial \vec{v}_\nu}{\partial \dot{q}^k} \right), \end{aligned} \tag{2.1}$$

where  $\delta A^{\Sigma \vec{F}_{w,\nu}}$  are work of the dissipative forces in the arbitrary infinitesimal displacements  $\delta \vec{r}_\nu$ .

We multiplied relation (2.1) with  $\delta \dot{q}^k$  and summarize left and right side with respect to index  $k$  from zero to  $n$ , and we obtained possible variation of the work of dissipative forces with respect to a unit of time, or rate of possible variation of dissipative energy, or possible variation of power of dissipative forces in following form:

$$\sum_{k=0}^n Q_{w,k} \delta \dot{q}^k = \sum_{k=0}^n \sum_{\nu=1}^N \left( \vec{F}_{w,\nu}, \frac{\partial \vec{v}_\nu}{\partial \dot{q}^k} \right) \delta \dot{q}^k = \sum_{\nu=1}^N \left( \vec{F}_{w,\nu}, \sum_{k=0}^n \frac{\partial \vec{v}_\nu}{\partial \dot{q}^k} \delta \dot{q}^k \right),$$

$$\sum_{k=0}^n Q_{w,k} \delta \dot{q}^k = \sum_{\nu=1}^N (\vec{F}_{w,\nu}, \delta \vec{v}_\nu).$$

Let consider the special cases:

a\* The dissipative forces are linearly proportional to the velocity  $\vec{v}_\nu$  of the corresponding material particle:  $\vec{F}_{w,\nu} = -b_\nu \vec{v}_\nu$  and with opposite direction to the velocity. Generalized dissipative forces (2.1) of this type may be derived in terms of the dissipative function:

$$Q_{w,k} = \sum_{\nu=1}^N \left( \vec{F}_{w,\nu}, \frac{\partial \vec{v}_\nu}{\partial \dot{q}^k} \right) = - \sum_{\nu=1}^N b_\nu \left( \vec{v}_\nu, \frac{\partial \vec{v}_\nu}{\partial \dot{q}^k} \right)$$

$$= - \sum_{\nu=1}^N \frac{\partial}{\partial \dot{q}^k} \left[ \frac{1}{2} b_\nu (\vec{v}_\nu, \vec{v}_\nu) \right] = - \frac{\partial \Phi(\dot{q}^0, \dot{q}^1, \dot{q}^2, \dots, \dot{q}^k, \dots, \dot{q}^n)}{\partial \dot{q}^k}.$$

For that case dissipative function is defined as:

$$\partial \Phi(\dot{q}^0, \dot{q}^1, \dot{q}^2, \dots, \dot{q}^k, \dots, \dot{q}^n) = \sum_{\nu=1}^N \frac{1}{2} b_\nu (\vec{v}_\nu, \vec{v}_\nu).$$

This function is known as Rayleigh's dissipation function.

b\* The dissipative forces are proportional to the square of the velocity  $\vec{v}_\nu$  of the corresponding material particle:  $\vec{F}_{w,\nu} = -b_\nu |\vec{v}_\nu| \vec{v}_\nu$  and with opposite direction to the velocity. Generalized dissipative forces of this type may be derived in terms of the dissipative function:

$$Q_{w,k} = - \sum_{\nu=1}^N b_\nu \left( |\vec{v}_\nu| \vec{v}_\nu, \frac{\partial \vec{v}_\nu}{\partial \dot{q}^k} \right) = - \sum_{\nu=1}^N \frac{\partial}{\partial \dot{q}^k} \left[ \frac{1}{3} b_\nu |\vec{v}_\nu| (\vec{v}_\nu, \vec{v}_\nu) \right]$$

$$= - \frac{\partial \Phi(\dot{q}^0, \dot{q}^1, \dot{q}^2, \dots, \dot{q}^k, \dots, \dot{q}^n)}{\partial \dot{q}^k}.$$

For that case dissipative function is defined as:

$$\Phi(\dot{q}^0, \dot{q}^1, \dot{q}^2, \dots, \dot{q}^k, \dots, \dot{q}^n) = \sum_{\nu=1}^N \frac{1}{3} b_\nu |\vec{v}_\nu| (\vec{v}_\nu, \vec{v}_\nu).$$

c\* The dissipative forces are proportional to the  $\bar{p} = 2p$ ,  $p = 1, 2, 3, \dots, K$ -th degree of the velocity  $\vec{v}_\nu$  of the corresponding material particle:  $\vec{F}_{w,\nu} = -b_\nu(\vec{v}_\nu, \vec{v}_\nu)^{p-1} |\vec{v}_\nu| \vec{v}_\nu$  and with opposite direction to the velocity. Generalized dissipative forces of this type may be derived in terms of the dissipative function:

$$Q_{w,k} = - \sum_{\nu=1}^N b_\nu \left( (\vec{v}_\nu, \vec{v}_\nu)^{p-1} |\vec{v}_\nu| \vec{v}_\nu, \frac{\partial \vec{v}_\nu}{\partial \dot{q}^k} \right) = - \sum_{\nu=1}^N \frac{\partial}{\partial \dot{q}^k} \left[ \frac{1}{2p+1} b_\nu |\vec{v}_\nu| (\vec{v}_\nu, \vec{v}_\nu)^p \right].$$

For that case dissipative function is defined as:

$$\Phi(\dot{q}^0, \dot{q}^1, \dot{q}^2, \dots, \dot{q}^k, \dots, \dot{q}^n) = \sum_{\nu=1}^N \frac{1}{2p+1} b_\nu |\vec{v}_\nu| (\vec{v}_\nu, \vec{v}_\nu)^p.$$

d\* The dissipative forces are proportional to the  $\bar{p} = 2p - 1$ ,  $p = 1, 2, 3, \dots, K$ -th degree of the velocity  $\vec{v}_\nu$  of the corresponding material particle:  $\vec{F}_{w,\nu} = -b_\nu(\vec{v}_\nu, \vec{v}_\nu)^{p-1} \vec{v}_\nu$  and with opposite direction to the velocity. Generalized dissipative forces of this type may be derived in terms of the dissipative function:

$$Q_{w,k} = - \sum_{\nu=1}^N b_\nu \left( (\vec{v}_\nu, \vec{v}_\nu)^{p-1} \vec{v}_\nu, \frac{\partial \vec{v}_\nu}{\partial \dot{q}^k} \right) = - \sum_{\nu=1}^N \frac{\partial}{\partial \dot{q}^k} \left[ \frac{1}{2p} b_\nu (\vec{v}_\nu, \vec{v}_\nu)^p \right].$$

For that case dissipative function is defined as:

$$\Phi(\dot{q}^0, \dot{q}^1, \dot{q}^2, \dots, \dot{q}^k, \dots, \dot{q}^n) = \sum_{\nu=1}^N \frac{1}{2p} b_\nu (\vec{v}_\nu, \vec{v}_\nu)^p.$$

From previous considerations we may generalize the relation between generalized dissipative force and dissipative function:

$$Q_{w,k} = - \frac{\partial \Phi(\dot{q}^0, \dot{q}^1, \dot{q}^2, \dots, \dot{q}^k, \dots, \dot{q}^n)}{\partial \dot{q}^k}.$$

§ 3. Work of the dissipative forces in unit of time. Let us determine the sum  $\sum_{k=0}^n Q_{w,k} \dot{q}^k$  for previously considered law of dissipative forces with respect to material particles velocities of the system with  $n$  degrees of freedom:

$$(3.1) \quad \sum_{k=0}^n Q_{w,k} \dot{q}^k = \sum_{k=0}^n \sum_{\nu=1}^N \left( \vec{F}_{w,\nu}, \frac{\partial \vec{v}_\nu}{\partial \dot{q}^k} \right) \dot{q}^k = \sum_{\nu=1}^N \left( \vec{F}_{w,\nu}, \sum_{k=0}^n \frac{\partial \vec{r}_\nu}{\partial \dot{q}^k} \dot{q}^k \right) \\ = \sum_{\nu=0}^N (\vec{F}_{w,\nu}, \vec{v}_\nu) = \frac{dA^{\Sigma \vec{F}_{w,\nu}}}{dt},$$

where  $\frac{dA^{\Sigma \vec{F}_{w,\nu}}}{dt}$  is the work of dissipative forces with respect to the unit of time, or rate of dissipative energy, or power of dissipative forces.

Now, let us determine the work of dissipative forces with respect to a unite of time  $\frac{dA^{\Sigma\bar{F}_{w,\nu}}}{dt}$ , or power of dissipative forces for previous considered generalized cases of defined dissipative forces.

a\* For the case:  $\bar{F}_{w,\nu} = -b_\nu(\bar{v}_\nu, \bar{v}_\nu)^{p-1}|\bar{v}_\nu|\bar{v}_\nu$  for  $\bar{p} = 2p, p = 1, 2, 3, \dots, K$ .

$$\begin{aligned}
 (3.2) \quad \frac{dA^{\Sigma\bar{F}_{w,\nu}}}{dt} &= \sum_{\nu=1}^N (\bar{F}_{w,\nu}, \bar{v}_\nu) = - \sum_{\nu=1}^N b_\nu((\bar{v}_\nu, \bar{v}_\nu)^{p-1}|\bar{v}_\nu|\bar{v}_\nu, \bar{v}_\nu) \\
 &= - \sum_{\nu=1}^N [b_\nu|\bar{v}_\nu|(\bar{v}_\nu, \bar{v}_\nu)^p] = -(2p+1)\Phi(\bar{v}_1, \bar{v}_2, \bar{v}_3, \dots, \bar{v}_\nu, \dots, \bar{v}_N) \\
 &= -(2p+1)\Phi(\dot{q}^0, \dot{q}^1, \dot{q}^2, \dots, \dot{q}^k, \dots, \dot{q}^n).
 \end{aligned}$$

b\* For the case:  $\bar{F}_{w,\nu} = -b_\nu(\bar{v}_\nu, \bar{v}_\nu)^{p-1}\bar{v}_\nu$ , for  $\bar{p} = 2p-1, p = 1, 2, 3, \dots, K$ .

$$\begin{aligned}
 (3.3) \quad \frac{dA^{\Sigma\bar{F}_{w,\nu}}}{dt} &= \sum_{k=0}^n Q_{w,k} \dot{q}^k \sum_{\nu=1}^N (\bar{F}_{w,\nu}, \bar{v}_\nu) = - \sum_{\nu=1}^N b_\nu((\bar{v}_\nu, \bar{v}_\nu)^{p-1}\bar{v}_\nu, \bar{v}_\nu) \\
 &= - \sum_{\nu=1}^N [b_\nu(\bar{v}_\nu, \bar{v}_\nu)^p] = -2p\Phi(\bar{v}_1, \bar{v}_2, \bar{v}_3, \dots, \bar{v}_\nu, \dots, \bar{v}_N) \\
 &= -2p\Phi(\dot{q}^0, \dot{q}^1, \dot{q}^2, \dots, \dot{q}^k, \dots, \dot{q}^n).
 \end{aligned}$$

By using previous and by introducing the following scalar  $\lambda$  we can write the following:

$$\begin{aligned}
 \frac{dA^{\Sigma\bar{F}_{w,\nu}}}{dt} - \sum_{i=1}^n \dot{q}^i \frac{\partial\Phi}{\partial\dot{q}^i} &= -\lambda\Phi(\bar{v}_1, \bar{v}_2, \bar{v}_3, \dots, \bar{v}_\nu, \dots, \bar{v}_N) \\
 &= -\lambda\Phi(\dot{q}^0, \dot{q}^1, \dot{q}^2, \dots, \dot{q}^k, \dots, \dot{q}^n).
 \end{aligned}$$

This relation is relation between the power of the dissipation forces and corresponding dissipation function.

**§ 4. The rate of the energy dissipation of nonconservative system having dissipative function.**

**4.1. Nonconservative system, with holonomic scleronomic constraints, having dissipative function.** Let us consider the Lagrange's differential equations of the second kind (see Ref. [2], [7] or [8]) for nonconservative system, with holonomic scleronomic constraints, having dissipative function corresponding to the dissipative forces, and with  $n$  degree of freedom. These equations for generalized coordinates  $q^k, k = 1, 2, 3, \dots, n = 3N - s$  are in the following form:

$$(4.1) \quad \frac{d}{dt} \frac{\partial E_k}{\partial \dot{q}^i} - \frac{\partial E_k}{\partial q^i} + \frac{\partial E_p}{\partial q^i} + \frac{\partial \Phi}{\partial \dot{q}^i} = 0, \quad i = 1, 2, 3, \dots, n.$$

We multiplied equations (4.1) with  $\dot{q}^i$  and summarize left side with respect to index  $i$  from 1 to  $n$ , and we obtain the following:

$$\frac{d}{dt} \left[ \sum_{i=1}^n \left( \dot{q}^i \frac{\partial E_k}{\partial \dot{q}^i} \right) \right] - \sum_{i=1}^n \left( \dot{q}^i \frac{\partial E_k}{\partial \dot{q}^i} + \dot{q}^i \frac{\partial E_k}{\partial q^i} \right) + \sum_{i=1}^n \dot{q}^i \frac{\partial E_p}{\partial \dot{q}^i} + \sum_{i=1}^n \dot{q}^i \frac{\partial \Phi}{\partial \dot{q}^i} = 0$$

Having in mind relations (3.3), (3.1) and (3.2) previous relation we can rewrite in following form:

$$(4.2) \quad \frac{d(E_k + E_p)}{dt} = \frac{dA^{\Sigma \bar{F}_{w,\nu}}}{dt} = -\lambda \Phi(\vec{v}_1, \vec{v}_2, \vec{v}_3, \dots, \vec{v}_\nu, \dots, \vec{v}_N) \\ = -\lambda \Phi(\dot{q}^1, \dot{q}^2, \dots, \dot{q}^k, \dots, \dot{q}^n),$$

where is  $\lambda = 2p$ , or  $\lambda = 2p + 1$ , scalar parameter depending of previous considered special cases of defined dissipative forces and corresponding dissipative functions.

The relation of the (4.2) is generalized theorem of the rate of energy dissipation. For the previous known Rayleigh's dissipation function corresponding to the dissipation forces linearly proportional to the velocity  $\vec{v}_\nu$  of the corresponding material particle this scalar parameter is equal to 2 (see Ref. [2] and [7], [8]).

**Generalized theorem of the rate of energy dissipation I:** *If in the non-linear nonconservative mass particles system with holonomic scleronomic constraints are present dissipative forces proportional to the  $\bar{p}$ -th degree of the velocity  $\vec{v}_\nu$  of the corresponding material particle, than the corresponding dissipative function multiplied by  $\bar{p} + 1$  is the rate of energy dissipation with respect to time.*

**4.2. Nonconservative system, with holonomic rheonomic constraints, having dissipative function.** Let consider extended system of the Lagrange's differential equations of the second kind (see Ref. [7]) for nonconservative system, with holonomic rheonomic constraints, having dissipative function corresponding to the dissipative forces, and with  $n$  degree of freedom. These equations for generalized coordinates  $q^k$ ,  $k = 1, 2, 3, \dots, n = 3N - s$ , extended by rheonomic coordinate  $q^0$  are in the following form:

$$(4.3) \quad \frac{d}{dt} \frac{\partial E_k}{\partial \dot{q}^i} - \frac{\partial E_k}{\partial q^i} + \frac{\partial E_p}{\partial \dot{q}^i} + \frac{\partial \Phi}{\partial \dot{q}^i} = 0, \quad i = 1, 2, 3, \dots, n, \\ \frac{d}{dt} \frac{\partial E_k}{\partial \dot{q}^0} - \frac{\partial E_k}{\partial q^0} + \frac{\partial E_p}{\partial \dot{q}^0} + \frac{\partial \Phi}{\partial \dot{q}^0} = R_0,$$

where  $R_0$  is rheonomic constraint force.

We multiplied equations (4.3) with  $\dot{q}^i$  including rheonomic coordinate  $q^0$  and summarize left side with respect to index  $i$  from 0 to  $n$ , and we obtain the following:

$$\frac{d(E_k + E_p)}{dt} = \frac{dA^{\Sigma \bar{F}_{w,\nu}}}{dt} = -\lambda \Phi(\dot{q}^0, \dot{q}^1, \dot{q}^2, \dots, \dot{q}^k, \dots, \dot{q}^n) + R_0 \dot{q}^0,$$



where is  $\lambda = 2p$ , or  $\lambda = 2p + 1$ , scalar parameter depending of previous considered special cases of defined dissipative forces and corresponding dissipative functions.

**Generalized theorem of the rate of energy dissipation II:** *If in the non-linear nonconservative mass particles system with holonomic rheonomic constraints are present dissipative forces proportional to the  $\bar{p}$ -th degree of the velocity  $\vec{v}_i$  of the corresponding material particle, than the difference of the corresponding dissipative function multiplied by  $\bar{p} + 1$  and product of rheonomic constraint force and derivative of the rheonomic coordinate with respect to time is the rate of energy dissipation with respect to time.*

In the other formulation: *The difference of the corresponding dissipative function multiplied by  $\bar{p} + 1$  and power of the rheonomic constraints change is the rate of energy dissipation with respect to time.*

**§ 5. Concluding remarks.** The dissipative functions corresponding to dissipative forces proportional to the  $\bar{p}$ -th degree of the velocity  $\vec{v}_i$  of the corresponding material particle, in the nonconservative material particles system, are determined. Two generalized theorem of the rate of energy dissipation with respect to time for the material particles systems with holonomic scleronomic and rheonomic systems are defined.

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### Appendix.

c\* The dissipative forces are proportional to the  $\bar{p} = 2p$ ,  $p = 1, 2, 3, \dots, K$ -th degree of the velocity  $\vec{v}_\nu$  of the corresponding material particle:  $\vec{F}_{w,\nu} = -b_\nu (\vec{v}_\nu, \vec{v}_\nu)^{p-1} |\vec{v}_\nu| \vec{v}_\nu$ . Generalized dissipative forces of this type may be derived in terms of the generalized coordinates:

$$Q_{w,k} = \sum_{\nu=1}^N \left( \vec{F}_{w,\nu}, \frac{\partial \vec{v}_\nu}{\partial \dot{q}^k} \right) = - \sum_{\nu=1}^N \frac{\partial}{\partial \dot{q}^k} \left[ \frac{1}{2p+1} b_\nu \left| \sum_{i=1}^n \frac{\partial \vec{r}_\nu}{\partial q^i} \dot{q}^i \right| \left( \sum_{i=n}^n \sum_{j=n}^n \left( \frac{\partial \vec{r}_\nu}{\partial q^i}, \frac{\partial \vec{r}_\nu}{\partial q^j} \right) \dot{q}^i \dot{q}^j \right)^p \right],$$

$$k = 1, 2, 3, \dots, n.$$

Dissipative function of this type may be derived in terms of the generalized coordinates:

$$\begin{aligned}\Phi(\dot{q}^1, \dot{q}^2, \dots, \dot{q}^k, \dots, \dot{q}^n) &= \sum_{\nu=1}^N \frac{1}{2p+1} b_{\nu} |\vec{v}_{\nu}| (\vec{v}_{\nu}, \vec{v}_{\nu})^p \\ &= \frac{1}{2p+1} \sum_{\nu=1}^N \left[ b_{\nu} \left| \sum_{i=1}^n \frac{\partial \vec{r}_{\nu}}{\partial \dot{q}^i} \dot{q}^i \right| \left( \sum_{i=1}^n \sum_{j=1}^n \left( \frac{\partial \vec{r}_{\nu}}{\partial \dot{q}^i}, \frac{\partial \vec{r}_{\nu}}{\partial \dot{q}^j} \right) \dot{q}^i \dot{q}^j \right)^p \right].\end{aligned}$$

d\* The dissipative forces are proportional to the  $\bar{p} = 2p - 1$ ,  $p = 1, 2, 3, \dots, K$ -th degree of the velocity  $\vec{v}_{\nu}$  of the corresponding material particle:  $\vec{F}_{w,\nu} = -b_{\nu} (\vec{v}_{\nu}, \vec{v}_{\nu})^{p-1} \vec{v}_{\nu}$ . Generalized dissipative forces of this type may be derived in terms of the generalized coordinates:

$$\begin{aligned}Q_{w,k} &= \sum_{\nu=1}^N \left( \vec{F}_{w,\nu}, \frac{\partial \vec{v}_{\nu}}{\partial \dot{q}^k} \right) = - \sum_{\nu=1}^N \frac{\partial}{\partial \dot{q}^k} \left[ \frac{1}{2p} b_{\nu} (\vec{v}_{\nu}, \vec{v}_{\nu})^p \right] \\ &= - \sum_{\nu=1}^N \frac{\partial}{\partial \dot{q}^k} \left[ \frac{1}{2p} b_{\nu} \left( \sum_{i=1}^n \sum_{j=1}^n \left( \frac{\partial \vec{r}_{\nu}}{\partial \dot{q}^i}, \frac{\partial \vec{r}_{\nu}}{\partial \dot{q}^j} \right) \dot{q}^i \dot{q}^j \right)^p \right],\end{aligned}$$

$$k = 1, 2, 3, \dots, n.$$

Dissipative function of this type may be derived in terms of the generalized coordinates:

$$\begin{aligned}\Phi(\dot{q}^1, \dot{q}^2, \dots, \dot{q}^k, \dots, \dot{q}^n) &= \sum_{\nu=1}^N \frac{1}{2p} b_{\nu} (\vec{v}_{\nu}, \vec{v}_{\nu})^p \\ &= \sum_{\nu=1}^N \frac{1}{2p} b_{\nu} \left( \sum_{i=1}^n \sum_{j=1}^n \left( \frac{\partial \vec{r}_{\nu}}{\partial \dot{q}^i}, \frac{\partial \vec{r}_{\nu}}{\partial \dot{q}^j} \right) \dot{q}^i \dot{q}^j \right)^p.\end{aligned}$$